

# Table of Contents

|   |           |
|---|-----------|
| <b>Introduction</b>   | <b>1</b>  |
| <b>1. Background</b>  | <b>3</b>  |
| 1.1. Gaussian Processes . . . . .                                     | 3         |
| 1.1.1. Gaussian Process Regression . . . . .                          | 4         |
| 1.2. Spectral Representation of Stationary Kernels . . . . .          | 5         |
| 1.3. Multi-Output Gaussian Processes . . . . .                        | 7         |
| 1.3.1. Multi-Output Gaussian Process Regression . . . . .             | 8         |
| 1.4. Existing work on Multi-Output Gaussian Processes . . . . .       | 9         |
| 1.4.1. Linear Model of Coregionalization . . . . .                    | 9         |
| 1.4.2. Intrinsic Coregionalization Model . . . . .                    | 10        |
| 1.4.3. Semi-Parametric Latent Factor Model . . . . .                  | 10        |
| 1.4.4. Convolution Model . . . . .                                    | 11        |
| 1.4.5. Cross-Spectral Mixture kernel . . . . .                        | 12        |
| 1.4.6. Multi-Output Spectral Mixture Kernel . . . . .                 | 13        |
| 1.5. Harmonizable Processes . . . . .                                 | 14        |
| <b>2. Multi-Output Harmonizable Spectral Mixture Kernel</b>           | <b>17</b> |
| 2.1. Derivation of the Proposed Kernel . . . . .                      | 17        |
| 2.2. Relationship with Other Models . . . . .                         | 22        |
| 2.3. Expressiveness of the Model . . . . .                            | 23        |
| 2.4. Practical Considerations . . . . .                               | 24        |
| 2.4.1. Training and Prediction . . . . .                              | 24        |
| 2.4.2. Parameter Initialization . . . . .                             | 25        |
| 2.5. Varying the Global Component of the Spectral Densities . . . . . | 27        |
| <b>3. Experiments</b>   | <b>30</b> |
| 3.1. Learning Derivatives and Delayed Signals . . . . .               | 30        |
| 3.2. GONU Data . . . . .  | 32        |
| 3.3. EEG Data . . . . .   | 35        |
| <b>Conclusion</b>   | <b>37</b> |
| <b>Bibliography</b>   | <b>38</b> |