

3D Spatial Exploration by *E. coli* Echoes Motor Temporal Variability

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Unraveling bacterial strategies for spatial exploration is crucial for understanding the complexity in the organization of life. Bacterial motility determines the spatiotemporal structure of microbial and controls infection spreading and the microbiota organization in guts or in soils. Most theoretical approaches for modeling bacterial transport rely on their run-and-tumble motion. For *Escherichia coli*, the run-time distribution is reported to follow a Poisson process with a single characteristic time related to the rotational switching of the flagellar motors. However, direct measurements on flagellar motors show heavy-tailed distributions of rotation times stemming from the intrinsic noise in the chemotactic mechanism. Currently, there is no direct experimental evidence that the stochasticity in the chemotactic machinery affects the macroscopic motility of bacteria. In stark contrast with the accepted vision of run and tumble, here we report a large behavioral variability of wild-type *E. coli*, revealed in their three-dimensional trajectories. At short observation times, a large distribution of run times is measured on a population and attributed to the slow fluctuations of a signaling protein triggering the flagellar motor reversal. Over long times, individual bacteria undergo significant changes in motility. We demonstrate that such a large distribution of run times introduces measurement biases in most practical situations. Our results reconcile the notorious conundrum between run-time observations and motor-switching statistics. We finally propose that statistical modeling of transport properties, currently undertaken in the emerging framework of active matter studies, should be reconsidered under the scope of this large variability of motility features.

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I. INTRODUCTION

The *run-and-tumble* (R&T) strategy developed by bacteria for exploring their environment is a cornerstone of quantitative modeling of bacterial transport. In this paradigm, bacteria swim straight during a *run time*, undergo a reorientation process during a *tumbling time*, and pursue thereafter the next run in a different direction. The now standard vision of the R&T strategy was established in the 1970s for swimming *Escherichia coli* by Berg and Brown [1,2], based on 3D trajectories obtained via a Lagrangian

tracking technique. They proposed that an adapted bacterium would perform, over long times, an isotropic random walk composed of the run-and-tumble phases, both distributed in time as a Poisson process [1–5]. For quantitative analysis, the run-time and tumble-time distributions are often taken as Poisson processes with typical values $\bar{\tau}_{\text{run}} \sim 1$ s and $\bar{\tau}_{\text{tumble}} \sim 1/10$ s [2,6]. These values change in the presence of chemical gradients, leading to a biased random walk known as chemotaxis.

Alongside the relevance of this result in the context of biology, medicine, or ecology, fluids laden with motile bacteria have become an epitome for active matter, where the organization of active particles recently led scientists to revisit many concepts of out-of-equilibrium statistical physics [7–10]. Suspensions of motile bacteria are systems of choice for these studies [11], and many original phenomena such as anti-Fick's law migration [12], collective motion [13], viscosity reduction [14–16], enhanced

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diffusion [7], or motion rectification [17–20] have been discovered. Most recent theoretical studies on active matter, aimed at understanding the emergence of collective motion or other macroscopic transport processes in bacterial fluids, assume uncorrelated orientational noise, which is the direct consequence of the Poisson character of the R&T process [9].

The simple approach of introducing a Poisson distribution for the run times, although useful for simple qualitative interpretations, is not fully consistent with a growing number of measurements performed on the individual rotary motors [21–25] driving the helix-shaped flagella. For *E. coli*, the forward (run) motion is associated with the counterclockwise (CCW) rotation of the motors, and the tumbles take place when the motors rotate clockwise (CW). The CCW to CW transition is regulated by an internal biochemical process associated with the phosphorylation of the CheY protein.

In a seminal work, Korobkova *et al.* [21] brought evidence for a heavy tail distribution for the duration of CCW rotations. Importantly, this highlights possible coupling between the stochastic fluctuations in the chemotactic biochemical network and the emergent bacterial motility. Its consequences could affect the macroscopic organization of bacterial populations, chemotactic response to chemical heterogeneity, and genetic and epigenetic feedback of bacterial populations to environmental constraints.

Its potential importance in the context of active matter studies remains overlooked. For multiflagellated bacteria, the correspondence between switching statistics, motor synchronization, flagellar bundling and unbundling dynamics, and, finally, large-scale exploration properties remains unclear. Recently, indirect experimental evidence suggested that the macroscopic motility of free-swimming bacteria is sensitive to the stochasticity borne by the chemotactic biological circuit [26]. Here, we give direct evidence of this sensitivity.

Conceptually, our analysis starts from the extreme sensitivity of the rotational CCW \rightarrow CW switching to the abundance of the phosphorylated protein CheY-P in the cell. This picture induces a timescale separation, since, at short times, the alternation of CCW and CW rotations keeps a memory of a quasifixed level of CheY-P. This memory is erased at longer times, and we thus expect very different run times and motility features at the macroscopic level.

For the first time, we link the individual motor rotation statistics to the global motility features that we observe in a large number of 3D trajectories of wild-type *E. coli* bacteria. At short observation times, the time persistence of the swimming orientations displays an exponential decay as classically admitted, but with a large distribution of characteristic times within a population of monoclonal bacteria. However, when tracking the cells individually over several tenths of minutes, we identify for each

cell a large behavioral variability. The motility data are quantitatively analyzed through a simple model initially proposed by Tu and Grinstein [27] involving the fluctuations of CheY-P triggering the tumbling events. The model is here adapted to render the spatial exploration process. It now explains the occurrence of a large behavioral variability of swimming direction and also why, at short observation times, a large distribution of these is expected over a population. The central outcome of this model is that the persistence time durations naturally follow a log-normal distribution, instead of a standard Poisson distribution. Importantly, we identify a source of measurement bias introduced in most practical situations that is a consequence of such a large distribution of run times. Finally, we discuss the consequences of measuring averaged quantities over a population displaying a large distribution of motility features. This source of measurement bias is relevant in the general framework of experiments on statistical physics of active matter.

II. VARIABILITY OF BACTERIAL MOTILITY IN A POPULATION

To characterize the bacterial motility, we build an automated tracking device suited to follow fluorescent objects and record their 3D trajectories. A swimming bacterium is kept automatically in the center of the visualization field and at the focus of an inverted microscope by a visualization feedback loop acting horizontally on a mechanical stage and vertically on a piezo stage. The method is fully detailed in Ref. [28] by Darnige *et al.* (see also Sec. VI) and was recently used to investigate the swimming of bacteria in a Poiseuille flow [29].

We first monitor more than 100 swimming *E. coli* from different strains (see Sec. VI) in homogeneous diluted suspensions (concentration $\sim 10^5$ bact/mL) confined between two horizontal glass slides, 250 μm apart. Figure 1(a) shows two typical trajectories from the same batch of monoclonal wild-type *E. coli*. We center our analysis on pieces of tracks exploring the bulk [Fig. 1(b)], i.e., in a measurement region located 10 μm above the surface and of maximum height $H = 130 \mu\text{m}$. For this series of experiments, the duration of a track is at minimum 8 s. We name these *experiments I*.

The bacterial velocities $\vec{V}(t)$ at each point of the trajectories are obtained by fitting the sequence of coordinates, along X , Y , and Z independently, over segments spanning 0.1 s, using a second-order polynomial. The first derivative of the polynomial evaluated at the center of the segment provides the velocity component. Figure 2 shows an example of a 3D trajectory and its velocity. Typically, the velocity curves for each track are irregular [Fig. 2(b)]. For a single track, the velocity distribution [Fig. 2(c)] shows a peak corresponding to the run phase and a low-velocity tail that might correspond to tumbling events. For the wild-type strain RP437 in a motility buffer, the average of the peak

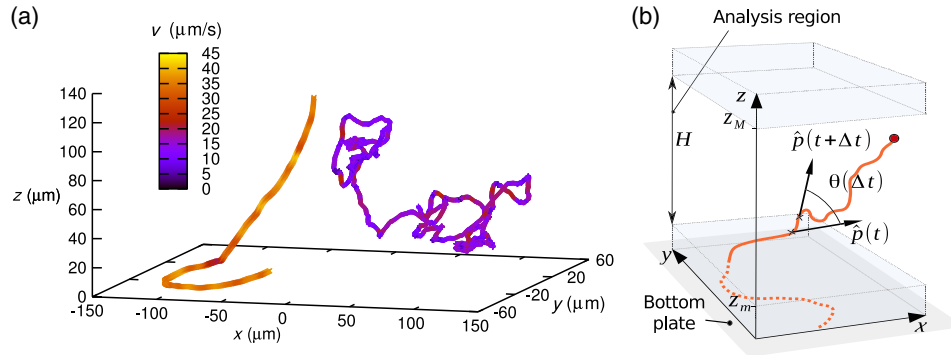


FIG. 1. Lagrangian 3D tracking of bacteria and analysis conditions. (a) RP437 wild-type *E. coli* displaying very different typical trajectories: persistent trajectory (bact 1: $\tau_p = 12$ s) and nonpersistent trajectory (bact 2: $\tau_p = 0.7$ s). (b) Sketch of the part of the track used for analysis and angles used for computing $C(\Delta t) = \langle \hat{p}(t) \cdot \hat{p}(t + \Delta t) \rangle = \langle \cos \theta(\Delta t) \rangle$, using a sliding window for an average on time t .

values for $V = |\vec{V}(t)|$ over the different tracks is $\langle V \rangle = 27 \pm 6 \mu\text{m/s}$.

Standard analysis to extract run-time distributions relies on the identification of tumbling events, usually done by detecting velocity drops and/or abrupt changes in the swimming direction [2,6,30]. However, as shown in Figs. 2(a) and 2(b), abrupt direction changes can take place without a representative velocity decrease, and velocity drops are sometimes not associated with reorientation. This observation is consistent with results from Refs. [30,31]. Moreover, by directly monitoring the flagellar dynamics, Turner *et al.* [31] identify partial flagellar debundling inducing weak velocity drops and directional changes. We find that, without a direct observation of the flagella, run-and-tumble detection requires the choice of arbitrary criteria. We demonstrate this arbitrariness in the Appendix A.

Here, in order to characterize the motility features, we do not seek to explicitly identify the tumbling events. Instead, we use the orientation correlation function $C(\Delta t)$ as a direct measurement of the swimming direction persistence. The director vectors pointing along the track are determined as $\vec{p} = \vec{V}(t)/V(t)$ for each track. For each trajectory, we compute $C(\Delta t) = \langle \hat{p}(t) \cdot \hat{p}(t + \Delta t) \rangle = \langle \cos[\theta(\Delta t)] \rangle$, where

θ is the angle between swimming directors separated by a time lag Δt [Fig. 1(b)]. The brackets denote an average over a time window sliding along the track. To ensure good statistics, the maximum lag time Δt is chosen as one-tenth of the total track duration. The orientation correlation reflects the R&T statistics but advantageously does not require an *ad hoc* criterion. In Fig. 3(a), 30 orientation correlation functions obtained from separate tracks of different bacteria (RP437 wild type in M9G) are displayed as a function of Δt .

From the classical picture of an exponential distribution of run times, the orientation correlation function is expected to decay exponentially with a typical decay time of τ_p , defining the persistence time of the trajectory. For a characteristic run time of $\bar{\tau}_{\text{run}} = 1$ s and a distribution of reorientation angles of mean value $\theta_m = 51^\circ$ [1], one finds $\tau_p = (\bar{\tau}_{\text{run}}/1 - \langle \cos(\theta) \rangle) = 1.5$ s [32]. Recently, a slight dependence of this angle on the swimming speed was demonstrated [33] but is neglected in our study. Taking into account rotational Brownian diffusion during the run phase also leads to an exponential decaying correlation function (see Appendix B). Its contribution represents a slight modification to τ_p due to the much longer timescales of Brownian diffusion. The predicted correlation function is

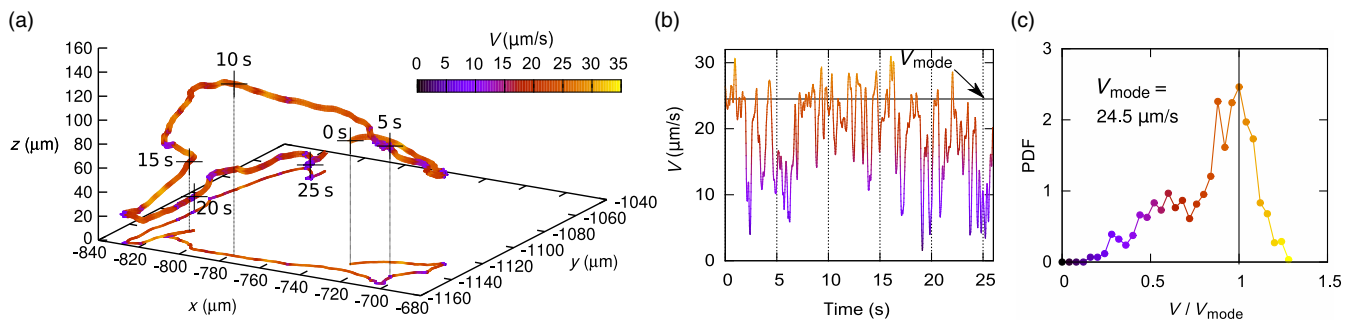


FIG. 2. Details of a typical trajectory. (a) 3D trajectory and its projection on the x - y plane, (b) velocity vs time, and (c) velocity distribution. The marks every 5 s in the 3D track are references for comparison with (b).

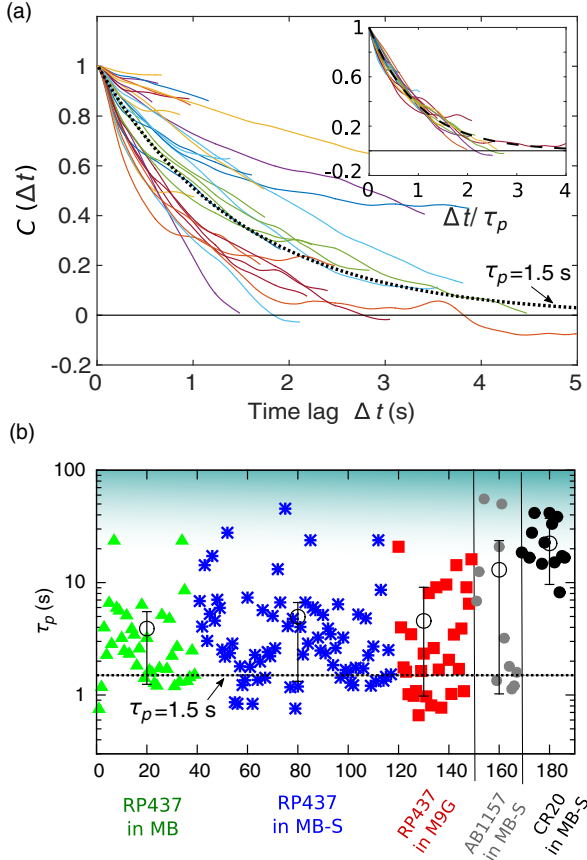


FIG. 3. Swimming orientation correlations. Experiments I. (a) Correlation function $C(\Delta t)$ obtained for 30 tracks of different RP437 bacteria in M9G, showing a large distribution of persistence times. The correlation functions are fitted with an exponential decay $\exp(-\tau/\tau_p)$ to extract the persistence times τ_p . The dotted line corresponds to $\tau_p = 1.5$ s as expected from Ref. [1]. Inset: Correlation functions as a function of Δt rescaled by τ_p . The dashed line is $\exp(-x)$. (b) Persistence times for individual bacteria of wild-type strains RP437 and AB1157 and smooth swimmer mutant CR20 in different media (MB, MB-S, and M9G). Circles and uncertainty bars correspond to the mean and 68% confidence intervals for each group. The blue background region designates the cutoff from Brownian diffusion. The dotted line corresponds to the expected $\tau_p = 1.5$ s also represented in (a). Uncertainty bars indicate the mean and confidence interval at 68%.

represented by the dotted line in Fig. 3(a). Strikingly, the experimental curves display a broad scattering, indicating a very large distribution of persistence times within this monoclonal population of bacteria.

By fitting the correlation functions with an exponential decay $\exp(-\tau/\tau_p)$, we determine the persistence times τ_p for each track. In Fig. 3(b), we display them on a logarithmic vertical axis for the strain RP437 in a motility buffer (MB) and a MB supplemented with serine (MB-S). In addition, persistence times obtained in a richer medium (M9G) and for a different wild-type strain AB1157 in

MB-S are shown. The results prove that the distribution of orientation persistence times for wild-type bacteria is very large. Within statistical errors, they are independent of the chemical environment (poor or rich), but they could depend on the strain, being larger in average for the 11 measurements performed on AB1157. For the very persistent tracks, the observed decorrelation remains weak over the accessible time lags. The obtained persistence times thus have a significant uncertainty, but we can be sure that their decorrelation time will be at least bigger than the time span of the track ($\tau_p > 8$ s). Finally, we consider the strain CR20, a smooth swimmer that tumbles only very rarely. In this case, the time distribution is gathered around the average $\tau_p = 25 \pm 10$ s, which is close to the Brownian rotational diffusion constant $\tau_p = \tau_B = 1/2D_r^B$, as expected. This value is, however, strongly dependent on the bacterial dimensions and aspect ratio [34,35]. A bacterium modeled as an ellipsoid of semiaxes $a = 4 \mu\text{m}$ and $b = c = 0.4 \mu\text{m}$ has a persistence time $\tau_p \sim 22$ s, while with $a = 6 \mu\text{m}$ it has a persistence time 3 times larger, $\tau_p \sim 66$ s [36]. Therefore, the wide distribution of persistence times for CR20 could arise from the bacterial size distribution. A possible origin of this dispersion on the measurement protocol is discussed in Sec. IV C.

III. VARIABILITY OF INDIVIDUAL BACTERIAL MOTILITY OVER TIME

The large diversity of trajectories here observed over short times in bacterial populations leads to the question of its origin. The diversity could arise from a phenotype multiplicity present in the monoclonal population [37,38], where each bacterium is characterized by a mean run time; alternatively, it could be due to temporal variability of the bacterial behavior, with mean run times varying over the course of time. To determine which scenario is taking place, we perform a second series of measurements, *experiments II*, where we follow individual bacteria over very long times (up to 20 min). In the new configuration, the top and bottom of the measurement chamber are within the observation range or the 3D tracker device. We follow individual bacteria as they alternate between the surfaces and the bulk, as sketched in Fig. 4(a). For the analysis, individual tracks are cut in pieces localized entirely in the bulk ($10 \mu\text{m}$ away from the walls). For each piece, we extract the persistence time from the correlation function. Finally, for each bacterium, we obtain a list of persistence times as a function of time. If the population displayed a large distribution of fixed run-times, one would expect for each bacterium a sequence of persistence times narrowly distributed around a characteristic value, but this value would be different for different bacteria. Figure 4(b) carries a very different message. For each of the tracks tested, the persistence times span a range of the same magnitude as

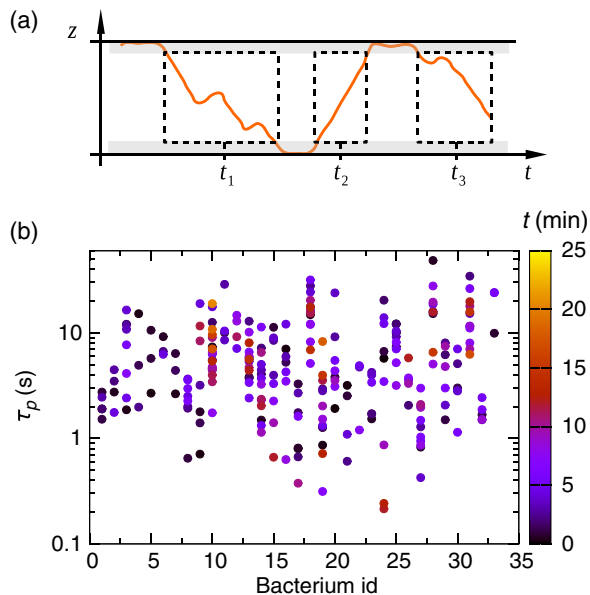


FIG. 4. Analysis for long tracks. Experiments II. (a) Sketch indicating the pieces of track from the same trajectory selected for demonstrating the behavioral variability. (b) τ_p for pieces of track from the same trajectories, for 33 different RP437 bacteria in MB-S. The color represents the starting time of the measurement. Each bacterium displays a large variation of persistence times.

for the whole population using shorter tracking times (see Fig. 3).

Previous studies based on 3D Eulerian tracking techniques [33,39], i.e., on a fixed reference frame, or even the Lagrangian tracking technique [6] were limited to short observation times and, consequently, were not able to catch such slow fluctuations of the run time. The fact that for a given bacterium the sequence of persistence times is largely distributed confirms the importance of behavioral variability in the motility process. However, due to tracking time limitations imposed by the bleaching of the fluorescent signal, we are not able to test precisely to what extent the behavioral variability contains features which could vary from one bacterium to the other, stemming from inherent phenotype variations, as identified, for example, by Dufour *et al.* [40].

IV. MOTILITY AND MOTOR ROTATION STATISTICS

The presence of a behavioral variability, as identified earlier, raises the question of its biochemical origins. Previous results point toward a definite influence of a stochastic process in the chemotactic sensory circuit. At the end of the biochemical cascade, there is a phosphorylation of a CheY protein (CheY-P) promoting a switch in the motor rotation from the CCW state (run phase) to the CW state (tumbling phase). The most accepted picture rendering the $\text{CCW} \rightleftharpoons \text{CW}$ transition is a two-state model initially proposed by Khan and Macnab [41], which considers the

switching of the rotation direction $\text{CCW} \rightarrow \text{CW}$ (equivalently, $\text{CW} \rightarrow \text{CCW}$) as an activated process regulated by the presence of CheY-P. The double-well Gibbs free energy associated with the transition $\text{CCW} \rightleftharpoons \text{CW}$ depends in a very sensible way on the CheY-P ($[Y]$) concentration values near the motor, as shown by Cluzel, Surette, and Leibler [42]. This strong sensitivity leads naturally to behavioral variations, as slow fluctuations around the mean value can change the motility features from preferentially tumbling (high CheY-P) to preferentially running (low CheY-P). It also means that at short times the CheY-P level does not change significantly and motility features remain constant. Therefore, at a given moment, the motility features should be largely distributed in a population of bacteria bearing different CheY-P concentrations. This large distribution is in essence what is observed in our experiments in Figs. 3 and 4.

A. Quantitative description of the behavioral variability model

To rationalize and quantify our experimental findings, we adapt the simple but enlightening physical model proposed by Tu and Grinstein [27]. The behavioral variability (BV) model we present here quantifies the role of fluctuations of the phosphorylated protein CheY-P in the regulation of the motor-switching statistics. The key idea is that the observed typical switching time at a given moment depends on the instantaneous CheY-P concentration $[Y](t)$. Then, considering concentration fluctuations around a mean value ($\delta Y(t) = [Y](t) - [Y_0]$), one obtains a two-state model with a time-varying barrier describing the $\text{CCW} \rightarrow \text{CW}$ switching process. Tu and Grinstein model the δY fluctuations as an Ornstein-Uhlenbeck process with a memory (relaxation) time T_Y , hence yielding a Gaussian distribution for δY values. Note that T_Y is considered to be larger than typical motor-switching times [see Fig. 5(a) for the relevant timescales].

For small fluctuations of concentration, the average switching time can be written as

$$\tau_s = \tau_0 e^{-\Delta_n \delta X}. \quad (1)$$

Here, δX corresponds to the fluctuations in concentration normalized by the δY standard deviation σ_Y ; τ_0 is a typical switching time corresponding to the mean concentration $[Y_0]$ and $\Delta_n = \alpha(\sigma_Y/Y_0)$. The parameter α is positive [42] and measures the sensitivity of the switch to variations in $[Y]$, which means that higher concentrations of CheY-P lead to shorter run times. Note that, in principle, the two switching times describing $\text{CCW} \rightarrow \text{CW}$ (run times) or $\text{CW} \rightarrow \text{CCW}$ (tumbling times) could be modeled with corresponding parameters τ_0 and Δ_n . However, as the results from Korobkova *et al.* [21] show that, in contrast with run times, the distribution of tumble times is exponential, meaning that the equivalent of Δ_n for tumbles is

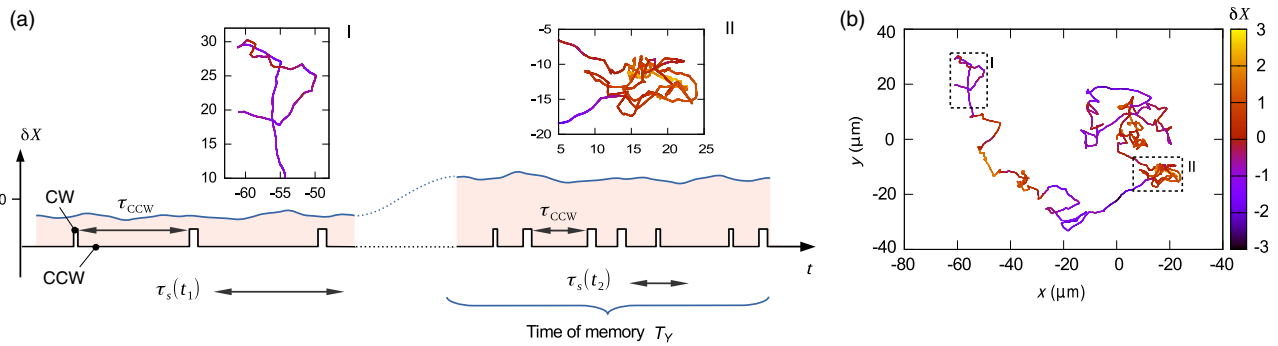


FIG. 5. Heuristic view of the behavioral variability model. (a) Timescales of the tumbling process and the CheY-P concentration governing them. The switching time τ_s represents the local average of the stochastic run times τ_{CCW} . The switching time τ_s stays relatively constant during the memory time T_Y and evolves as a function of the normalized CheY-P concentration: $\delta X = ([Y] - [Y_0]) / \sigma_Y$. (b) 2D projection of the simulated 3D trajectory where the δX fluctuations drive the tumbling process. The insets correspond to different levels of $[\delta X]$: Inset I depicts a low CheY-P level, and inset II depicts a high CheY-P level.

small. Hence, we consider the tumbling times as a Poissonian process, well described by a single timescale.

Let us first consider the CCW \rightarrow CW switching time distributions. Each observed time belongs to a Poisson distribution with a typical time τ_s set by the current CheY-P concentration $[Y](t)$ [see Eq. (1)]. As a consequence, the observed switching statistics for an individual bacterium, when observed over a time interval shorter than the memory time, should approximately appear as an effective Poisson process, which is indeed the case, as shown from the collapse of the rescaled orientation correlation functions onto a single exponential decay shown in Fig. 3(a). The model provides a second important outcome. A random choice of a bacterium in a population is like a random choice of δX , hence defining a typical switching time τ_s for this bacterium. A Gaussian distribution for δX , as assumed by the BV model, leads to a Gaussian distribution of $\ln(\tau_s)$ characterized by an average $\ln(\tau_0)$ and a standard deviation $\sigma_{\ln \tau_p} = \Delta_n$, yielding naturally a large log-normal distribution of τ_s provided the switch

sensitivity α is large. Note that the power law distribution discussed by Tu and Grinstein [27] is obtained in the limit of very large Δ_n and not in contradiction with the above statement. As τ_s and τ_p are proportional, the distribution of $\ln(\tau_p)$ should also be Gaussian.

To illustrate this idea, a very long 3D trajectory is synthesized numerically using the switching statistics from the BV model. Figure 5(b) shows a 2D projection (see Sec. VI for technical details and Sec. IV C for the parameter values). The simulated trajectory contains very persistent (inset I) and very nonpersistent (inset II) parts. The colors represent the local values of δX illustrating the direct influence of the slow variations of CheY-P concentration on the bacterial motility, hence explaining the observed behavioral variability.

B. Memory time

The evolution of persistence times τ_p along individual trajectories displays large variations. It is shown in Fig. 6(a)

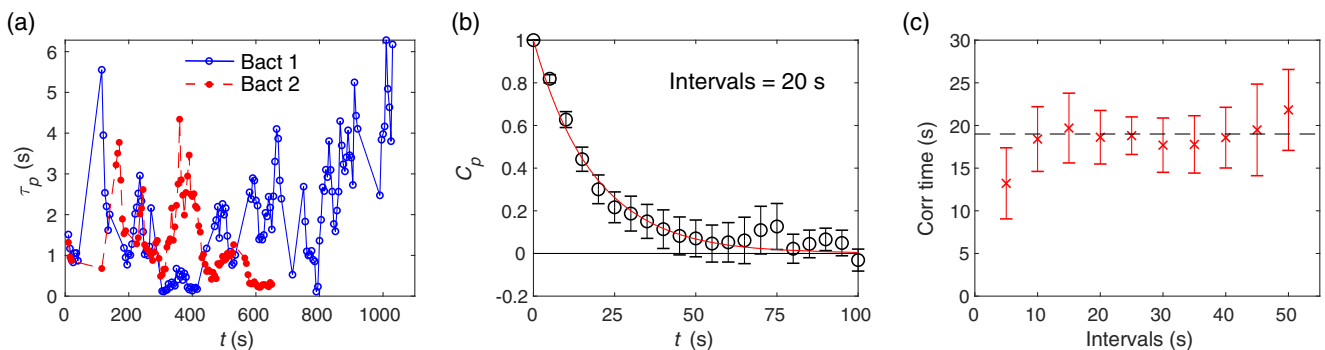


FIG. 6. Determination of the memory time from experiments II. (a) Persistence times τ_p computed over pieces of span 20 s and shifted 5 s for two different bacteria. Gaps larger than 5 s between consecutive points correspond to lapses in which the bacteria are swimming close to surfaces. (b) Persistence times self-correlation function C_p using pieces of 20 s. Points represent the average over the ensemble of bacteria. (c) Correlation time of the persistence times as a function of the lengths of the pieces. We extract the memory time to be $T_Y = 19.0 \pm 1.3$ s.

for the case of two different bacteria continuously tracked for 11 and 17 min. The values of τ_p for each track are extracted from intervals of span 20 s shifted 5 s along the trajectory. Gaps larger than 5 s between consecutive points correspond to lapses in which the bacterium is swimming close to a surface. Analyzing, for example, the bacterium of the blue longer trajectory, at time 300 s (5 min) it displays a persistence time close to 0.1 s, in contrast with a persistence time close to 5 s around time 1000 s (~ 17 min). This temporal variation of τ_p is considered in the framework of the BV model. The memory time T_Y is then a central parameter of the BV model, as it provides a natural separation between short-time measurements and long-time measurements. Therefore, for a correct statistical interpretation of the results, τ_p values must be extracted from pieces of tracks not longer than the memory time T_Y .

We estimate the memory time T_Y from the long-time tracking data in experiments II, using the following procedure. For each bacterial trajectory, we compute a sequence of τ_p using intervals of a specific duration. For each sequence of τ_p , we compute the self-correlation function of persistence times, $C_p(t) = \langle \ln \tau_p(t+t') \ln \tau_p(t') \rangle - \langle \ln \tau_p \rangle^2$, where the average is done over t' . The average of C_p over the ensemble of trajectories is fitted with an exponential, giving the correlation time [Fig. 6(b)]. With this procedure, we investigate different lengths of intervals [Fig. 6(c)], finding that the correlation times grow with the duration of the interval until saturation at the value of the memory time $T_Y \approx 19.0 \pm 1.3$ s.

C. Comparison with the model

The BV model depends on several parameters: the memory time T_Y , the mean switch time and sensitivity τ_0 and Δ_n , respectively, the rotational diffusion coefficient D_r^B , and the dimensionless rotational diffusion coefficient \tilde{D}_r^{eff} used to model the reorientation during tumble (see Sec. VI for details). We determine T_Y from the experiments, while the rest of the parameters are fitted using the following protocol. A long simulated trajectory is generated and cut in pieces of duration 20 s, similar to the analysis of the experimental tracks, and the persistence time is computed for each piece. We look for the values of the parameters that best agree with the experimental values of the first four moments of the distribution of $\ln \tau_p$. The result is $\tau_0 = 1.53$ s, $\Delta_n = 1.62$, $D_r^B = 0.025$ s $^{-1}$, and $\tilde{D}_r^{\text{eff}} = 3.86$. Note that the velocity does not appear in the fit, because we compare simulations and experiments using the persistence times, which depend only on the orientations.

Figure 7(a) compares the experimental distribution of $\ln \tau_p$ with the results from simulations using the optimal parameters. The agreement is very good, with two features that need discussion. First, in agreement with the BV model, the distributions are not exactly Gaussian but

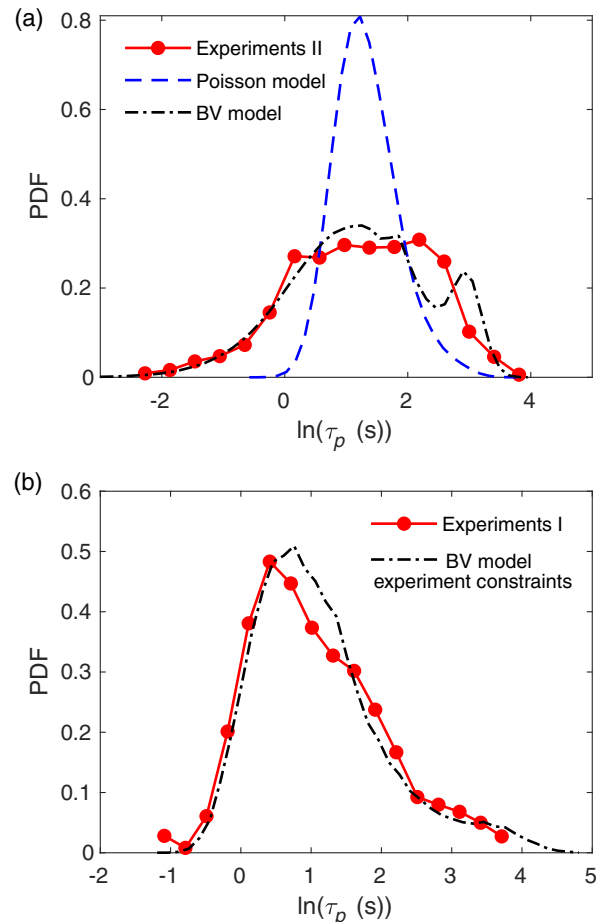


FIG. 7. Probability density function of the logarithm of persistence times ($\ln \tau_p$). (a) The values τ_p are extracted from pieces of track from experiments II that last 20 s. Simulations using two different models are shown: The Poisson model does not reproduce the experiments, while the BV model reproduces the main features. (b) The experimental distribution corresponds to the combined RP437 bacteria in all media, from Fig. 3 in experiments I. “BV model experiment constraints” are determined from the same simulations of “BV model” but analyzing pieces of trajectories that follow the experimental constraints in this case. It reproduces experiments I without additional free parameters.

present a negative excess kurtosis. With 63% probability, the switch times are in the range $[\tau_0 e^{-\Delta_n}, \tau_0 e^{\Delta_n}] = [0.30$ s, 7.7 s]. Hence, there is no complete separation of timescale with T_Y . As a consequence, in each piece, δX is not constant, and the measured and simulation distributions result from the mixture of different values of τ_s . Note that shorter pieces would imply too few tumble events and would make it unreliable to use the orientation correlation function. A perfect log-normal distribution could be observed if there was a good separation of timescales, allowing a choice of intervals such that $\tau_0 \ll T_{\text{interval}} \ll T_Y$.

The second feature is the small peak at $\ln \tau_p \approx 3$ in the simulations. This peak corresponds to pieces of the

trajectory where no single tumble took place. The change in orientation is due only to rotational diffusion during a run. Because $\tau_B = 1/2D_r^B \approx 20$ s is similar to T_Y , no complete reorientation occurs in the interval, resulting in a distribution of τ_p for nontumbling swimmers. In fact, the persistence times for the nontumbling bacteria [strain CR20 from experiments I, Fig. 3(b)] coincide with this peak. This feature should also be present in experiments, but, as discussed in Sec. II, D_r^B depends strongly on the bacterial dimensions, which vary within the population. This dispersion of rotational diffusion and other imperfections blur this peak in the experiments, contrary to the simulations, where all swimmers are identical. Note that, despite of the diversity, the fitted value of D_r^B matches closely the prediction made in Sec. II for ellipsoidal swimmers.

Since the pieces of trajectories are of a finite length, the orientation correlation function is not perfectly sampled, and, even for a constant switch time τ_s , the persistence times τ_p obtained from an exponential fit would present some dispersion. To test whether the observed dispersion is due only to the data analysis protocol, we perform simulations with a Poisson model. For this test, we look for the best parameters to reproduce the first fourth moments of the distribution of $\ln \tau_p$, setting $\Delta_n = 0$. The result is $\tau_0 = 1.18$ s, $D_r^B = 0.026$ s⁻¹, and $\tilde{D}_r^{\text{eff}} = 1.61$. Figure 7(a) presents the resulting distribution, which is far from the experimental one. We conclude that a Poisson process cannot explain the broad distribution of persistence times observed experimentally.

Finally, for consistency, we return to the persistence times obtained in Fig. 3 from experiments I. In this experimental protocol, the trajectories are selected within a certain height (10–140 μm from the surface) and longer than 8 s. The corresponding experimental distribution of $\ln(\tau_p)$ for RP437 bacteria in all media [Fig. 7(b)] displays a clear positive skewness, which differs strikingly from the experimental measures of Fig. 7(a), done using the same bacterial strain and confinement and a similar chemical environment. This difference originates from a measurement bias built into the analysis of Fig. 7(b) (and Fig. 3). The bias is a consequence of a preferential selection of long trajectories staying essentially in the x - y plane, with limited bounds in the vertical direction. The skewness is enhanced by the broad distribution of run times, since very persistent swimmers will likely quit the measurement region in a very short time, hence privileging small persistence times. The curve “BV model” represents the distribution of persistence times from simulations of the BV model that fit the experiments in Fig. 7(a) (experiments I). When this same simulation is analyzed by taking pieces following strictly the experimental constraints, on both duration and vertical spatial exploration, the resulting distribution (“BV model experiment constraints”) compares very well and noticeably without any additional fitting parameter, to the experimental curve in Fig. 7(b) (experiments II).

V. CONCLUSIONS

We have shown that the 3D spatial exploration of an adapted *E. coli* reflects a behavioral variability that we associate with intrinsic noise in the chemotaxis pathway controlling the run-and-tumble sequence. Our results for free-swimming bacteria are consistent with models describing motor-switching dynamics based on tethered cell measurements. We identified a large log-normal distribution of persistent times stemming from the slow fluctuations of an internal variable accounting for the CheY-P concentration near the motors. In the context of many recent works on statistical physics of active matter, we suggest that this large variability should be included in the description of bacterial fluids. This variability is expected to influence the computation of averaged quantities like diffusivity, viscosity, or any constitutive relations of macroscopic transport processes.

The broad distribution of run times is likely to introduce measurement biases in practical situations. Here, we reduce the bias by taking pieces of trajectories of equal length, not larger than the memory time. Mixing trajectories of different lengths can result in highly distorted distributions.

The large distribution of motility features has been related to the time bacteria spend close to surfaces. As an example, the existence of a large distribution of motor-switching statistics was found crucial to understand large-scale upstream bacterial contamination of narrow channels [26], where substantial transport occurs along surfaces [43–46].

We expect the chemotactic drift to be sensitive to the distribution of CheY-P concentrations, since a nonlocal spatiotemporal coupling will take place between chemical gradients and bacterial concentration. This sensitivity should be taken into account in future motility modeling. Finally, these findings may also impact quantitative modeling on how bacterial populations react to environmental changes, colonize space, swarm in a biofilm [47], or interact with other communities.

VI. MATERIALS AND METHODS

A. Bacterial strains and culture

We use the wild-type strains RP437 and AB1157 and a smooth swimmer mutant strain CR20 (ΔCheY) expressing yellow fluorescent protein (YFP) from a plasmid. Bacteria are grown overnight at 30 °C in M9G medium [M9 minimal medium supplemented with glucose (4 g/L), casamino acids (1 g/L), MgSO_4 (2 mM), and CaCl_2 (0.1 mM)] plus the corresponding antibiotics, up to optical density = 0.5 at 595 nm. Cells are then washed 3 times by centrifugation at 2000 g for 5 min and suspended in a motility buffer (10 mM potassium phosphate buffer $\text{pH} \sim 7.0$, 0.1 mM EDTA, 1 μM L-methionine, and 10 mM sodium L-lactate), supplemented with polyvinylpyrrolidone (PVP-360 kDa 0.002%) and, when indicated, with L-Serine (0.04 g/mL).

B. The 3D Lagrangian tracker

We develop a device for keeping individual microscopic objects—as swimming bacteria—in focus, as they move in microfluidic chambers [28]. The system is based on real-time image processing, determining the displacement of the stage to keep the chosen object at a fixed position in the observation frame. The z displacement of the stage is based on the refocusing of the fluorescent object that keeps the moving object in focus. The algorithm for z determination is designed for not being affected by photobleaching.

The instrument is mounted on an epifluorescent inverted microscope (Zeiss-Observer, Z1) with a high magnification objective ($100\times/0.9$ DIC Zeiss EC Epiplan-Neofluar), an x - y mechanically controllable stage with a z piezomover from Applied Scientific Instrumentation (ms-2000-flat-top-xyz), and a digital camera ANDOR iXon 897 EMCCD. The device works nominally at 30 frames per second on a 512×512 pix² matrix, but a faster tracking speed of 80 Hz can be achieved by reducing the spatial resolution to 128×128 pix². It provides images of the object and its track coordinates with respect to the microfluidic device.

The tracking limitations come essentially from the z exploration range, restricted by the working distance of $150\ \mu\text{m}$ of the objective. In the x - y plane, the spatial limitations are virtually nonexistent, since the stage displacement can be as long as 15 cm, which is much bigger than the typical sizes of the sample (a few millimeters). Details of the apparatus are given in Ref. [28], as well as an exhaustive explanation of a method for correcting the mechanical backlash typically affecting these systems and a discussion of the device's performance and limitations.

C. Experimental geometries and bacteria tracking

We monitor hundreds of single *E. coli* in a drop of a diluted homogeneous suspension (concentration $\sim 10^5$ bact/mL) squeezed between two horizontal glass slides. The drop has typically a diameter of 1 mm. The gap between the two glass plates is $250\ \mu\text{m}$. For experiments I, displayed in Fig. 3, only pieces of 3D trajectories remaining between the vertical bounds $z_m = 10\ \mu\text{m}$ from the bottom surface and $z_M = 140\ \mu\text{m}$, the highest possible height, and lasting more than 8 s are taken into account. For the set of very long tracks in Fig. 4, experiments II, the gap between the glass plates is also $250\ \mu\text{m}$, but the whole trajectories are captured, as they alternate between the bottom and top. For the analysis, only pieces farther than $10\ \mu\text{m}$ from the surfaces are taken into account.

The velocities are determined from second-order Savitzky-Golay filtering of the coordinates over 0.1 s, resulting in uncertainties close to 5% [36]. For each track, the velocity distribution shows a peak corresponding to the mean run velocity and a low-velocity tail corresponding to the contribution of sudden velocity drops (Fig. 2). Peak

velocities are on average $\langle V \rangle = 27 \pm 6\ \mu\text{m/s}$. To compute the correlation function $C(\Delta t)$, the average is made over time, and the lag time is offset by 0.2 s to avoid the short-time decorrelation due to wobbling [36,48]. The correlation function is then normalized by its value at 0.2 s to yield 1 at the lag time origin.

D. Track simulations using the BV model

Swimmers are described by their position \vec{r} , orientation \hat{p} , and the instantaneous value of the normalized fluctuations of the CheY-P concentration $\delta X = ([Y] - [Y_0])/\sigma_Y$. During the run phase, they obey the equations

$$\dot{\vec{r}} = V\hat{p}, \quad (2)$$

$$\dot{\hat{p}} = \sqrt{D_r^B}(I - \hat{p}\hat{p})\vec{\eta}(t), \quad (3)$$

$$\delta\dot{X} = -\delta X/T_Y + \sqrt{2/T_Y}\xi(t), \quad (4)$$

where V is the swim velocity, D_r^B is the rotational diffusion coefficient, T_Y is the memory time, $(I - \hat{p}\hat{p})$ is a projector orthogonal to \hat{p} , ξ is a white noise of zero mean and correlation $\langle \xi(t)\xi(s) \rangle = \delta(t-s)$, and $\vec{\eta}$ is a white noise vector of zero mean, where the components have correlations $\langle \eta_i(t)\eta_k(s) \rangle = \delta_{ik}\delta(t-s)$.

The BV model yields a relation between the characteristic switching time for the transition CCW \rightarrow CW (run to tumble) and the CheY-P concentration. As a simplification, we assume that, due to the small cellular dimensions, all six flagella operate at the same CheY-P concentration and that the reverse of the rotation direction of a single flagellum is enough to trigger a tumble. Hence, the probability to tumble in Δt would be $6\Delta t/\tau_s$. To simplify notation, we absorb the factor 6 into τ_0 , resulting in a tumble probability $\Delta t e^{\Delta_n \delta X} / \tau_0$.

The BV model predicts that the characteristic switching time for the transition CCW \rightarrow CW (tumble to run) is also given from an activated process. But, as the corresponding value of Δ_n is small, the tumble duration is given by a Poisson process with characteristic time τ_1 . In addition, the reorientation dynamics during a tumble needs to be modeled. *A priori*, the link between motor switch and tumble is far from being trivial, as, in principle, one needs to account for the hydrodynamically complex bundling and unbundling process of the multiflagellated *E. coli* bacteria [49,50]. Here, we rather follow a simple effective approach inspired by Saragosti, Silberzan, and Buguin [51]. We model the reorientation dynamics during tumbling as an effective rotational diffusion process with a coefficient D_r^{eff} . Defining the dimensionless combination $\tilde{D}_r^{\text{eff}} = D_r^{\text{eff}}\tau_1$, the dimensionless tumble durations are sorted from an exponential distribution with a typical time equal to one, and, during a tumble, the dynamics is

$$\dot{\vec{r}} = 0, \tag{5}$$

$$\dot{\hat{p}} = \sqrt{\tilde{D}_r^{\text{eff}}} (I - \hat{p} \hat{p}) \vec{\eta}(t), \tag{6}$$

$$\delta \dot{X} = 0. \tag{7}$$

After the tumble phase, a new run phase starts.

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APPENDIX A: RUN DURATION ANALYSIS

Figure 8 displays a series of analyses on a single trajectory, evidencing that tumble detection is criterium dependent. Here, we set a threshold velocity, cutoff V , and identify as runs all the continuous parts of the track where the bacterial velocity is above the prescribed threshold. The plot demonstrates that, by changing the cutoff value for the velocity, we can obtain average run times of duration 1–8 s.

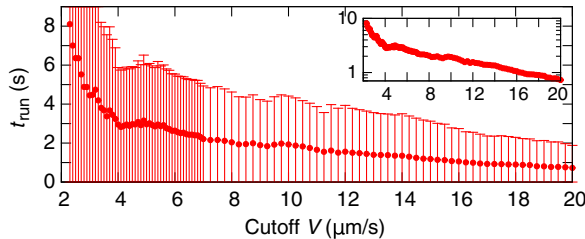


FIG. 8. Average run duration as a function of the threshold in bacterial velocity (cutoff V). The runs are identified as continuous parts of the track where $V > \text{cutoff } V$. The plot demonstrates that an arbitrary choice of velocity drops along the trajectory leads to arbitrary run-time duration. Inset: Log-normal plot.

APPENDIX B: PERSISTENCE CORRELATION FUNCTION

The orientation correlation function is defined as

$$C(\tau) = \langle \hat{p}(t) \cdot \hat{p}(t + \tau) \rangle = \langle \cos[\theta(\tau)] \rangle, \tag{B1}$$

where \hat{p} is the director vector and the average is done over time t .

To compute the correlation function, we use a kinetic theory approach. The object under study is the distribution function $f(\hat{p}, t)$, which gives the probability that a bacterium has an orientation \hat{p} at time t . In this context, the correlation function is obtained assuming that the initial condition at $t = 0$ is with the bacterium pointing in a specific direction, say, \hat{p}_0 . Hence, we have to compute $C(\tau) = \langle \hat{p}(\tau) \cdot \hat{p}_0 \rangle$, where now the average is over the distribution function. At the end, another average, over \hat{p}_0 , should be done. In practice, this last average is unnecessary by the isotropy of space, because the first average gives already a value independent of \hat{p}_0 .

The distribution function obeys the kinetic equation [52,53]

$$\frac{\partial f}{\partial t} = -L f, \tag{B2}$$

with

$$f(\hat{p}, 0) = \delta(\hat{p} - \hat{p}_0) \tag{B3}$$

and L the evolution operator. Two models must be considered. In the case of Brownian rotational diffusivity,

$$L f = -D_r^B \nabla_{\hat{p}}^2 f, \tag{B4}$$

where D_r^B is the rotational diffusion coefficient and $\nabla_{\hat{p}}^2$ is the angular part of the Laplacian. In the case of tumbling with a characteristic switch time τ_s ,

$$L f = \frac{1}{\tau_s} \left[f - \int d\hat{p}' W(\hat{p}', \hat{p}) f(\hat{p}') \right]. \tag{B5}$$

The kernel $W(\hat{p}', \hat{p})$ gives the probability that for a swimmer with director \hat{p}' , after tumbling, the new director is \hat{p} . It is normalized to $\int d\hat{p}' W(\hat{p}', \hat{p}) = 1$, indicating that some director \hat{p} must be chosen. If the space is isotropic, the kernel depends only on the relative angle between the directors, that is, $W(\hat{p}', \hat{p}) = w(\hat{p}' \cdot \hat{p})$. Finally, if tumbling and diffusion are present, the operator is just the sum of both.

If the space is isotropic, the evolution operator is also isotropic, which in this case implies that it commutes with the angular Laplacian $\nabla_{\hat{p}}^2$. Therefore, both operators share eigenfunctions, which are the spherical harmonics $Y_{lm}(\hat{p})$. Then, there are eigenvalues λ_l ,

$$LY_{lm} = \lambda_l Y_{lm}, \quad (\text{B6})$$

that, by isotropy, do not depend on the second index m . For the diffusion case, the eigenvalues are known exactly, while for tumbling they are proportional to $1/\tau_s$ and depend on the kernel model. In summary,

$$\lambda_l = D_r^B l(l+1) + 1/(a_l \tau_s), \quad (\text{B7})$$

where a_l are dimensionless parameters of the order of 1 that depend on the kernel w .

Using the basis of the spherical harmonics, the solution of the kinetic equation (B2) is

$$f(\hat{p}, t) = \sum_{lm} f_{lm}(0) Y_{lm}(\hat{p}) e^{-\lambda_l t}, \quad (\text{B8})$$

where $f_{lm}(0)$ depend on the initial condition (B3).

Now, the correlation function is

$$C(t) = \langle \hat{p}(t) \cdot \hat{p}_0 \rangle \quad (\text{B9})$$

$$= \int d\hat{p} \hat{p}_0 \cdot \hat{p} f(\hat{p}, t) \quad (\text{B10})$$

$$= \sum_{lm} f_{lm}(0) e^{-\lambda_l t} \hat{p}_0 \cdot \int d\hat{p} \hat{p} Y_{lm}(\hat{p}). \quad (\text{B11})$$

Using that \hat{p} can be written as a linear combination of Y_{1m} , with $m = 0, \pm 1$ and the orthogonality of the spherical harmonics, it is obtained that the integral is not vanishing only for $l = 1$. Combining factors, one obtains

$$C(t) = C_0 e^{-t/\tau_p}, \quad (\text{B12})$$

where

$$\tau_p = \frac{a_1 \tau_s}{1 + a_1 \tau_s / \tau_B} \quad (\text{B13})$$

and $\tau_B = 1/(2D_r^B)$ is the Brownian decorrelation time.

In the classical picture, where all bacteria have a single value for τ_s , the decorrelation time τ_p is single valued also. When τ_s is broadly distributed, the decorrelation time τ_p also follows a broad distribution for $\tau_p \ll \tau_B$, and it is bounded from above by τ_B . Finally, in the description of Berg and Brown [1], the tumble angles are distributed with a peak at 63° . In this case, $a_1 = 1/(1 - \langle \cos \theta \rangle)$ [51].

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