

# Methodology for Analyzing Dissolved Oxygen Consumption in Benthic Chambers

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**Abstract:** Dissolved oxygen (DO) consumption in the sediments of natural aquatic ecosystems occurs by mass flux across the water-sediment interface. This mass flux is determined as either the rate of oxygen consumption in the sediment or the rate of DO diffusion across the diffusive sublayer. The thickness of the diffusive sublayer is determined by the flow conditions in the turbulent water column. Consequently, feedback occurs between the biochemical consumption that occurs in the sediment and the flow that occurs in the water column. Together, these conditions define the DO flux across the water-sediment interface. Benthic chambers have been used to measure this flux in field and experimental conditions. However, these measurements do not account either for the fact that the flow inside a benthic chamber is not representative of field conditions or for the DO consumption in the water column. Thus, they can provide an inaccurate estimation of the sediment DO demanded in the field. This article aims to present and discuss an approach for analyzing a time series of DO depletion inside a benthic chamber. Based on this approach, the processes related to turbulent water transport in the column are separated from the processes that characterize biochemical consumption in the sediments and the water column. Under these conditions, the parameters related to biochemical consumption in the sediments can be used to compute the expected DO demanded of the sediments in field conditions. Sediment samples from a lagoon near the Universidad de Chile campus in Santiago, the capital city of Chile, were used to illustrate the application of the proposed method. In addition, dimensionless numbers were used to define the method's validity and limitations. DOI: 10.1061/(ASCE)EE.1943-7870.0000926. © 2014 American Society of Civil Engineers.

**Author keywords:** Benthic chamber; Sediment oxygen demand; Turbulent diffusion; Experimental methods.

## Introduction

One of the most important variables in aquatic ecosystems is dissolved oxygen (DO) concentration, which defines the viability threshold for life and the dominant chemical speciation of different elements (Wetzel 2001). The DO concentration in a specified volume depends on the DO sources and sinks in the control volume (Odum 1956; Ryther 1956; Herzfeld et al. 2001) and on the DO fluxes across boundaries. These DO exchanges with the surrounding ambient include advective and diffusive fluxes across open boundaries and the diffusive fluxes across the air-water (Guatieri and Guatieri 2008) and water-sediment interfaces (WSI) (Jørgensen and Des Marais 1990; Dade 1993). The DO flux across the WSI, hereafter referred to as  $J$  ( $\text{gO}_2\text{m}^{-2}\text{d}^{-1}$ ), depends on the diffusive transport on both sides of the interface (Jørgensen and Des Marais 1990; Mackenthun and Stefan 1998; O'Connor and Hondzo 2008) and on the rate of DO production and consumption in the sediment (Bouldin 1968; Jørgensen et al. 1983; Kühl and Jørgensen 1992).

Multiple techniques can be used to measure DO flux across the WSI, including DO microprofiles and benthic chambers. DO microprofiles are effective for measuring  $J$  in situ and in the laboratory. Since early applications of this technique (Revsbech et al. 1980a, b), several studies have shown that microprofiles provide detailed information that can be used to quantify mass exchanges across the WSI and biochemical processes in sediments

(e.g., Jørgensen and Revsbech 1985; Jørgensen and Gundersen 1990; de la Fuente 2014). Based on microprofile measurements,  $J$  can be determined in at least five different forms (see Bryant et al. 2010 for a review). However, microprofiles are expensive and fragile instruments that require sophisticated equipment for collecting precise measurements (with a resolution of micrometers) (Kemp et al. 1993; Berg et al. 1998; de la Fuente 2014). Also, their measurements are representative of a very small area of the sediments near the tip of the microelectrode, and it is not clear how to integrate them into larger areas (Kemp et al. 1993; Viollier et al. 2003; Roy et al. 2005). In contrast, benthic chambers are inexpensive, robust, and easily implemented in laboratory and field conditions (Hall et al. 1989; Herzfeld et al. 2001; Viollier et al. 2003; Arega and Lee 2005). Benthic chambers isolate a volume of water from its surrounding fluid. The DO depletion rates within them are used to compute  $J$  (e.g., Sommer et al. 2008; Jahnke et al. 2008; Gao et al. 2012).

The problem with benthic chambers is that the computed  $J$  is only valid for turbulent conditions inside the chamber (Mackenthun and Stefan 1998; Viollier et al. 2003). To address this limitation, Tengberg et al. (2004), Arega and Lee (2005), and Ferrón et al. (2008), among others, studied the hydrodynamic conditions inside benthic chambers for obtaining curves that relate operational conditions (e.g., stirring rate, exchanged-flow rate) to the diffusional mass transfer coefficient,  $k_t$ , which is the turbulent parameter that drives (e.g., Dade et al. 2001). The rate at which gypsum plates in a benthic chamber are dissolved can be used to estimate  $k_t$  inside them (Santschi et al. 1983; Tengberg et al. 2004). As Viollier et al. (2003) pointed out, one of the four basic assumptions required for computing  $J$  in a benthic chamber is that "the hydrodynamic regime inside the chamber does not alter solute exchange across the sediment-water interface as compared to natural conditions." However, the authors also stated that this assumption is not always true,

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Note. This manuscript was submitted on January 21, 2014; approved on November 18, 2014; published online on December 24, 2014. Discussion period open until May 24, 2015; separate discussions must be submitted for individual papers. This paper is part of the *Journal of Environmental Engineering*, © ASCE, ISSN 0733-9372/04014098(11)/\$25.00.

which must be kept in mind during data analysis and interpretation of results.

The purpose of this article is to present a method for analyzing the DO time series inside a benthic chamber which isolates the influence of turbulent transport in the chamber from the rest of the processes. This method can be used to understand the DO consumption rate in sediments without the influence of flow conditions. To illustrate the method, four laboratory experiments were conducted in a benthic chamber with sediment samples collected from the lagoon of a park near the Universidad de Chile campus in Santiago. In addition, DO consumption in the sediments was characterized with DO microprofiles and dimensionless numbers were used to define the proposed method's application range.

The article is organized as follows. First, the theoretical background, experimental apparatus, and proposed method for analyzing DO time series in a benthic chamber are presented. Next, the proposed method and a sensitivity analysis are applied to four experiments. Lastly, results are discussed.

## Materials and Methods

### DO Flux across the WSI

The proposed methodology uses the early conceptual model of Nakamura and Stefan (1994) to compute the downward flux of DO across the WSI,  $J$   $\text{gO}_2 \text{m}^{-2} \text{d}^{-1}$ . This equation can be written as

$$J = k_t \left( C - \frac{J^2}{S} \right) \quad (1)$$

or as

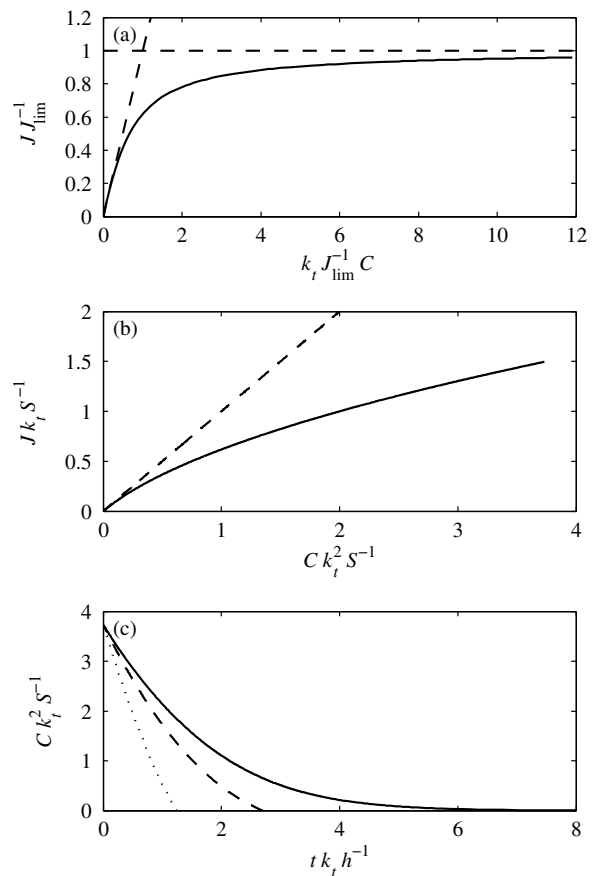
$$J = \frac{S}{2k_t} \left( -1 + \sqrt{1 + \frac{4k_t^2}{S} C} \right) \quad (2)$$

where  $C$  = DO concentration in the water column outside the benthic boundary layer; and  $k_t$  ( $\text{md}^{-1}$ ) = mass transfer velocity or diffusional mass transfer coefficient (Dade 1993; Steinberger and Hondzo 1999; Hondzo et al. 2005).

In addition,  $S = 2\phi R_{O_2} D_s$  ( $\text{gO}_2 \text{m}^{-1} \text{d}^{-2}$ ) is a coefficient that quantifies all of the processes that occur in the sediments, where  $R_{O_2}$  is the bulk rate of volumetric DO consumption  $\text{gO}_2 \text{m}^{-3} \text{d}^{-1}$ ,  $\phi$  is the upper sediment porosity, which can be assumed to be 0.95 (Bryant et al. 2010), and  $D_s$  ( $\text{m}^2 \text{d}^{-1}$ ) is the DO diffusion coefficient, which also depends on porosity (Rasmussen and Jørgensen 1992; Bryant et al. 2010). Here,  $D_s = D\phi$  with  $D$  the molecular diffusion that depends on water temperature. Use of a homogeneous  $R_{O_2}$  is supported by the observations of Kühl and Jørgensen (1992) and Rasmussen and Jørgensen (1992). More discussion on this assumption is given in later sections of this article.

The solution of Eq. (2) is asymptotic to  $J_{\text{lim}} = \sqrt{SC}$  when  $k_t \rightarrow \infty$ . This situation occurs when the biochemical consumption rate limits the  $J$  value. In contrast, when turbulent diffusion across the WSI is the limiting factor (equivalent to large  $S$ ), the  $J$  value is asymptotic to  $k_t C$ . Fig. 1(a) shows the curve  $JJ_{\text{lim}}^{-1}$  as function of  $k_t C J_{\text{lim}}^{-1}$ . Both asymptotic limits are shown in the figure, which depicts the relationship between  $J$  and  $k_t$ . Furthermore, Fig. 1(b) shows the  $Jk_t S^{-1}$  values as a function of  $Ck_t^2 S^{-1}$ , where the limit  $J \approx k_t C$  is represented by the dashed line. This figure represents the relationship between  $J$  and  $C$ .

An alternative mathematical model for computing  $J$  as a function of  $C$  is (Jørgensen and Bendricchi 2001; Hipsey et al. 2014)



**Fig. 1.** (a) Dimensionless DO flux across the WSI as a function of dimensionless transfer velocity [dashed lines = asymptotic values of  $J$  depending on the region in which the flux was limited by turbulent transport (diagonal) or the rate of biochemical consumption in the sediments (horizontal)]; (b) relationship between the dimensionless DO flux across the WSI and the DO concentration (dashed line = asymptotic values of  $J$  in which the flux was limited by turbulent transport); (c) time series of the dimensionless DO concentration in the benthic chamber computed with Eq. (6) [solid line =  $(2k_t r_w / S) = 0$ ; dashed line =  $(2k_t r_w / S) = 0.5$ ; dotted line =  $(2k_t r_w / S) = 2$ ]

$$J = k_s \frac{C}{(k_{O_2} + C)} \quad (3)$$

where  $k_s$  ( $\text{grO}_2 \text{m}^{-2} \text{d}^{-1}$ ) = specific rate of DO consumption in the sediments [determined in a benthic chamber (Jørgensen and Bendricchi 2001)] and  $k_{O_2}$  ( $\text{grO}_2 \text{m}^{-3}$ ) the half-saturation constant for the Michaelis-Menten limitation of  $J$  in terms of  $C$ .

However,  $J$  as computed with Eq. (3) does not include the role of turbulence inside the benthic chamber, so it is not useful for the purposes of this article. A similar situation can be found with another mathematical representation of  $J$  (Jørgensen and Bendricchi 2001; Cole and Buchak 1995) that also neglects the effect of  $k_t$  on  $J$ .

### DO Mass Conservation in Benthic Chambers

If the changes in  $C$  inside a benthic chamber occur over a longer period than the duration of diffusion in the sediments, the accumulation/depletion rate of DO in the sediments can be neglected. In this case, Eq. (2) is assumed to represent the flux across

the WSI for unsteady conditions. With this, the biochemical oxygen demand (BOD) in the water column is included and the mass conservation of DO in a benthic chamber is written as

$$V \frac{dC}{dt} = -AJ - Vr_w = -A \frac{S}{2k_t} \left( \sqrt{1 + \frac{4k_t^2}{S} C} - 1 \right) - Vr_w \quad (4)$$

where  $V$  = volume of the chamber;  $A$  = area exposed to the sediments; and  $r_w$  ( $\text{gO}_2 \text{ m}^{-3} \text{ d}^{-1}$ ) = rate of DO consumption in the water column due to BOD.

BOD degradation is usually represented with a first-order kinetic reaction such that (Jørgensen and Bendoricchi 2001)

$$-r_w = \frac{dBOD}{dt} = -\alpha BOD \quad (5)$$

where  $\alpha$  = first-order rate coefficient of BOD degradation. The coefficient  $\alpha$  takes values in the range of  $\alpha = 0.05\text{--}0.15 \text{ d}^{-1}$  for rivers and drinking water (Jørgensen and Bendoricchi 2001). With a constant value of  $\alpha$ , the solution of Eq. (5) provides that  $r_w(t) = \alpha BOD_o \exp(-\alpha t)$ , where  $BOD_o$  is the initial condition of the problem. However, in a timescale of one experiment (1 day),  $r_w$  varies only 5–15%, so it can be assumed constant. This assumption simplifies the integration of Eq. (4) and reduces from two ( $\alpha$  and  $BOD_o$ ) to one ( $r_w$ ) the number of parameters required for characterizing BOD. With this simplification ( $r_w = \text{constant}$ ), the analytic solution of Eq. (4) is written as

$$\begin{aligned} -k_t \frac{t}{h} = & \left( 1 - \frac{2k_t r_w}{S} \right) \ln \left( \sqrt{1 + \frac{4k_t^2}{S} C} + \frac{2k_t r_w}{S} - 1 \right) + \sqrt{1 + \frac{4k_t^2}{S} C} \\ & - \left( 1 - \frac{2k_t r_w}{S} \right) \ln \left( \sqrt{1 + \frac{4k_t^2}{S} C_o} + \frac{2k_t r_w}{S} - 1 \right) \\ & - \sqrt{1 + \frac{4k_t^2}{S} C_o} \end{aligned} \quad (6)$$

where  $C_o$  = initial concentration; and  $h = V/A$ .

The time series of  $C$ , which is described by Eq. (6), is shown in Fig. 1(c).

Finally, when  $C$  approaches zero,  $J \approx k_t C$  and Eq. (4) becomes independent of the parameter  $S$  and is written as

$$h \frac{dC}{dt} = -k_t C - hr_w \quad (7)$$

Eq. (7) shows that for small DO concentrations, the linear rate of DO depletion inside the benthic chamber is given by  $hr_w$  whereas the curvature of this decay is controlled by  $k_t$ . The analytic solution of Eq. (7) is

$$C(t) = \left( C_o + \frac{hr_w}{k_t} \right) \exp \left( -k_t \frac{t}{h} \right) - \frac{hr_w}{k_t} \quad (8)$$

where  $C_o$  = initial condition.

Eq. (8) is used to fit the value of the parameters  $k_t$  and  $r_w$ .

### Experimental Facility

Experiments were conducted in a benthic chamber in which a volume of water was isolated from the atmosphere and from lateral DO fluxes to obtain a time series of DO exchange across the WSI and BOD (Hall et al. 1989; Herzfeld et al. 2001; Arega and Lee 2005). The DO mass balance in the benthic chambers is described by Eq. (4). Fig. 2(a) shows the experimental setup.

The benthic chamber consisted of a closed acrylic cylinder of 12 cm height and 4 cm inner diameter. Both top and base covers

were removable and were screwed to the cylinder. DO and water temperature were measured with the CellOx 325 sensor (WTW, Weilheim, Germany), which was mounted in a tube of 1.5 cm inner diameter fixed to the top cover. Because the solutes of the benthic chamber must be homogeneously mixed to use Eq. (4), the water was stirred with a standard magnetic stirrer that rotated over a perforated plate located approximately 3 cm above the WSI. The plate was perforated with 21 holes of inner diameter 5 mm arranged as shown in Fig. 2(b). Effective mixing across the perforated plate was tested by placing inked water below the plate, and well-mixed conditions were observed a few seconds after the magnetic stirrer was switched on. Finally, the sediment sample was placed in a cylindrical compartment of 3.6 cm inner diameter located on the bottom of the chamber.

The total volume of the benthic chamber was  $V = 132 \text{ ml}$  with a height of  $h = VA^{-1} = 13 \text{ cm}$ , indicating that DO concentrations were expected to change by  $5 \text{ gO}_2 \text{ m}^{-3}$  over 12 h. This result was based on a characteristic value of  $\tilde{J} = 1.3 \text{ gO}_2 \text{ m}^{-2} \text{ d}^{-1}$ , which was obtained from the results of Arega and Lee (2005), Gin and Gopalakrishnan (2010), and Inoue and Nakamura (2011).

Justification is required for the use of the steady-state solution of Eq. (2) to compute  $J$  in a problem where  $C$  changes in time. Particularly, Eq. (2) can be used if the timescale in which  $C$  varies is within the timescale in which diffusion in the sediments occurs. Then a permanent solution is rapidly reached in the sediment. The timescale of changing  $C$  inside the benthic chamber was estimated based on Eq. (4) and  $r_w = 0$ :

$$T_c = \frac{h\Delta C}{\tilde{J}} \quad (9)$$

where  $\Delta C$  = characteristic concentration fluctuation equal to the accuracy of the instrument ( $\Delta C = 0.1 \text{ gO}_2 \text{ m}^{-3}$ ).

In contrast, the diffusion timescale in the sediments was estimated as

$$T_d = \frac{(\Delta\delta)^2}{\phi D_s} \quad (10)$$

where  $\Delta\delta$  = changes in the penetration depth of oxygen into the sediments due to changes in DO concentration in the benthic chamber.

The penetration depth is written as (Bouldin 1968; Kühl and Jørgensen 1992; Rasmussen and Jørgensen 1992)

$$\delta = \frac{2\phi D_s \tilde{J}}{\tilde{S}} \approx 1.7 \text{ mm} \quad (11)$$

where  $\tilde{S} = 0.38 \text{ (gO}_2 \text{ m}^{-1} \text{ d}^{-2})$ , a characteristic value of  $S$  that was estimated with  $\tilde{J} = 1.3 \text{ (gO}_2 \text{ m}^{-2} \text{ d}^{-1}) = \sqrt{\tilde{S} \tilde{C}}$  and  $\tilde{C} = 5 \text{ (gO}_2 \text{ m}^{-3})$ .

Finally  $\Delta\delta$  is written as

$$\Delta\delta = \frac{2\phi D_s}{\tilde{S}} \left( \tilde{J} - \sqrt{\tilde{S}(\tilde{C} - \Delta C)} \right) \approx 0.02 \text{ mm} \quad (12)$$

In this way,  $T_d \approx 0.15 \text{ s}$  and  $T_c \approx 18 \text{ min}$ . As a consequence, the timescale at which  $C$  varies inside the chamber is much greater than the timescale at which diffusion from the sediments occurs, justifying the use of Eq. (2) to compute  $J$ .

### Experimental Procedure

Sediment samples were collected from the artificial lagoon of O'Higgins Park near the University campus in Santiago, Chile.

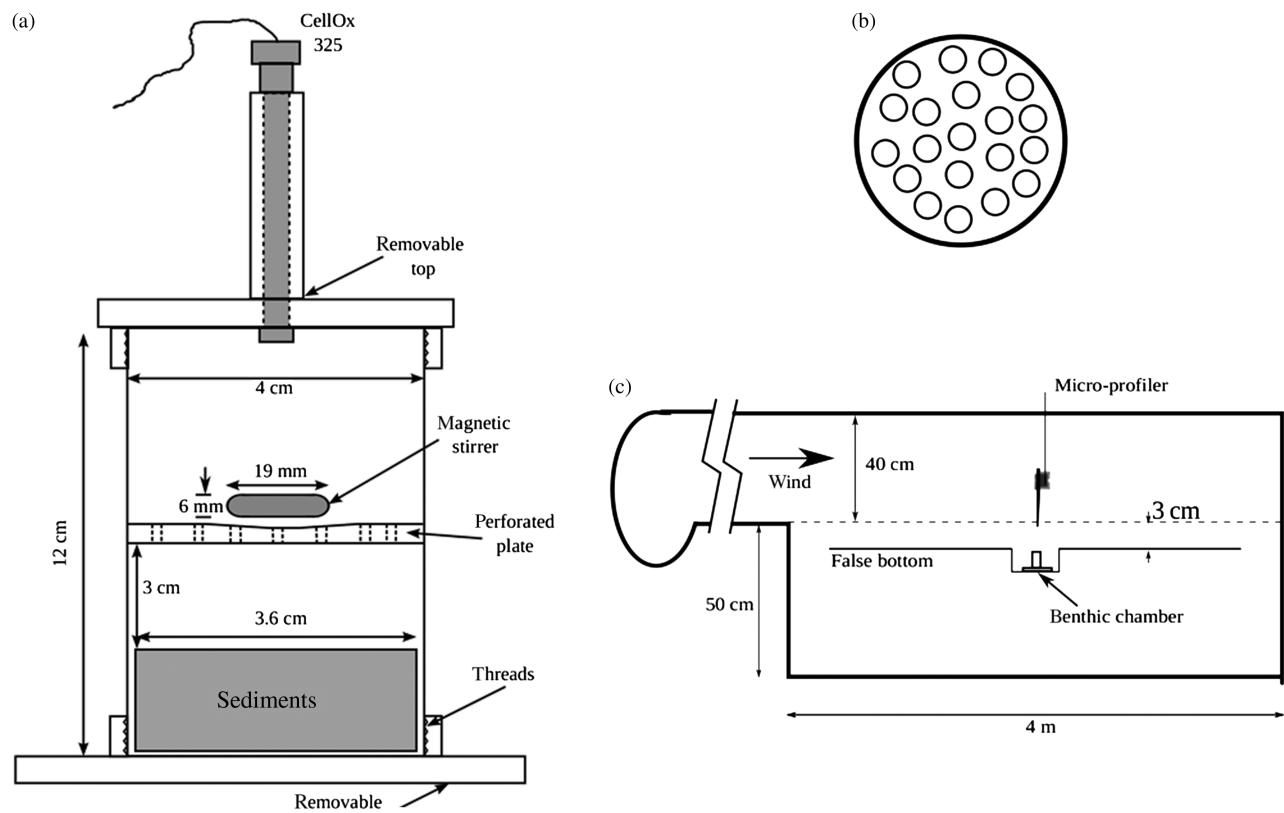


Fig. 2. Experimental setup

Before each experiment, the sediment cores were installed in the benthic chamber and allowed to equilibrate for 3 h. During the equilibration period, the magnetic stirrer was on and the top cover was unmounted.

The experiment began when the DO sensor was placed and sealed with silicone. The DO and water temperature time series from inside the benthic chamber was recorded with a CellOx325 sensor each minute. Resolution of the sensor was  $0.01 \text{ gO}_2 \text{ m}^{-3}$  and  $0.1^\circ\text{C}$ , and the accuracy was 0.05% and  $0.1^\circ\text{C}$  for DO and temperature, respectively. The 95% response time of the sensor was 16 s, and the self-consumption rate of DO was  $0.08 \mu\text{g h}^{-1}(\text{mg l}^{-1})^{-1}$ , which was neglected because it was equivalent to  $J = 0.01(\text{gO}_2 \text{ m}^{-2} \text{ d}^{-1})$ . The CellOx325 sensor was calibrated according to the procedure described in the user manual. The first three hours of measurements were not included in the analysis.

Four experiments were conducted to illustrate the application of the method. Experiments 1 and 2 were conducted with drinking water and with angular velocities of the magnetic stirrer of 3 and 5.2 Hz, respectively. Experiments 3 and 4 used distilled water and angular velocities of 3 and 5.2 Hz, respectively. The experimental conditions of each experiment are summarized in Table 1, and the measured time series of DO and temperature are shown in Fig. 3. The angular velocity of the magnetic stirrer was measured with

a camera recording at 60 fps. Unfortunately, it was not possible to use other angular velocities to obtain a detailed curve of  $k_t$  versus  $\omega$ .

### Microprofiles

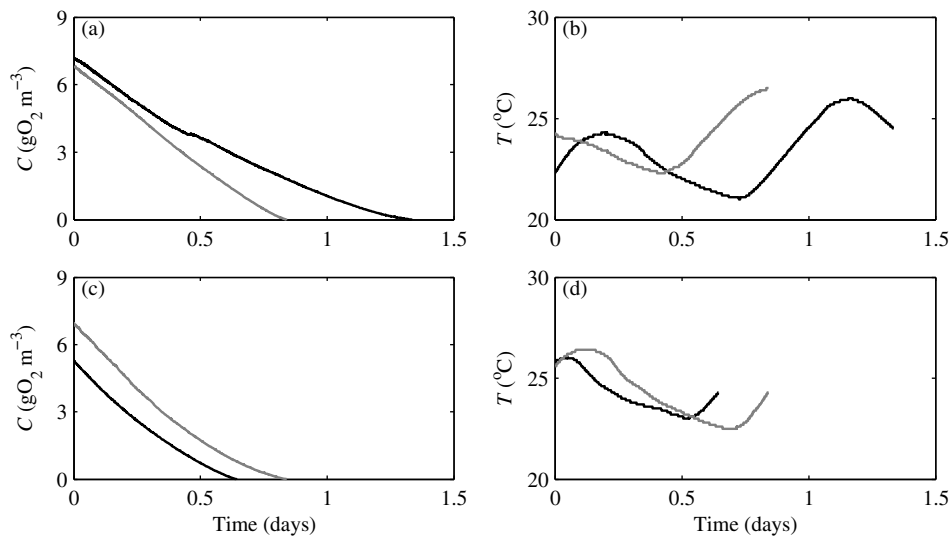
To test the accuracy of the method, DO microprofiles were measured with one OX25 Unisense microelectrode and the corresponding Unisense Microsensor Multimeter data amplifier and Unisense Sensor Trace PRO acquisition software (Unisense, Aarhus, Denmark). The calibration of the microelectrode was conducted as described in the user manual. Microprofiles were measured with the sediment sample inside the benthic chamber without the top cover and the magnetic stirrer. Turbulence in the water column was produced with the wind tunnel shown in Fig. 2(c) (Ordoñez et al. 2013). The wind tunnel had on its down-wind end a 4-m long, 0.5-m wide, and 0.5-m deep tank containing a false bottom 3 cm below the bottom of the wind tunnel. In the middle of the false bottom there was a 0.15-m long compartment where the benthic chamber was placed [Fig. 2(c)]. The microelectrode was mounted on a gauge set on a platform over the wind tunnel; the elevation of the gauge was automatically manipulated with an electronic motor. Microprofiles were measured with drinking and distilled water in

Table 1. Summary of Experimental Conditions

Run	Water	Duration (d)	$\omega$ (Hz)	DO ( $\text{gO}_2 \text{ m}^{-3}$ )	$T$ ( $^\circ\text{C}$ )	$\nu \times 10^6$ ( $\text{m}^2 \text{ s}^{-1}$ )	$Sc$	$n$
1	Drinking	1.34	3.0	0–7.19	$23.4 \pm 1.5$	0.932	433	1,924
2	Drinking	0.84	5.2	0–6.86	$23.9 \pm 1.2$	0.922	424	1,212
3	Distilled	0.64	3.0	0–5.29	$24.2 \pm 1.0$	0.915	416	928
4	Distilled	0.84	5.2	0–6.95	$24.3 \pm 1.4$	0.913	415	1,212

Note: Duration indicates length of the time series used for the analysis;  $\omega$  = angular velocity of the magnetic stirrer; DO = range of variation of DO concentration;  $T$  = average temperature  $\pm$  standard deviation;  $\nu$  = water viscosity;  $Sc$  = Schmidt number; and  $n$  = length of time series.





**Fig. 3.** Measured time series of DO and water temperature for experiments with (a and b) drinking water; (c and d) distilled water, black line = experiment with  $\omega = 3$  Hz; gray line = experiment with  $\omega = 5.2$  Hz

the benthic chamber, and two replicates were obtained for each type of water used (dr1 and dr2 for drinking water and ds1 and ds2 for distilled water)

Vertical spacing for the microprofiler was set to  $160 \mu\text{m}$  in the sediments and  $200 \mu\text{m}$  in the water column. Each microprofile was conducted based on 90-s cycles, recorded at 1 Hz, in which the first 30 s were spent moving the microelectrode between two consecutive elevations and acclimating the sensor to the new conditions; the last 60 s corresponded to measurements that were averaged for obtaining the final DO concentration.

For each microprofile, three characteristic values of  $S$  were obtained. First, to use a homogeneous  $S = 2\phi R_{O_2} D_s$  in the sediments means that DO concentration follows a quadratic equation, with the depth,  $z$ , being the coefficient associated with  $z^2$  equal to  $S/(2\phi D_s)^2$ . Consequently, the first characteristic  $S$  (called  $S_I$ ) was obtained by fitting a quadratic equation to a microprofile of the DO concentrations in the sediments. Furthermore, the vertical DO gradient has a maximum absolute value at the WSI and linearly decreases with depth at a slope equal to  $S/(2\phi D_s)^2$ . The vertical gradient of DO at the  $i$ th elevation in the profile was obtained as the slope of the linear regression computed with the points  $i-2$ ,  $i-1$ ,  $i$ ,  $i+1$ , and  $i+2$ . The second characteristic value of  $S$  (called  $S_{II}$ ) was then computed as the slope of linear fit of these DO vertical gradients with respect to the elevation. Finally,  $J$  can also be computed as  $J = \sqrt{SC_s}$ , where  $C_s$  denotes the concentration at the WSI (Bouldin 1968). On this basis, a third characteristic value of  $S$  was computed as  $S_{III} = J^2/C_s$ , where  $J$  is the diffusive flux at the WSI and  $C_s$  is the observed DO concentration at the WSI.

### Fitting Algorithm and Confidence Interval

The fitting algorithm used to obtain the value of the coefficients  $S$ ,  $k_t$ , and  $r_w$  of Eqs. (4) and (7) was based on nonlinear parameter fitting (Seber and Wild 2003), accomplished using the standard Gauss-Newton iterative method in *MATLAB*. However, this nonlinear fitting problem can also be solved with the *Solver* function in MS-Excel or with more sophisticated functions in *MATLAB* like *fit* or *lsqcurvefit*.

The Gauss-Newton iterative method considers a data set with  $n$  pairs of dependent ( $Y_i$ ) and independent ( $X_i$ ) variables. In addition, a continuum function  $[F(\alpha_j, X)]$  was fitted to the observed

variables to obtain the parameters of the problem  $\alpha_j$ ,  $\alpha_j$  being equal to  $S$ ,  $k_t$ , or  $r_w$ . This method minimizes the least-squares error. The iterative procedure also considers that the values of the parameters  $\alpha_j$  are known for a particular iteration. These values are corrected and used in the following iteration:

$$\Delta\alpha_j = \frac{\sum_{i=1}^n \frac{\partial F_i}{\partial \alpha_j} (Y_i - F_i)}{\sum_{i=1}^n \left(\frac{\partial F_i}{\partial \alpha_j}\right)^2} \quad (13)$$

where  $F_i = F(\alpha_j, X_i)$ .

The gradients of  $F$  are numerically estimated as  $\partial F_i / \partial \alpha_j = [F(\alpha_j + \delta, X_i) - F(\alpha_j, X_i)] / \delta$ , and  $\delta = 1 \times 10^{-10}$ . The procedure ends when the following result occurs:  $\max[\text{abs}(\Delta\alpha_j) / \alpha_j] < 1 \times 10^{-4}$ . Each parameter is given an initial value of 1 prior to the iteration.

A confidence interval of 95% for each estimated parameter was used to estimate error. These confidence intervals were computed using the nonlinear least-squares estimation described in Seber and Wild (2003). The upper and lower confidence limits of  $\alpha_j$  were defined by the roots,  $\hat{\alpha}_j$ , of the following second-degree polynomial equation:

$$(\hat{\alpha}_j - \alpha_j)^2 \sum_{i=1}^n \left(\frac{\partial F_i}{\partial \alpha_j}\right)^2 = \frac{p}{n-p} f_{p,n-p}^{0.95} \sum_{i=1}^n (Y_i - F_i)^2 \quad (14)$$

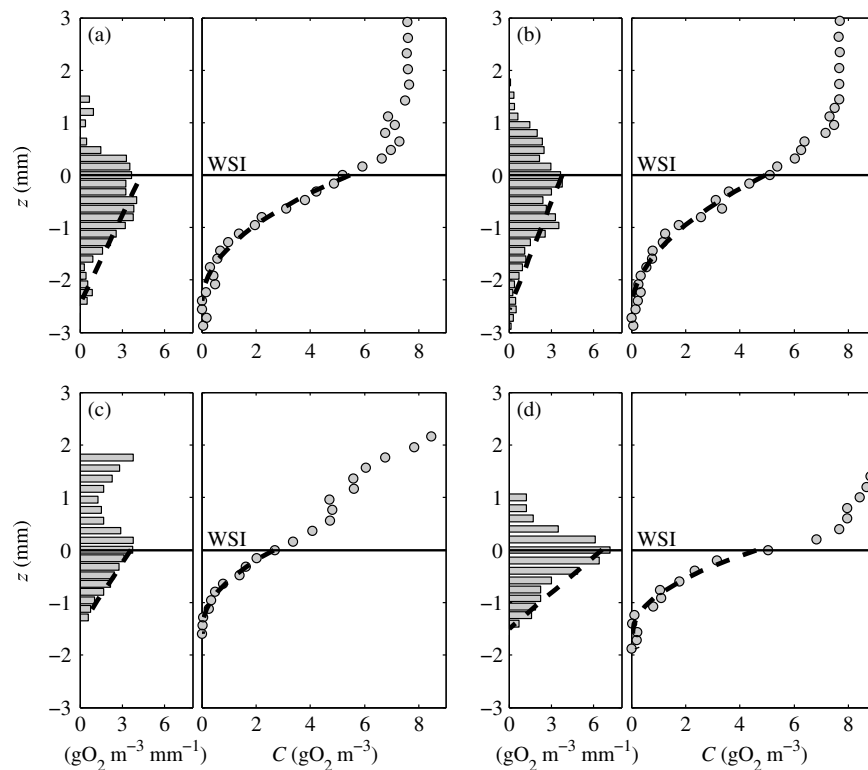
where  $f_{p,n-p}^{0.95}$  = inverse of the 95% accumulative probability distribution function,  $F$ , with two degrees of freedom,  $p$ , and  $n-p$ , where  $p$  = the number of fitting parameters.

The roots of Eq. (14) are symmetric with respect to the fitted  $\alpha_j$ . Thus, the confidence interval can be written as

$$\hat{\alpha}_j = \alpha_j \pm \sqrt{\frac{\frac{p}{n-p} f_{p,n-p}^{0.95} \sum_{i=1}^n (Y_i - F_i)^2}{\sum_{i=1}^n \left(\frac{\partial F_i}{\partial \alpha_j}\right)^2}} \quad (15)$$

### Methodology for Fitting of $S$

A two-step fitting methodology was used. First, the values of two parameters,  $r_w$  and  $k_t$ , must be known before obtaining the value of  $S$ . For each experiment, these values were obtained by fitting



**Fig. 4.** DO microprofiles (gray circles) and vertical gradient of DO (horizontal bars): (a and b) dr1 and dr2 with drinking water; (c and d) ds1 and ds2 with distilled water; dashed lines = fitted curves for characteristic values obtained for the coefficient  $S$

Eq. (8) with the data set of small DO concentrations, defined as  $C \leq 0.3 \text{ gO}_2 \text{ m}^{-3}$ . Based on the notation used in Eqs. (13)–(15),  $C$  was used as the dependent variable ( $Y$ ), the time  $t$  was used as the independent variable ( $X$ ), and there were three parameters to fit:  $\alpha_j = k_t, r_w,$  and  $C_0$  [ $p = 3$ ; see Eq. (14)], where  $C_0$  was an auxiliary parameter not relevant in the analysis.

With these fitted values of  $k_t$  and  $r_w$ , two alternatives for analyzing the DO time series were tested. The first alternative required a data set of  $h\partial C/\partial t$  versus  $C$  for a fixed flow velocity inside the benthic chamber. Based on the notation used in Eqs. (13)–(15),  $h\partial C/\partial t$  was used as the dependent variable ( $Y$ ),  $C$  was used as the independent variable ( $X$ ), and one parameter was fit [ $\alpha_j = S$ ;  $p = 2$ ; see Eq. (14)]. The rate of DO depletion in the benthic chamber ( $\partial C/\partial t$ ) was computed as the slope of the linear fit of 30 min of measurements, and  $C$  was computed as the average value of those measurements. The second alternative to obtain the value of  $S$  used the DO time series inside the benthic chamber. These data were fit with Eq. (5) to obtain  $\alpha_j = S$  and  $C_0$  [ $p = 2$ ; see Eq. (14)]. Again,  $C_0$  was an auxiliary parameter not relevant in the analysis. Because it was not possible to obtain an algebraic expression for  $C(t)$ , it was more efficient to fit  $t$  as a function of  $C$ . In this case, the independent variable ( $X$ ) was  $C$  and the dependent variable ( $Y$ ) was  $t$ .

## Results

### DO Microprofiles

Fig. 4 shows the four measured DO micro-profiles (gray circles) and the corresponding vertical gradient of DO (horizontal bars) having positive values because the DO flux is against the  $z$ -axis. The dashed lines show the fitted curve for measuring  $S$  based on the quadratic fitting of DO concentration in the sediments ( $S_I$ )

and the linear fit of the DO diffusive fluxes ( $S_{II}$ ). Table 2 summarizes the results of Fig. 4, where it is observed that  $S_I$ ,  $S_{II}$ , and  $S_{III}$  have similar values with a standard deviation of less than 20% with respect to the average. Thus, it is argued that the microprofile process was correct and that the average value of  $S$  characterized the biochemical processes in the sediment sample. One important observation was that the value of  $S$  computed for distilled water was approximately twice as large as the value obtained for drinking water (0.260 and  $0.116 \text{ gO}_2 \text{ m}^{-1} \text{ d}^{-2}$ , respectively). This influence of the water used in the benthic chamber was also noticed in the benthic chamber measurements; however, studying this relationship was not an objective of this study.

### Fitting of $S$

Table 3 shows, for each experiment, the fitted values of  $k_t$  and  $r_w$ . Fig. 5 compares the observed DO concentrations and the fitted Eq. (7). The average  $k_t$  for  $\omega = 3$  and  $5.2 \text{ Hz}$  were  $0.71$  and  $1.01 \text{ md}^{-1}$ , respectively. Unfortunately, operational restrictions with the magnetic stirrer prevented measuring other values of  $\omega$ . The determination coefficient in all experiments was close to 1, and the confidence interval of  $r_w$  and  $k_t$  was also small.

**Table 2.** Summary of Microprofile Results

Run	Water	$S (\text{gO}_2 \text{ m}^{-1} \text{ d}^{-2})$			Average $\pm$ standard deviation
		$S_I$	$S_{II}$	$S_{III}$	
dr1	Drinking	0.144	0.134	0.098	$0.116 \pm 0.019$
dr2		0.109	0.112	0.100	
ds1	Distilled	0.178	0.188	0.193	$0.260 \pm 0.088$
ds2		0.280	0.335	0.388	

**Table 3.** Summary of Results from Fitting of  $r_w$ ,  $k_t$ , and  $S$ 

Run	$\omega$ (Hz)	$k_t$ (md <sup>-1</sup> )	$r_w$ (gO <sub>2</sub> m <sup>-3</sup> d <sup>-1</sup> )	$S_1$ (gO <sub>2</sub> m <sup>-1</sup> d <sup>-2</sup> )	$S_2$ (gO <sub>2</sub> m <sup>-1</sup> d <sup>-2</sup> )	$S$ (gO <sub>2</sub> m <sup>-1</sup> d <sup>-2</sup> )
1	3.0	0.756 ± 0.052 $r^2$ :0.99, $n$ :199	1.376 ± 0.053	0.147 ± 0.018 $r^2$ :0.80, $n$ :62	0.159 ± 0.002 $r^2$ :0.99, $n$ :1,864	0.156 ± 0.023
2	5.2	1.157 ± 0.148 $r^2$ :0.99, $n$ :0.91	3.538 ± 0.156	0.133 ± 0.022 $r^2$ :0.20, $n$ :40	0.187 ± 0.003 $r^2$ :0.99, $n$ :1,212	
3	3.0	0.656 ± 0.148 $r^2$ :0.99, $n$ :0.95	3.775 ± 0.164	0.321 ± 0.017 $r^2$ :0.99, $n$ :30	0.312 ± 0.001 $r^2$ :1.00, $n$ :928	0.377 ± 0.077
4	5.2	0.861 ± 0.104 $r^2$ :0.99, $n$ :136	2.282 ± 0.107	0.398 ± 0.058 $r^2$ :0.85, $n$ :40	0.476 ± 0.002 $r^2$ :0.99, $n$ :1,212	

Note:  $\omega$  = angular velocity of magnetic stirrer;  $n$  = number of points in the data set;  $r^2$  = coefficient of determination.  $S_1$  was obtained with alternative 1;  $S_2$ , with alternative 2.

Using the fitted parameters  $k_t$  and  $r_w$ , the coefficient  $S$  was computed following alternatives 1 and 2— $S_1$  and  $S_2$  in Table 3, respectively. The average fitted  $S$  for distilled water was 0.377(gO<sub>2</sub> m<sup>-1</sup> d<sup>-2</sup>), which is 2.4 times larger than the fitted value for drinking water,  $S = 0.156$ (gO<sub>2</sub> m<sup>-1</sup> d<sup>-2</sup>). Fig. 6 shows that this result is congruent with microprofile observation; however, the ration between observed  $S$  values in the benthic chamber and those observed in the micro-profiles was 1.41 (1.34 for drinking water and 1.46 for distilled water). This difference can be attributed to the fact that microprofiles represent localized processes whereas a benthic chamber represents the surface integrated value of  $S$ . Further arguments to support this hypothesis are given in the discussion.

The results shown in Fig. 7 indicate that the fitting technique and the theoretical background represent the measurements sufficiently to explain the long-term evolution of DO inside the benthic chamber. The figure compares measurements and fitted curves for obtaining  $S$  coefficients following alternative 1 [Figs. 7(a, c, e, g)] and alternative 2 [Figs. 7(b, d, f, h)]. The fitted curves agreed well with the measurements over the entire range of observations. This agreement was especially prevalent in experiments 1, 3, and 4, where the observations followed the same curvature predicted by

Eqs. (4) and (6). The determination coefficients  $r^2$  in alternative 2, were very close to 1 in all experiments (Table 4 and the numbers in bracket in Fig. 6); however, the values of  $r^2$  in alternative 1 were smaller because alternative 1 required localized observations of only 30 min whereas alternative 2 integrated these fluxes over a long period of time. As a consequence, alternative 2 smoothed the solution so its obtained determination coefficients were much larger than the corresponding value obtained by alternative 1.

The two-step fitting methodology was required because the dimensionless number  $k_t C / \sqrt{SC}$  was larger than 2 for most of the measured  $C$ , which means that  $J$  was more dependent on  $S$  than  $k_t$  [Fig. 1(a)]. Thus, if  $k_t$ ,  $r_w$ , and  $S$  were fitted at once with the entire data set, the fitted coefficient  $k_t$  would be unrealistically large (on the order of 1,000 md<sup>-1</sup>) with an even larger confidence interval.

### Sensitivity Analysis

A sensitivity analysis was required to quantify the influence of coefficients  $k_t$  and  $r_w$  on coefficient  $S$  in order to recompute  $S$  using the fitted  $k_t$  and  $r_w$  coefficients  $\pm 20\%$ .

Fig. 8 summarizes the results of the sensitivity analysis. First, increasing or decreasing  $r_w$  or  $k_t$  reduces or increases the fitted value of  $S$ . Thus, it is observed that increasing the transfer velocity by 20% produces, on average, a reduction in  $S$  smaller than 10%. On the other hand, reducing the value of  $k_t$  by 20% causes  $S$  to increase by approximately 13%. However,  $\Delta S$  in the sensitivity analysis for  $r_w$  has the same order of magnitude as the corresponding  $\Delta r_w$ , which suggests that the uncertainty in estimating  $r_w$  is directly transmitted to estimating  $S$ .

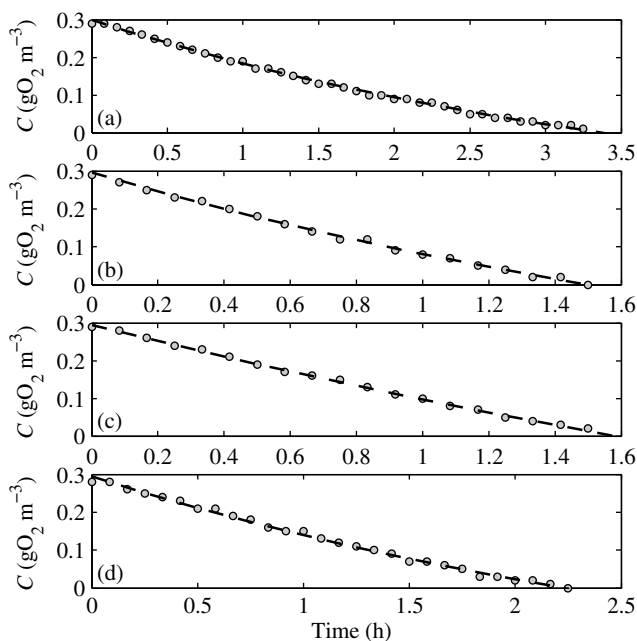
Moreover,  $k_t$  and  $r_w$  were estimated with Eq. (8), which required  $J \approx k_t C$ . This simplification is valid for small values of  $k_t C / \sqrt{SC}$  [Fig. 1(a)] and underestimates  $k_t$ . Using the average  $S$  and  $C \leq 0.3$ (gO<sub>2</sub> m<sup>-3</sup>), the average  $k_t C / \sqrt{SC}$  was computed and the average percentage of error associated with the assumption  $J = k_t C$  was estimated as

$$\Delta J = 100 \text{avg} \left( \frac{(k_t C - J)}{J} \right) \quad (16)$$

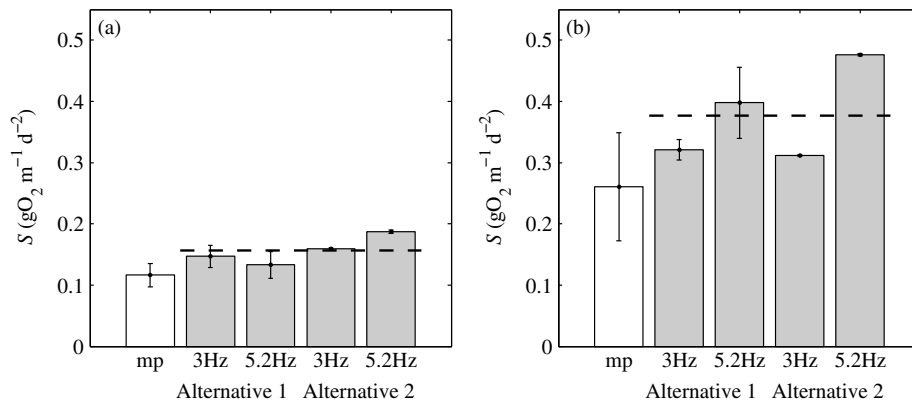
In Eq. (16)  $J$  was computed with Eq. (2), so the error in  $k_t$  due to the assumption  $J \approx k_t C$  (called  $\Delta k_t^*$ ) was estimated from

$$\Delta J = \frac{\partial J}{\partial k_t} \Delta k_t^* \quad (17)$$

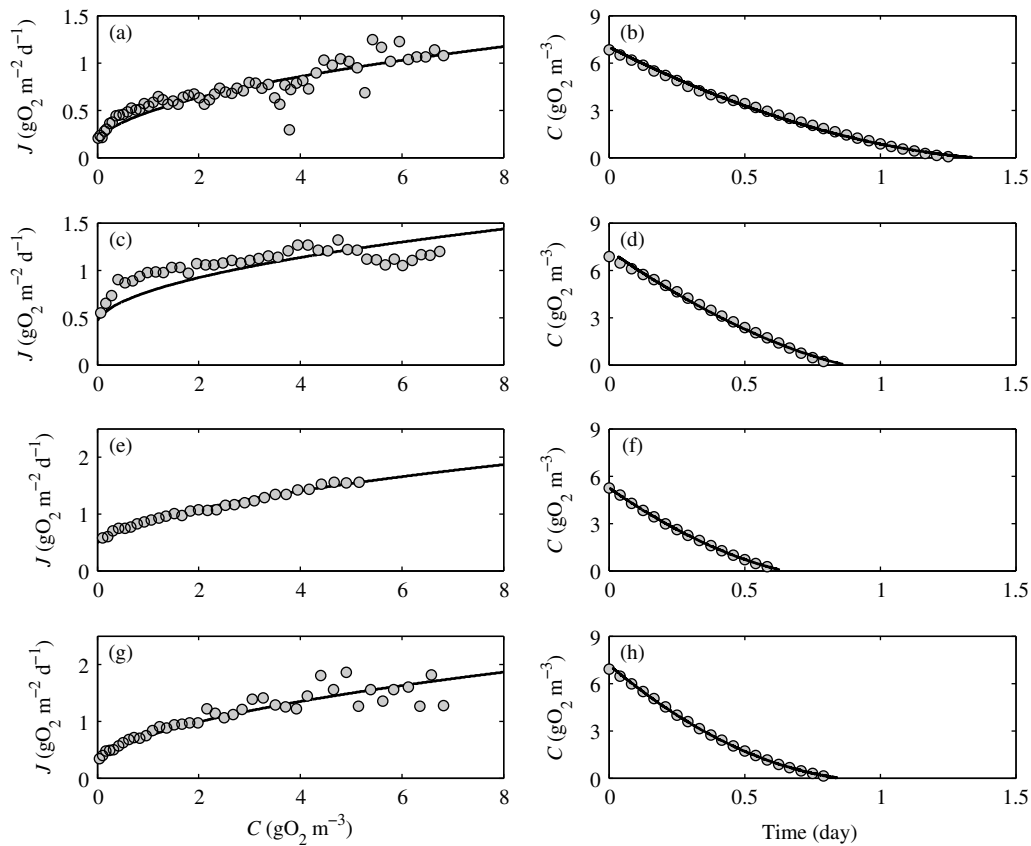
Table 4 summarizes the average  $k_t C / \sqrt{SC}$ ,  $\Delta J$ , and  $\Delta k_t^*$ . As shown, the approximation  $J \approx k_t C$  has a 15% error for experiments in distilled water and a 32% error for those in drinking water. This difference is explained by the value  $S$  in distilled water, which was larger than that in drinking water. The errors in the estimation of



**Fig. 5.** Time series of DO concentration for  $C < 0.1$  gO<sub>2</sub> m<sup>-3</sup> (dashed lines = fitted curve for obtaining coefficients  $k_t$  and  $r_w$ ): (a) experiment 1; (b) experiment 2; (c) experiment 3; (d) experiment 4



**Fig. 6.** Results from fitting coefficient  $S$ : (a) experiments 1 and 2; (b) experiments 3 and 4; white bars = microprofile measurements; gray bars = experiment with angular frequencies; processing alternatives are shown on the horizontal axis; dashed line = average of coefficient  $S$



**Fig. 7.** Results from fitting coefficient  $S$ : comparison of measured (circles) and fitted (line) values as a function of DO concentration in the benthic chamber for each experiment listed in Table 1; (a, c, e, and g) fitting of coefficient  $S$  following alternative 1; (b, d, f, and h) fitting of coefficient  $S$  following alternative 2; (a and b) experiment 1; (c and d) experiment 2; (e and f) experiment 3; (g and h) experiment 4

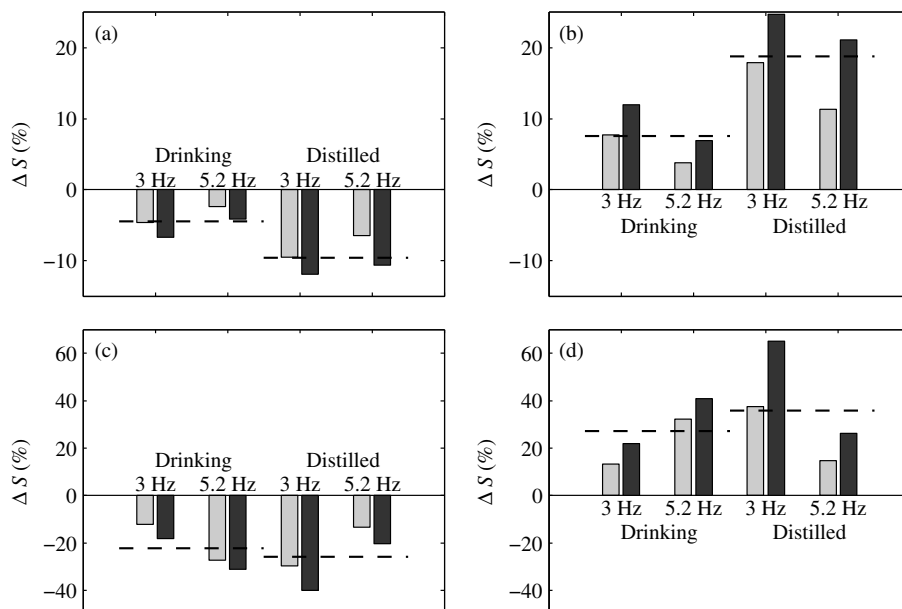
**Table 4.** Estimation of the Error in the Estimation of  $k_t$  with Eq. (8)

Run	$\text{avg} \left( \frac{k_t C}{\sqrt{SC}} \right)$	$\Delta J$ (%)	$\Delta k_t^*$ (%)
1	0.67	24.5	28
2	1.10	40.0	111
3	0.48	16.1	12
4	0.47	15.8	11

Note: The coefficient  $S$  is the average value of the table.  $\Delta J$  was defined in Eq. (16);  $\Delta k_t^*$ , in Eq. (17).

$J$  produced errors in the estimation of  $k_t$  estimated to be 11% in distilled water and 28% in experiment 1. The error in the estimation of  $k_t$  in experiment 2 was very large, and in such cases repeating the measurements is recommended. Finally, given that Eq. (9) underestimates the value of  $k_t$ , the sensitivity analysis in Table 4 shows that increasing  $k_t$  by 20% produces a 7% reduction in the fitted parameter  $S$ . The conclusion is that the error in the estimation of  $k_t$  based on Eq. (8) does not have large impact on the estimation of  $S$ .





**Fig. 8.** Results of the sensitivity analysis,  $\Delta S = 100(S^* - S)/S$ , where  $S^* =$  fitted coefficient  $S$  with  $k_t^* = k_t(1 + \Delta k_t/100)$  and  $r_w^* = r_w(1 + \Delta r_w/100)$ : (a)  $\Delta k_t = 20\%$ ; (b)  $\Delta k_t = -20\%$ ; (c)  $\Delta r_w = 20\%$ ; (d)  $\Delta r_w = -20\%$ ; light and dark gray bars = alternatives 1 and 2, respectively; dashed line = average

## Discussion

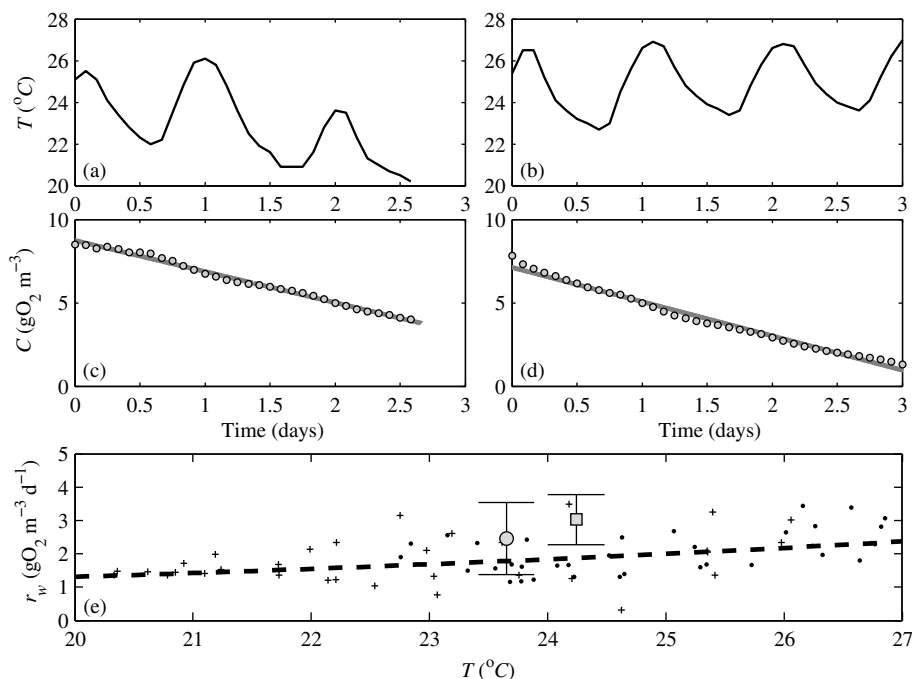
This article states that DO consumption in benthic chambers depends on biochemical processes in sediments,  $S$ , water column,  $r_w$ , and turbulent mixing,  $k_t$ . Whereas the values of  $r_w$  and  $k_t$  are controlled by the particular conditions inside the benthic chamber, the coefficient  $S$  can be used to understand DO in sediment in the field. Once  $S$  was obtained based on the proposed method,  $k_t$  was estimated for field conditions using the expressions proposed by Dade (1993), Steinberger and Hondzo (1999), and Hondzo et al. (2005). In addition, the value of  $J$  was computed with Eq. (2). Hence, the rate of DO diffusion from sediments was related to the localized biochemical features of the sediments and to the particular hydrodynamic conditions of the study site.

The proposed methodology uses an expression for computing  $J$  given in Eq. (2). However, this equation contains several simplifications. From a biochemical standpoint, Eq. (2) was derived by considering a constant and homogeneous  $S$  in the sediments whose values do not depend on DO concentration in the water column. This simplification is based on early observations of Kühl and Jørgensen (1992), Rasmussen and Jørgensen (1992), and others. Microprofile measurements shown in Fig. 4 also support this assumption. Notice that the DO concentrations in the sediments vary between 0 and DO at the WSI (approximately  $5 \text{ gO}_2 \text{ m}^{-3}$ ; see Fig. 4). Furthermore, the good fitting of Eqs. (4) and (6) with experiments 1, 2, and 4 (Fig. 7) validates the use of this equation to compute  $J$ , with DO concentrations inside the benthic chamber between 0 and  $7 \text{ (gO}_2 \text{ m}^{-3})$ . This conclusion cannot be directly extended to any sediment sample, however, particularly because biological processes are altered for small DO concentrations [ $\lesssim 2 \text{ (gO}_2 \text{ m}^{-3})$ ] (Nakamura and Stefan 1994; Glud et al. 2007). In these cases, the proposed methodology should be used to fit two different coefficients  $S$ : one for measurements with  $C < 2 \text{ (gO}_2 \text{ m}^{-3})$  and one for measurements with  $C > 2 \text{ (gO}_2 \text{ m}^{-3})$ .

The correlation of the fitted  $S$  in the benthic chamber and that in the microprofiles was good; however, the ratio between the coefficient  $S$  obtained in the benthic chamber and the coefficient  $S$

observed in the microprofiles was 1.4. This difference might have been due to bioturbation and bioirrigation (Violler et al. 2003; Berg et al. 2003), although no macrofauna were observed in the sediment sample. It might also have been because microprofiles describe localized conditions whereas the coefficient  $S$  fitted with DO observations in the benthic chamber integrates conditions in the planar area of exposed sediments. Roy et al. (2005) studied the influence of sediment microtopography in the average diffusive flux and showed that the effective area of diffusive flux can be 10–20% larger than the flat area, thus reducing  $h = VA^{-1}$  and modifying the value of all fitted parameters. For example, by increasing the surface area by 20% [ $A' = 1.2A$ , following the notation of Roy et al. (2005)], the fitted coefficients  $S$  match the microprofile observation. However, it is recommended that future applications use the geometric flat area of the sediments so that  $S$  includes microtopographic, bioturbation, and bioirrigation effects in  $J$ .

Water temperature varied in the benthic chamber according to air temperature. The standard deviation of diurnal oscillation reached  $1.5^\circ\text{C}$  in experiment 1 [Fig. 3(a)]. This oscillation influenced the value of biochemical parameters, particularly,  $S$  and  $r_w$ . To quantify this influence, two experiments without sediment were conducted with drinking water and  $\omega = 3$  and  $5.2 \text{ Hz}$ , respectively. DO inside the benthic chamber decreased according to  $r_w$  [Eq. (3), with  $J = 0$ ]. Figs. 9(a–d) show these measurements. The gray lines in Figs. 9(c and d) were obtained with the linear fit of the DO time series ( $r^2 = 0.991$  and  $0.997$  for  $\omega = 3$  and  $5.2 \text{ Hz}$ , respectively). These values indicate that a constant  $r_w$  is a reasonably good approximation. Despite this preliminary observation, the rate of DO consumption did vary with  $T$ . Fig. 9(e) shows  $r_w(T)$ , which was computed using the slope of the linear fit of two hours of measurements. The curve  $r_w(T) = r_w(20)\theta^{T-20}$  was fitted with these observations, obtaining  $\theta = 1.089 \pm 0.042$  and  $r_w(20) = 1.307 \pm 0.288 \text{ (gO}_2 \text{ m}^{-3} \text{ d}^{-1})$ . For sediment oxygen demand,  $\theta = 1.08$  is expected (Jørgensen and Bendricchio 2001). Finally, the influence of water temperature can be included in alternative 1 [Eq. (4)] by assuming  $S(T) = S_{20}\theta^{T-20}$ , where  $S_{20}$  = the coefficient to fit,  $T$  = the observed water temperature,



**Fig. 9.** Measured time series of water temperature (a and b) and DO (c and d) for experiments without sediments (gray line = fitted line for computing average  $r_w$ ): (a and c) experiment with  $\omega = 3$  Hz; (b and d) experiment with  $\omega = 5.2$  Hz; (e) comparison of observed  $r_w$  as a function of water temperature for  $\omega = 3$  Hz (pluses) and  $\omega = 5.2$  Hz (black dots) [dashed line = fitted curve  $r_w(T) = r_w(20)\theta^{T-20}$  ( $\theta = 1.089 \pm 0.042$  and  $r_w(20) = 1.307 \pm 0.288(\text{gO}_2 \text{ m}^{-3} \text{ d}^{-1})$ ); gray circles and squares = averaged  $r_w$  fitted with sediments and drinking and distilled water, respectively]

and  $\theta = 1.08$  (Jørgensen and Bendoricchio 2001). With the fitted  $S_{20}$ , the difference between the fitted coefficients in Table 3 and the temporal average of  $S(T) = S_{20}\theta^{T-20}$  was smaller than 9%. The determination coefficients did not change with respect to the values shown in Table 4. In summary, even though there were water temperature changes in time, neglecting them was a good solution for this problem, and the fitted coefficients  $r_w$  and  $S$  were representative of the temporal average water temperature in the benthic chamber.

Some aspects of the biochemical processes related to DO consumption in sediments and water require further analysis. On the one hand,  $r_w \neq 0$  was obtained in experiments 3 and 4 with distilled water, where DO consumption was not expected in the water column. The average  $r_w$  in drinking water was  $2.46(\text{gO}_2 \text{ m}^{-3} \text{ d}^{-1})$  and in distilled water was  $3.03(\text{gO}_2 \text{ m}^{-3} \text{ d}^{-1})$ —approximately 50% higher than what was observed in experiments without sediments [the gray squares and circles in Fig. 9(e)]. Thus, it is hypothesized that the value of  $r_w$  is influenced by diffusive processes from the sediments to the water, but detailed studies are required to validate this. The observed  $S$  in distilled water was twice as large as that in drinking water, which indicates that  $S$  depends on the water quality in the benthic chamber. Further studies are required to define this interaction.

In conclusion, DO time series in a benthic chamber should not be used directly to understand DO consumption in the field. The methodology proposed here enables the analysis of benthic chamber measurements without the influence of flow conditions inside the apparatus.

## Acknowledgments

This article was financed by the project Iniciación Fondecyt no. 11100306 and project Fondecyt Regular no. 1140821. In addition, the author wishes to thank the reviewers of this article for their

constructive comments, Rodrigo Pérez and María del Mar Bustos for conducting the experiments, and Carolina Meruane for providing useful comments on an early version of the manuscript.

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