THE DISTANCE TO SN 1999em FROM THE EXPANDING PHOTOSPHERE METHOD¹

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ABSTRACT

We present optical and infrared spectroscopy of the first 2 months of evolution of the Type II supernova SN 1999em. We combine these data with high-quality optical/infrared photometry beginning only 3 days after shock breakout, in order to study the performance of the "expanding photosphere method" (EPM) in the determination of distances. With this purpose, we develop a technique to measure accurate photospheric velocities by cross-correlating observed and model spectra. The application of this technique to SN 1999em shows that we can reach an average uncertainty of 11% in velocity from an individual spectrum. Our analysis shows that EPM is quite robust to the effects of dust. In particular, the distances derived from the VI filters change by only 7% when the adopted visual extinction in the host galaxy is varied by 0.45 mag. The superb time sampling of the BVIZJHK light curves of SN 1999em permits us to study the internal consistency of EPM and test the dilution factors computed from atmosphere models for Type II plateau supernovae. We find that, in the first week since explosion, the EPM distances are up to 50% lower than the average, possibly because of the presence of circumstellar material. Over the following 65 days, on the other hand, our tests lend strong credence to the atmosphere models, and confirm previous claims that EPM can produce consistent distances without having to craft specific models to each supernova. This is particularly true for the VI filters, which yield dis-

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tances with an internal consistency of 4%. From the whole set of BVIZJHK photometry, we obtain an average distance of 7.5 ± 0.5 Mpc, where the quoted uncertainty (7%) is a conservative estimate of the internal precision of the method obtained from the analysis of the first 70 days of the supernova evolution.

Subject headings: distance scale — galaxies: distances and redshifts — supernovae: general — supernovae: individual (SN 1999em)

1. INTRODUCTION

The last 10 years have witnessed enormous progress in our knowledge of the optical properties of supernovae (SNe) of all types. However, comparatively little is still known about these objects in infrared (IR) wavelengths. Light curves in the JHK bands have been obtained for only a handful events since the pioneering work of Elias et al. (1981, 1985) on Type Ia SNe. Aside from SN 1987A (e.g., Suntzeff & Bouchet 1990), SN 1990E (Schmidt et al. 1993), and SN 1980K (Dwek et al. 1983), there are only a few Type II SNe with sparse JHK light curves (Mattila & Meikle 2001). The spectroscopic studies have also been mostly limited to optical wavelengths (3000-10000 Å), and except for the Type II SN 1987A (Elias et al 1988; Meikle et al. 1989), SN 1995V (Fassia et al. 1998), and SN 19985 (Fassia et al. 2001), few spectra have been obtained beyond this range. Bowers et al. (1997) presented a summary of the few IR spectra obtained for Type Ia SNe.

Given the rapid technological development of IR light detection over recent years, the next logical step is to expand the SN observations to the broadest possible spectral range. With this idea in mind, in 1999 we started a program to obtain optical and IR photometry and spectroscopy of nearby SNe (z < 0.08), in order to better understand (1) the nature of SNe, (2) the explosion mechanisms, (3) the relation of SN properties to their stellar environments, and (4) the use of SNe as distance indicators. The Supernova Optical and Infrared Survey (SOIRS) uses telescopes at the Cerro Tololo Inter-American Observatory (CTIO), the Carnegie Institution of Washington at Las Campanas Observatory (LCO), the European Southern Observatory (ESO) at La Silla and Cerro Paranal, the Steward Observatory (SO) of The University of Arizona, and the Cerro El Roble observatory of the University of Chile. To ensure sufficient targets for the observing runs, we schedule SN search runs with the Maksutov camera at Cerro El Roble (Maza et al. 1981) prior to the follow-up runs. With photographic film, this camera permits us to sample a wide field of view $(5^{\circ} \times 5^{\circ})$ down to a limiting magnitude of 18. With this setup the photographic survey finds SNe up to z = 0.08, which are ideally suited to the follow-up program. We also coordinate the follow-up runs with the Nearby Galaxies Supernova Survey (NGSS) carried out with the Kitt Peak 0.9 m telescope and the wide-field mosaic CCD array, which discovers SNe down to a limiting magnitude of $R \sim 21$ (z < 0.15; Strolger et al. 1999). We include in our list of targets SNe found at other observatories and reported in the IAU Circulars.

In the course of 1999–2000 the SOIRS program has gathered high-quality observations for ~20 SNe. In this paper we report observations of one of the best-observed objects included in our program, the Type II SN 1999em discovered on 1999 October 29 (JD 2451480.94) in the course of the Lick Observatory Supernova Search (Li 1999). The supernova occurred in NGC 1637, a spiral galaxy with a heliocentric radial velocity of 717 km s⁻¹ (Haynes et al. 1998). A prediscovery image of NGC 1637 taken on

October 20.45 showed nothing at the position of SN 1999em (with a limiting magnitude of ~19.0), which indicated that the SN had been caught at an early stage. An optical spectrum taken 1 day later (October 30.34) showed that SN 1999em had the H line P Cygni profiles characteristic of a Type II event. The blue continuum and the presence of the He I λ 5876 line confirmed that SN 1999em had been found at an early epoch (Jha et al. 1999). Given its proximity and early evolutionary stage, SN 1999em proved to be an excellent target to test the "expanding photosphere method" (EPM) in detail, and determine the distance to the host galaxy.

The discovery of SN 1999em occurred right in the middle of a SOIRS observing campaign previously scheduled for 1999 October–December. As soon as the discovery of SN 1999em was reported, we decided to initiate a follow-up program in order to obtain high-quality data for this event. During this observing run we obtained superb optical and IR sampling of the first 180 days of the UBVRIZJHK light curves, as well as optical/IR spectroscopy for the first 60 days of the evolution of SN 1999em. Except for the subluminous/peculiar SN 1987A, this object is the bestobserved event of the Type II class to date.

All the photometry for SN 1999em, except for the Zband, was reduced and analyzed by Suntzeff and coworkers and will be published separately. In § 2.1 we give a brief summary of these observations and describe the main features of the light curves. We also report the Z-band photometry of SN 1999em. In § 2.2 we summarize our spectroscopic observations and present the resulting spectra. In § 3 we use EPM to compute the distance to the host galaxy, after which $(\S 4)$ we discuss our results. Finally (§ 5), we present the main conclusions of this study. In Appendix A we summarize the basic ideas behind EPM and our implementation to compute distances to SNe II. Appendix B describes the details of computing the synthetic magnitudes required by EPM. Having defined our synthetic photometric system, in Appendix C we proceed to compute the distance correction factors from the SN II atmosphere models published by Eastman, Schmidt, & Kirshner (1996, hereafter E96). In Appendix D we define the Z photometric system and list magnitudes for the standards that we used in our observations.

2. OBSERVATIONS AND REDUCTIONS

2.1. Photometry

We obtained extensive optical and IR photometric follow-up of SN 1999em covering 180 days from discovery until the SN went behind the Sun. The data will be presented in a separate paper by N. B. Suntzeff et al. (in preparation). Table 1 lists additional *UBVRI* observations taken with the CTIO 1.5 m, SO 1.5 m, SO 2.3 m, and ESO NTT telescopes. We include in this table Z-band photometry gathered with the CTIO 0.9 m and reduced relative to a photometric sequence properly calibrated with respect to the standards listed in Appendix D. In the following discussion we adopt a minimum photometric uncertainties beyond the photon

TABLE 1UBVRIZ PHOTOMETRY OF SN 1999em

| JD -2451000 | U | В | V | R | Ι | Ζ | Telescope |
|-------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|
| 481.76 | | | | | | 13.703 (015) | CTIO 0.9 m |
| 483.72 | | ••• | | | | 13.607 (015) | CTIO 0.9 m |
| 484.76 | | | | | | 13.570 (015) | CTIO 0.9 m |
| 485.79 | | ••• | | | | 13.542 (015) | CTIO 0.9 m |
| 486.80 | | ••• | | | | 13.549 (015) | CTIO 0.9 m |
| 487.76 | | | | | | 13.512 (015) | CTIO 0.9 m |
| 488.80 | | ••• | | | | 13.514 (015) | CTIO 0.9 m |
| 489.81 | | | | | | 13.489 (015) | CTIO 0.9 m |
| 498.78 | 14.420 (017) | 14.357 (015) | 13.869 (015) | 13.600 (015) | 13.483 (015) | ••• | CTIO 1.5 m |
| 499.81 | 14.522 (017) | 14.414 (015) | 13.894 (015) | 13.599 (015) | 13.482 (015) | | CTIO 1.5 m |
| 501.75 | ••• | ••• | ••• | ••• | ••• | 13.296 (015) | CTIO 0.9 m |
| 506.77 | | ••• | | | ••• | 13.265 (015) | CTIO 0.9 m |
| 508.82 | | | | | | 13.241 (015) | CTIO 0.9 m |
| 509.86 | | ••• | | | ••• | 13.234 (015) | CTIO 0.9 m |
| 511.85 | | 14.833 (015) | 13.968 (015) | 13.633 (015) | 13.414 (015) | ••• | SO 2.3 m |
| 522.70 | 16.043 (015) | 15.142 (015) | 14.016 (015) | 13.618 (015) | 13.351 (015) | | SO 1.5 m |
| 531.76 | ••• | 15.185 (015) | 14.011 (015) | 13.577 (015) | 13.284 (015) | | SO 2.3 m |
| 538.56 | | | , | | | 13.090 (015) | CTIO 0.9 m |
| 540.55 | | | | | | 13.102 (015) | CTIO 0.9 m |
| 546.55 | | | | | | 13.112 (015) | CTIO 0.9 m |
| 550.55 | | | | | | 13.108 (015) | CTIO 0.9 m |
| 578.63 | | 16.060 (015) | 14.409 (015) | 13.828 (015) | 13.492 (015) | | SO 1.5 m |
| 607.64 | | 18.388 (040) | 16.467 (015) | 15.541 (015) | 14.956 (015) | | SO 1.5 m |
| 636.04 | 21.300 (400) | 18.370 (030) | 16.658 (015) | 15.721 (015) | 15.239 (015) | 14.924 (015) | ESO NTT |
| 665.97 | ••• | 18.600 (035) | 16.968 (015) | 15.999 (015) | 15.503 (025) | •••• | ESO NTT |

statistics quoted by Suntzeff et al. Figure 1 presents the light curves, which reveal the exceptional sampling obtained. The U light curve shows that maximum light occurred just after discovery, on JD 2451482.8 (October 31), followed by a phase of rapid decline during which the SN dimmed by ~ 4 mag in 70 days. The faintness of the SN made further observations through the U filter difficult. The B light curve shows that maximum occurred two days later than in U, a rapid decline for ~ 30 days during which the SN dimmed by



FIG. 1.—UBVRIZJHK light curves of SN 1999em

~1 mag, a phase of 70 days of slowly decreasing luminosity (plateau) during which the flux decreased by one additional magnitude, a fast drop in flux by 2.5 mag in only 30 days, and a linear decay in magnitude as of JD 2451610 that signaled the onset of the nebular phase. The V light curve was characterized by a plateau of nearly constant brightness that lasted ~100 days (until JD 2451580), followed by a drop of 2 mag in ~30 days, and a linear decline at the slow pace of ~0.01 mag day⁻¹. The R, I, Z, J, H, and K light curves had the same basic features as the V light curve, except that the SN gradually increased its luminosity during the plateau. The brightening increased with wavelength, and reached 0.5 mag in the K band.

Barbon, Ciatti, & Rosino (1979) divided Type II SNe into two main subclasses according to their photometric behavior in blue light. The observations of SN 1999em clearly show that this object belongs to the "plateau" (SNe II-P) group, the most frequent type of SNe II, as opposed to the "linear" (SNe II-L) class, which is characterized by a rapid postmaximum decline in brightness.

Figure 2 shows some of the color curves of SN 1999em. They all reveal the reddening of the SN due to the cooling of its atmosphere. In U-B and B-V, the reddening was more pronounced because of the many metal lines that depressed the SN flux at the wavelengths sampled by the Uand B bands. The V-I color, on the other hand, was less affected by line blanketing and better sampled the continuum emission. The evolution of SN 1999em in this color showed rapid cooling during the first 50 days, after which V-I remained nearly constant for another ~30 days. During this phase, the photosphere was near the hydrogen recombination surface and was then of nearly constant temperature (E96). The end of the plateau phase at JD 2451580 coincided with a sudden reddening of the SN, while the exponential tail was characterized by a nearly constant V-I color.



FIG. 2.—Color curves of SN 1999em

2.2. Spectroscopy

We obtained optical and IR spectra of SN 1999em with the ESO NTT/EMMI at La Silla and VLT/ISAAC at Cerro Paranal between 1999 November 2 and 28, and additional optical spectra with the CTIO 1.5 m telescope on October 30 (one day after discovery), and the SO Bok 2.3 m telescope and Boller & Chivens spectrograph on December 16 and 31. Table 2 presents a journal of the observations.

2.2.1. Optical Spectroscopy

The NTT observations employed three different setups. We used the blue channel of EMMI equipped with a Tek CCD (1024 \times 1024) and grating 5 (158 lines mm⁻¹), which, in first order, delivered spectra with a dispersion of 3.5 Å pixel⁻¹ and a useful wavelength range between 3300 and 5250 Å. With the red channel, CCD Tek 2048, and grating 13 (150 lines mm⁻¹), the dispersion was 2.7 Å pixel⁻¹ and the spectral coverage ranged from 4700 through 11000 Å in first order. Since this setup had potential second-order contamination beyond \sim 6600 Å, we decided to take one spectrum with the OG530 filter and a second observation without the filter, in order to provide an overlap with the

blue spectrum. Thus, a single-epoch observation usually consisted of three spectra. On two occasions (November 3 and 14), however, we were unable to obtain the observation with the OG530 filter, so the red end of the spectra were most likely contaminated by second-order blue light (more below).

The observations with EMMI started with calibrations during daytime (bias and dome flat-field exposures). The night began with the observation of a spectrophotometric standard (from the list of Hamuy et al. 1994) through a wide slit of 10", after which we observed the SN with a slit of 1". We took two exposures per spectral setup, each of the same length (typically 120–180 s) and always along the parallactic angle. Immediately following this observation we observed an He-Ar lamp, at the same position of the SN and before changing the optical setup, in order to ensure an accurate wavelength calibration. At the end of the night we observed a second flux standard.

We carried out all reductions using IRAF.⁷ They consisted of subtracting the overscan and bias from every frame. Next, we constructed a flat field from the guartz-lamp image, duly normalized along the dispersion axis. We proceeded by flat-fielding all the object frames and extracting one-dimensional spectra from the two-dimensional images. We followed the same procedure for the He-Ar frames, which we used to derive the wavelength calibration for the SN. We then derived a response curve from the two flux standards, which we applied to the SN spectra in order to get flux-calibrated spectra. During this process we also corrected for atmospheric extinction using an average continuum opacity curve scaled for the air mass at which we observed the object, but we did not attempt to remove telluric lines. From the pair of flux-calibrated spectra that we secured for each spectral setup, we removed cosmic rays and bad pixels and obtained a clean spectrum of the SN. The last step consisted of merging the three spectra that sampled different wavelength ranges. To avoid discontinuities in the combined spectrum, we grayshifted the three spectra relative to each other. Finally, we computed the synthetic V-band magnitude from the resulting spectrum (following the precepts described in Appendix B) and grayshifted it so that the flux level matched our observed Vmagnitude. We checked the spectrophotometric quality of

⁷ IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

| TABLE 2 |
|---|
| JOURNAL OF THE SPECTROSCOPIC OBSERVATIONS |

| UT Date | Julian Date - 2451000 | Observatory | Telescope | Wavelength (µ) | Dispersion (Å pixel ⁻¹) | Weather | Observer (s) |
|-------------|--------------------------|-------------|-----------|-------------------|--|---------|-----------------------|
| 1999 Oct 30 | 481.79 | Tololo | 1.5 m | 0.33-0.97 | 5.7 | | Smith |
| 1999 Nov 2 | 484.64 | Paranal | VLT/Antu | 0.98-2.50 | 2.9-7.1 | clear | Hamuy, Lidman, Petr |
| 1999 Nov 3 | 485.67 | La Silla | NTT | 0.33-1.01 | 2.7-3.5 | clear? | Maza |
| 1999 Nov 9 | 491.67 | La Silla | NTT | 0.33-1.00 | 2.7-3.5 | clear | Hamuy, Brillant |
| 1999 Nov 14 | 496.67 | La Silla | NTT | 0.33-1.01 | 2.7-3.5 | clear | Hamuy, Doublier |
| 1999 Nov 18 | 500.64 | Paranal | VLT/Antu | 0.98-2.54 | 2.9-7.1 | clear | service observing |
| 1999 Nov 19 | 501.66 | La Silla | NTT | 0.33-1.01 | 2.7-3.5 | clear | Hamuy, Doublier |
| 1999 Nov 28 | 510.63 | Paranal | VLT/Antu | 0.98-2.53 | 2.9-7.1 | clear | Hamuy, Lidman, Chadid |
| 1999 Dec 16 | 528.76 | Steward | 2.3 m | 0.49-0.93 | 3.6 | clear | Corbally, Omizzolo |
| 1999 Dec 31 | 543.76 | Steward | 2.3 m | 0.33-0.71 | 3.6 | | Burstein, Li |

the spectra by computing synthetic magnitudes for the BRIZ bands. This test showed differences between the synthetic and observed magnitudes of up to 0.03 mag in the B and R bands, which implies that the relative spectrophotometry at these wavelengths was very good. The I and Z synthetic magnitudes, on the other hand, disagreed with the observed magnitudes by up to 0.1 mag, particularly when the blocking filter could not be used; second-order contamination was as large as 10% at those wavelengths.

We obtained a spectrum of the SN 1 day after discovery with the CTIO 1.5 m telescope and the Cassegrain spectrograph, a 1200×800 LORAL CCD, grating 16 (527 lines mm^{-1}) and 2" slit, in first order. The resulting spectrum had a dispersion of 5.7 Å pixel⁻¹ and useful wavelength coverage of 3300-9700 Å. Second-order contamination was expected beyond 6600 Å because of first-order 3300 Å light, since we did not use a blocking filter. On two nights we employed the SO Bok telescope with the Boller & Chivens spectrograph, a 1200×800 LORAL CCD, and a 300 lines mm^{-1} grating which, in first order, produced spectra with a dispersion of 3.6 Å pixel⁻¹. The wavelength coverage was 4900-9300 Å on December 16 and 3500-7100 Å on December 31. We did not include a blocking filter in the optical path, so it could well be that these spectra were affected by second-order contamination beyond 6600 Å. The observing and reduction procedures for the CTIO and SO spectra were the same as those described above for the NTT data.

Figure 3 displays the optical spectra in the rest-frame of the SN, after correcting the observed spectra for the 717 km s⁻¹ recession velocity of the host galaxy. The strongest SN lines are indicated along with the telluric lines (by circled crosses). The first spectrum, taken on JD 2451481.79 (1 day after discovery), showed a blue continuum with a *BVI* color temperature of 15,600 K, P Cygni profiles for the H Balmer



FIG. 3.—Optical spectroscopic evolution of SN 1999em in AB magnitudes. Julian Day (-2451000) is indicated for each spectrum. Some of the strongest lines are labeled. Circled crosses show the main telluric features.

lines, and the He I λ 5876 line, which is characteristic of SNe II during their hottest phases. The expansion velocity from the minimum of the absorption features was ~10,000 km s⁻¹, which is typical of SNe II during the initial phases. The presence of the interstellar Na I D lines $\lambda\lambda$ 5890, 5896 with an equivalent width of ~2 Å suggested substantial interstellar absorption in the host galaxy. However, there is additional evidence that the SN did not suffer significant extinction (see § 3.3), so we did not attempt to correct for dust the spectra of Figure 3.

As the SN evolved the atmospheric temperature dropped, the He I λ 5876 line disappeared, and several new lines became evident, namely, the Ca II H and K $\lambda\lambda$ 3934, 3968 blend, the Ca II triplet $\lambda\lambda$ 8498, 8542, 8662, the Na I D blend, and several lines attributed to Fe II, Sc II, and Ba II. Table 3 summarizes the line identifications, their rest wavelengths (taken from the list of Jeffery & Branch 1990), and their wavelengths measured from the absorption minimum. We include several lines with unknown identifications in this table. By the time of our last spectrum on JD 2451543.76 (62 days after discovery), the *BVI* color temperature was only 5000 K, approximately the recombination temperature of H.

2.2.2. Infrared Spectroscopy

We obtained three IR spectra with the VLT/Antu telescope at Cerro Paranal, between November 2 and 28. We employed the IR spectro-imager ISAAC (Moorwood 1997) in low-resolution mode ($R \sim 500$), with four different gratings that permitted us to obtain spectra in the Z, J, H, and K bands. We used these gratings in 5th, 4th, 3d, and 2d order, respectively, which yielded useful data in the spectral ranges 9840–11360, 11090–13550, 14150–18180, and 18460– 25600 Å. The detector was a Hawaii-Rockwell 1024 × 1024 array.

A typical IR observation started during daytime by taking calibrations. We began taking flat-field images using an internal source of continuum light. We secured multiple on- and off-image pairs with the same slit used during the night (0".6). We then took Xe-Ar lamp images (and off-lamp images) with a narrow slit (0".3) in order to map geometric distortions. The observations of SN 1999em consisted of an O-S-O-S-O cycle, where O is an on-source image and S is a sky (off-source) frame. Given that the angular size of the host galaxy was comparable to the slit length (2'), it was not possible to use the classical technique of nodding the source along the slit, and it proved necessary to offset the telescope by several minutes of arc to obtain the sky images. At each position we exposed for 200 s, conveniently split into two 100 s images in order to remove cosmic rays and bad pixels from the final spectra. After completing the O-S-O-S-O cycle, we immediately obtained a pair of on-off arc lamp exposures without moving the telescope or changing optical elements, to ensure an accurate wavelength calibration. We then switched to the next grating and repeated the above object-arc procedure until completing the observations with the four setups. For flux calibration, we observed a bright solar-analog star close in the sky to the SN, in order to minimize variations in the atmospheric absorptions (Maiolino, Rieke, & Rieke 1996). The selected star was Hip 21488, of spectral type G2 V, V = 8.5, B - V = 0.6, and located only 12° from the SN (SIMBAD Astronomical Database). In this case we nodded the object between two positions (A and B) along the slit, and we took two AB pairs for each grating. To avoid saturating the detector, we took

| | TABLE 3 | | | | |
|---|----------------|------------|----------|-------|--------|
| OPTICAL LINE IDENTIFICATIONS AND OBSERVED | WAVELENGTHS OF | ABSORPTION | Features | of SN | 1999em |

| | | Oct 30 | Nov 3 | Nov 9 | Nov 14 | Nov 19 | Dec 16 | Dec 31 |
|----------------------|--------------------|--------|----------|--------|--------|--------|--------|--------|
| Identification | λ_{rest} | 481.79 | 485.67 | 491.67 | 496.67 | 501.66 | 528.76 | 543.76 |
| | | | | 3671 | 3671 | 3675 | | 3683 |
| СапК | 3934 | | | 3846 | 3847 | 3852 | | 3868 |
| СапН | 3968 | | | 3846 | 3847 | 3852 | | 3868 |
| Ηδ | 4102 | | 3996 | 4016 | 4021 | 4029 | | 4025 |
| | | | | | 4095 | 4107 | | |
| Sr II + Ca I + Fe II | 4225 | | | | 1050 | 4169 | | 4178 |
| H _v | 4340 | 4214 | 4224 | 4234 | 4240 | 4246 | | 4260 |
| Тіπ | 4395 | 1211 | 1221 | 1251 | 1210 | 4318 | | 4342 |
| 11 | 4575 | | ••• | ••• | ••• | 4510 | ••• | 4412 |
| Вап – Тіп | 4552 | | 4370 | 4425 | 4458 | 4473 | ••• | 4500 |
| | 4552 | ••• | 4370 | 4423 | 44,50 | 4475 | ••• | 4500 |
| Т П | 4023 | | ••• | ••• | ••• | ••• | ••• | 4500 |
| | ••• | ••• | ••• | ••• | ••• | ••• | ••• | 4020 |
| | | | | | | | ••• | 4693 |
| Ηβ | 4861 | 4694 | 4721 | 4735 | 4746 | 4761 | | 4763 |
| | | | | | | 4836 | ••• | 4817 |
| Fe п + Ва п | 4929 | | | | | | | 4874 |
| Fe п | 5018 | | | 4911 | 4920 | 4934 | 4965 | 4969 |
| Fe п + Mg I + Ti п | 5185 | | | 5047 | 5065 | 5081 | 5113 | 5117 |
| - | | | | | | | 5178 | 5182 |
| Fe I | 5270 | | | 5178 | 5208 | 5229 | 5221 | 5229 |
| | | | | | | | 5263 | 5270 |
| | | | | | | | 5373 | 5376 |
| Sc II + Fe II | 5531 | | | | | 5437 | 5475 | 5481 |
| | 5695 | ••• | | ••• | ••• | 5457 | 5607 | 5612 |
| | 5076 | 5665 | 5710 | | ••• | | 5007 | 5012 |
| He I | 5870 | 2002 | 5/18 | ••• | | | | |
| Na I | 5893 | | ••• | | ••• | 5789 | 5829 | 5831 |
| Fe II + Ba II | 6146 | | | ••• | | 6042 | 6086 | 6093 |
| Fe п + Sc п | 6244 | | | | | 6144 | 6184 | 6194 |
| Si п | 6355 | | | ••• | | | 6316 | 6319 |
| Ηα | 6563 | 6292 | 6337 | 6362 | 6379 | 6392 | 6455 | |
| Сап | 8498 + 8542 + 8662 | | | | | 8344 | 8380 | |

NOTE.—All wavelengths are measured in Å in the SN rest frame.

the shortest possible exposures (1.77 s) allowed by the electronics that controlled the detector. Since the minimum time required before offsetting the telescope was ~ 60 s, we took 10 exposures at each position, which provided an exceedingly good signal-to-noise ratio (S/N) for the flux standard.

The reductions of the IR data began by subtracting the off-lamp images from the on-lamp flat-field frames, median filtering the multiple flat images, and normalizing the resulting frame along the dispersion axis. Then we divided all the object images by the normalized flat field. The next step consisted of mapping the geometric distortions using the arc lamp taken with the narrow slit. The emission lines displayed a curvature of a few pixels across the spatial direction of the image. From the narrow-slit arc exposure we obtained sharp emission lines, which allowed us to form a two-dimensional map of the distortions. We then fitted a low-order two-dimensional polynomial to the line tracings, after which we applied a geometric correction to all the images obtained during the night. Since the sky background is so large in the IR, a small flat-fielding residual or a patchy sky can introduce large background fluctuations. This made it necessary to subtract the sky from the two-dimensional images before attempting to extract the object spectrum. Given that the IR sky changes on short timescales, we always used the sky image taken immediately before or after the SN frame. We followed the same procedure for the flux standard. We then extracted one-dimensional spectra of the SN and the spectrophotometric standard from the skysubtracted frames, making sure to subtract residual sky from a window adjacent to the object. We also extracted a spectrum of the Xe-Ar frame taken at the same position of the SN, in order to derive a wavelength calibration. We then combined the multiple spectra of the SN and the standard with a "minmax" rejection algorithm that removed deviant pixels from the average at each wavelength.

Flux calibration in the IR is in general quite involved, because there are no flux standards at these wavelengths. To get around this problem we adopted the technique described by Maiolino et al. (1996), which consists of dividing the spectrum of interest by a solar-type star to remove the strong telluric IR features, and multiplying the resulting spectrum by the solar spectrum to eliminate the intrinsic features (pseudonoise) introduced by the solar-type star. In its original version this method used a solar spectrum normalized by its continuum slope, so the object's spectrum was not properly flux calibrated. More recently, this technique was modified to incorporate a flux-calibrated semiempirical spectrum of the Sun, so that the object's final spectrum is in flux units.⁸ The adopted spectrum is a combination of the observed solar line spectrum in the JHKbands (Livingston & Wallace 1991) and the Kurucz solar model with parameters $T_{\rm eff} = 5777$ K, $\log g = 4.4377$,

 8 For more details, see http://www.arcetri.astro.it/ \sim maiolino/solar/solar.html.



FIG. 4.—IR spectroscopic evolution of SN 1999em in AB magnitudes. The most prominent features are labeled. Julian Day (-2451000) is indicated for each spectrum.

[Fe/H] = 0, and $V_{microturb} = 1.5 \text{ km s}^{-1}$ (Kurucz 1995). In the Vega magnitude system (described in Appendix B), the solar spectrum has a visual magnitude of -26.752. The remaining broadband magnitudes are listed below in Table 12.

Before using the solar spectrum, we convolved it with a kernel function in order to reproduce the spectral resolution of the solar-analog standard Hip 21488, and we scaled it down to the equivalent of V = 8.5, which corresponds to the observed magnitude of Hip 21488. From the ratio of this solar spectrum and the observed spectrum of Hip 21488, we derived an instrumental response curve that included both the telluric absorption lines and the instru-

| TA | BL | Æ | 4 |
|----|----|---|---|
|----|----|---|---|

IR LINE IDENTIFICATIONS AND OBSERVED WAVELENGTHS OF ABSORPTION FEATURES OF SN 1999em

| Identification | $\lambda_{ m rest}$ | Nov 2 484.64 | Nov 18 500.64 | Nov 28 510.63 |
|----------------|---------------------|-----------------|------------------|------------------|
| Ρδ | 10049 | | 9901 | 9909 |
| Sr II? | 10327 | | | 10180 |
| Fe II? | 10547 | | 10418 | 10418 |
| C I + He I? | 10695 + 10830 | | | 10549 |
| Не 1 | 10830 | 10503 | | |
| Ργ | 10938 | | 10741 | 10788 |
| Ρβ | 12818 | 12473 | 12573 | 12627 |
| Βθ | 16412 | | | 16219 |
| Βη | 16811 | | 16566 | 16612 |
| Βζ | 17367 | | 17108 | 17150 |
| Βε | 18179 | | 17884 | 17949 |
| Ρα | 18751 | | | |
| Βδ | 19445 | | | 19210 |
| Βγ | 21656 | | 21289 | 21368 |

Note.—All wavelengths are measured in Å in the SN rest frame.



FIG. 5.—Combined optical and IR spectra of SN 1999em in AB magnitudes. The IR spectra were obtained 1 day before the optical observation, and the mean Julian Day (-2451000) is indicated next to each spectrum. The flux excess between 7500 and 10000 Å in the first-epoch spectrum is due to second-order blue light contamination.

mental sensitivity of ISAAC. Finally, we multiplied the SN spectrum by the response function to obtain the fluxcalibrated SN spectrum. This technique worked very well to remove telluric lines. On the other hand, it introduced a small systematic error in the flux calibration of the SN due to departures between the solar spectrum and the actual spectral energy distribution of the solar-analog standard. According to atmosphere models, the difference in continuum flux for stars with $T_{eff} = 5500$ and 6000 K (which correspond to spectral types G8 V–F9 V; Gray & Corbally 1994) is smaller than 10% in the NIR region. A G2 V star like Hip 21488 has the same spectral type as the Sun, so its effective temperature must be close (within ± 100 K) to that of the adopted solar model. Hence, the flux difference between the solar-analog standard and the adopted spectrum should be less than 10%. The B - V = 0.6 color of Hip 21488 suggests little or no reddening, so the SN spectra fluxes are probably accurate to 5% or better.

The result of these operations are four spectra covering the Z, J, H, and K bands, which we combined into one final spectrum. Given the significant overlap of the Z- and J-band spectra, we were able to grayshift the Z spectrum relative to the J spectrum. Since none of the other spectra overlapped (because of the strong absorption of telluric lines between the J, H, and K bands), we shifted them individually by computing synthetic magnitudes (see Appendix B) and bringing them into agreement with the observed photometry.

Figure 4 shows the resulting rest-frame spectra of SN 1999em, revealing the exquisite spectral resolution and the superb S/N delivered by ISAAC. The first spectrum, taken 4 days after discovery, showed a few prominent lines, namely He I $\lambda 10830$, P α , P β , By, and B δ , on top of a blue contin-

uum. The second spectrum (20 days after discovery) showed prominent $P\gamma$ and $P\delta$ lines in lieu of the strong He I feature. A few faint lines appeared around 17000 Å, from higher transitions in the Brackett series. The third spectrum, taken 30 days after discovery, confirmed the presence of these faint lines. Three lines could be seen at ~ 10500 Å, between $P\gamma$ and $P\delta$. It is possible that the feature at 10180 Å was due to the 10327 Å line of the multiplet 2 of Sr II, which was also observed in SN 1987A (Elias et al. 1988) and SN 1995V (Fassia et al. 1998). The other two lines of the multiplet at 10037 and 10915 Å were probably blended with $P\delta$ and $P\gamma$, respectively. The feature at 10418 Å is probably due to Fe II 10547, which was present in SN 1995V. Meikle et al. (1989) identified the C I λ 10695 multiplet 1 line in an early-time spectrum of SN 1987A, which might be responsible for the 10549 Å feature in the SN 1999em spectrum. They also reported the presence of the He I $\lambda 10830$ absorption line in late-time spectra of SN 1987A. It is possible then that the 10549 Å feature in SN 1999em could be a blend of C I 10695 and He I 10830, as suggested by Fassia et al. (1998). Table 4 summarizes the line identifications, their rest wavelengths, and the values measured from the absorption minima.

Given that two of the IR spectra were obtained 1 day apart from the optical spectra, we were able to combine these observations in Figure 5. This exercise revealed the excellent agreement between the optical and IR fluxes, a result made possible by synthesizing broadband magnitudes and adjusting the flux scales according to the observed magnitudes. Second-order contamination can be clearly seen in the first-epoch spectrum as a flux excess between 7500 and 10000 Å.

3. THE APPLICATION OF THE EXPANDING PHOTOSPHERE METHOD TO SN 1999em

EPM involves measuring a photometric angular radius and a spectroscopic physical radius, from which the SN distance can be derived. In this section we apply the method to SN 1999em following this order. In Appendix A we summarize the basic ideas behind EPM.

3.1. The Angular Radius of SN 1999em

The angular radius, θ , of the SN can be determined from equation (A1) by fitting Planck curves $[B_{\lambda}(T_S)]$ to the observed magnitudes. With two wavelengths the solution is exact (two equations and two unknowns). For three or more wavelengths we use the method of least-squares at each epoch to find the color temperature, T_S , and the parameter $\theta \zeta_S$ that minimize the quantity

$$\chi^2 = \sum_{\bar{\lambda} \in S} \frac{[m_{\bar{\lambda}} + 5 \log (\theta \zeta_S) - b_{\bar{\lambda}}(T_S)]^2}{\sigma_m^2} \,. \tag{1}$$

In this equation $m_{\bar{\lambda}}$ is the SN's apparent magnitude in a photometric band with central wavelength $\bar{\lambda}$, σ_m is the corresponding photometric error, $b_{\bar{\lambda}}(T_S)$ is the synthetic magnitude of $\pi B_{\lambda}(T_S) 10^{-0.4A(\lambda)}$ (computed with the precepts described in Appendix B), and $A(\lambda)$ is the dust extinction affecting the SN. Once $\theta\zeta_S$ is determined from the χ^2 fit, we solve for θ using the dilution factor ζ_S corresponding to filter subset S, which we compute from the color temperature using equation (C2).

Using the VI photometry and adopting a foreground extinction of $A_{\text{Gal}}(V) = 0.13$ (Schlegel, Finkbeiner, & Davis 1998) and $A_{\text{host}}(V) = 0.18$ for dust absorption in the host

FIG. 6.—V magnitude, photospheric angular radius, and color temperature of SN 1999em vs. Julian Day.

galaxy (Baron et al. 2000), we compute T_{VI} and the corresponding angular radius, which are plotted in Figure 6. This figure shows that the initial color temperature was $\sim 13,000$ K and that the SN cooled down for nearly 60 days until reaching a value near 6500 K. The photosphere remained at this temperature for 30 days more until the end of the plateau phase. In the rapid fall off the plateau, the atmosphere cooled to ~ 4000 K, after which the temperature remained nearly constant. At this stage the SN began the nebular phase and the spectrum was dominated by recombination lines, so the color temperature cannot be associated with a thermal process. During the initial cooling period of 60 days, the photospheric radius steadily increased as the photosphere was swept outward by the expansion of the ejecta, and then decreased as the wave of recombination moved into the flow with ever-increasing speed. It is this balance between increasing radius and steady cooling that explains the long plateau of nearly constant luminosity (Fig. 6, top panel). Following the plateau phase, both the radius and the temperature decreased, leading inevitably to the luminosity drop around day JD 2451580.

Since the radiation field forms at a depth that varies with wavelength (depending on the value of the absorptive opacity), the angular radii derived before corrections for the dilution factors are expected to vary significantly depending on the filters employed in the blackbody fits. By contrast, the photosphere is defined as the region of total optical depth $\tau = \frac{2}{3}$, the last scattering surface. Since continuum opacity in the optical and NIR is dominated by electron scattering, the opacity is gray, and the photospheric angular radius is not expected to change with wavelength (E96). We can check this prediction in Figure 7 by comparing the photospheric angular radii derived from filter subsets $\{BV,$ VI, VH for the entire plateau phase of SN 1999em. The relative agreement is excellent (<5%) over the first 10 days of SN evolution, after which there is a period of ~ 30 days in which the photospheric radii derived from the three filter subsets disagree by up to 25%. Over the following 60 days the agreement is much better, at the level of 10%. This test





FIG. 7.—Photospheric angular radius of SN 1999em derived from filter subsets $\{BV, VI, VH\}$, as a function of time.

reveals the overall good agreement of the photospheric radii determined from different filters and the good performance of the dilution factors.

3.2. The Physical Radius of SN 1999em

The next step in deriving an EPM distance involves the determination of photospheric velocities from the SN spectra. To date the photospheric velocities have been estimated from the minimum of spectral absorption features (Schmidt et al. 1992, 1994). There are several problems with this approach, however. First, the location of the line minimum shifts toward bluer wavelengths (higher velocity) as the optical depth of the line and the scattering probability increase. This is a prediction of line profile models in homologously expanding scattering atmospheres (see Fig. 3 of Jeffery & Branch 1990, for example), and is also an observational fact, as Figure 8 demonstrates. This plot shows the expansion velocities derived from the metal (Sr, Ca, Fe, Na, Si) lines of the spectrum taken on 1999 December 31, as a function of the equivalent width of the line. Even though it proves difficult to measure line strengths because of the lack of a well-defined continuum, the trend is quite evident in the sense that stronger features yield higher velocities. It is well known that hydrogen lines (which are not shown in this plot) yield much higher expansion velocities than the metal lines in SN II spectra because of their high optical depths, but no attention has yet been paid to this effect among the weakest absorptions. This plot shows that it is possible to incur significant errors if we measure expansion velocities from the minima of absorption features, even from the weakest lines. Second, even if we could extrapolate the observed velocities to zero strength, the inferred velocity would correspond to that of the thermalization surface (where the radiation field forms) and not to the photosphere (the last scattering surface). Since the dilution factors computed by E96 correspond to the ratio of the luminosity of the SN model to that of a blackbody with the photospheric radius of such a model (see Appendix C), the use of the



FIG. 8.—Expansion velocity derived from the minimum of spectral metal absorptions in the December 31 spectrum vs. the equivalent width of the absorption.

velocity of the thermalization surface is inappropriate, even though it has been common practice in the past. Third, velocities derived from absorption lines are affected by line blending or possible line misidentifications, both of which can lead to an erroneous estimate of the photospheric velocity.

To get around these problems, we adopt an approach based on cross-correlating the SN spectrum with the models of E96 (with known photospheric velocities) using the IRAF fxcor task. Before applying this technique to the observed spectra, we must test it with the model spectra of E96. In doing so, we cross-correlate models with other models having BVI color temperatures within ± 1000 K of each other. For each pair of models, we end up with a relative velocity derived from the cross-correlation (CC) technique, which can then be compared with the actual value. The hope is that the whole set of pairs can be used to derive a relationship between the CC relative velocity and the actual value. We carry out tests separately in the optical and the IR in order to apply this method to spectra observed in different spectral windows. In the optical we select two wavelength ranges (3000-5000 and 5700-6700 Å) and a NIR a window between 10000 and 13500 Å. We end up with these ranges after numerous experiments which show that beyond 13500 Å there are too few spectral lines to help us in constraining the expansion velocity. In the optical, these tests suggest that we eliminate the red wings of the strong H α and H β , which have the potential to bias the derivation of expansion velocities from the CC procedure. Figure 9 compares the CC relative velocities and the actual values, in both the optical and NIR, from the whole set of models (except s15.5.1 and s25.5.1, which are not appropriate for SNe II-P; E96). In both cases we get a reasonable correlation which permits us to convert the velocity offsets measured from cross-correlation into a photospheric velocity. The scatter in these relationships is 900 km s⁻¹, which provides an estimate of the precision in the derivation of a photospheric velocity from a single model. The data can be



FIG. 9.— (a) Relative expansion velocities derived from the crosscorrelation technique for pairs of model spectra with similar color temperatures, vs. the actual relative velocities. The cross-correlation was restricted to the range 3000–5000, 5700–6700 Å. (b) Same as (a), but for the range 10000–13500 Å.

adequately modeled with straight lines, in both the optical and IR. Least-squares fits yield slopes of 1.18 in the optical and 1.38 in the NIR, and zero points of -3 km s^{-1} in both cases. This implies that the magnitude of the relative velocity is *smaller* than the actual value. Overall, this is an encouraging result, although it must be mentioned that the points with the largest scatter in Figure 9 correspond to pairs with the largest temperatures. This means that the precision of the CC technique drops to ~2000 km s⁻¹ when $T_{BVI} > 8000 \text{ K}$.

Having come up with a method for estimating photospheric expansion velocities, we can proceed to derive velocities for SN 1999em. We start by selecting atmosphere models with BVI color temperatures within ± 1000 K of each observed spectrum, after which we cross-correlate the SN spectrum and the subsample of models in the aforementioned wavelength windows. The outcome of this operation is a cross-correlation function (CCF) with a well-defined peak whose location in velocity space gives the relative velocity of the observed and reference spectrum. The height of the CCF is a measure of how well the spectral features of the two spectra match each other. Figure 10 shows examples of the CC technique. Figure 10a compares the optical spectrum obtained on JD 2451501.66 (thick line) with four models of similar color temperature (thin lines), and Figure 10b shows the corresponding CCFs. The two models that best match the observed spectrum, p6.60.1 and p6.40.2, are the ones that give the highest CCF peaks. Models s15.43.3 and s15.46.2, on the other hand, provide poorer matches to the observed spectrum, and consequently the lowest CCF peaks. For each cross-correlation we get a relative velocity that we proceed to correct using the calibrations shown in Figure 9, in order to get the actual relative velocity. Since the photospheric velocities of the models are known, we can



FIG. 10.— (a) Optical spectrum taken on JD 2451501.66 (thick line) compared to four models with similar color temperature (thin lines). The horizontal bars show the wavelength ranges (3000-5000, 5700-6700 Å) used in the derivation of relative velocities from the cross-correlation technique. (b) Cross-correlation function between the observed spectrum and the four models shown above. The two curves with the highest peaks correspond to models p6.60.1 and p6.40.2, both of which match well the observed spectrum. The two lower curves correspond to models s15.43.3 and s15.46.2, which provide a poorer match to the observed spectrum.

derive independent photospheric velocities for each SN spectrum. Table 5 summarizes the velocities derived with this method for all the spectra of SN 1999em. In this table, $\Delta v_{\rm CC}$ is the relative velocity determined from the CC method, $v_{\text{model}} - v_{\text{SN}}$ is the actual relative velocity derived from the calibration provided by the straight lines in Figure 9, and $v_{\rm SN}$ is the photospheric expansion velocity of the SN. Note that, for a given epoch, the expansion velocities derived from different models agree quite well. Table 6 presents the average velocity $v_{\rm CC}$ obtained for each epoch along with the rms value derived from the different models. Note the great agreement in the photospheric velocities determined from optical and IR wavelengths. While the lines used in the different spectral regions form at different depths, the CC technique yields photospheric velocities that do not depend on the wavelength region employed in the cross-correlation, which is the expected behavior for the photosphere. Inspection of Table 6 shows that the scatter in velocity yielded by multiple cross-correlations varies between 5% and 21%. The errors in the average velocities are probably smaller than the tabulated values, because we make use of various models to compute such averages.

For comparison, we include in Table 6 velocities determined from the conventional method of measuring the wavelength of weak absorption lines. Following the approach of Schmidt et al. (1994), we list velocities measured from Fe II $\lambda\lambda$ 5018 and 5169 ($v_{\rm Fe}$), and from Sc II $\lambda\lambda$ 5526 and 5658 ($v_{\rm Sc}$). We also include estimates from all metal lines except the strong calcium features ($v_{\rm lines}$). This

DISTANCE TO SN 1999em

| JD -2451000 | Model | v_{model} (km s ⁻¹) | $\Delta v_{\rm CC} \ ({\rm km~s^{-1}})$ | $v_{ m model} - v_{ m SN} \ ({ m km~s^{-1}})$ | v _{sn} (km s ⁻¹) | JD -2451000 | Model | $v_{model} \ (\mathrm{km\ s}^{-1})$ | $\Delta v_{\rm CC} \ ({\rm km~s^{-1}})$ | $v_{ m model} - v_{ m SN} \ ({ m km~s^{-1}})$ | v _{sn} (km s ⁻¹) |
|-------------|-----------------------|-----------------------------------|---|---|--|-------------|-----------------------|-------------------------------------|---|---|--|
| 481.79 | p12.10.5 | 10992 | -614 | -728 | 11720 | 500.64 | s15.40.1 | 7040 | 1834 | 2528 | 4512 |
| | p12.10.6 | 11002 | - 591 | -700 | 11702 | | s15.43.2 | 7241 | 1563 | 2154 | 5087 |
| | p12.10.9 | 11001 | -744 | -881 | 11882 | | s15.46.1 | 6453 | 1220 | 1681 | 4772 |
| | s15.12.4 | 11403 | 720 | 847 | 10556 | | s15.46.2 | 6707 | 1404 | 1935 | 4772 |
| | s15.12.5 | 11251 | 401 | 470 | 10781 | | s15.60.4 | 5215 | 318 | 436 | 4779 |
| 484.64 | p9.10.1 | 11594 | -206 | -287 | 11881 | | s25.60.1 | 4667 | 310 | 425 | 4242 |
| | p9.10.2 | 11564 | 274 | 375 | 11189 | 501.66 | p6.40.2 | 8624 | 2398 | 2827 | 5797 |
| | p9.10.3 | 11329 | 477 | 655 | 10674 | | p6.60.1 | 5409 | 200 | 233 | 5176 |
| | p9.10.4 | 11375 | - 366 | - 508 | 11883 | | p6.60.2 | 5170 | 154 | 179 | 4991 |
| | p12.10.3 | 8481 | -1656 | -2288 | 10769 | | p6.60.3 | 5384 | 464 | 545 | 4839 |
| | p12.10.5 | 10992 | -84 | -119 | 11111 | | p6.60.4 | 5263 | 293 | 343 | 4920 |
| | p12.10.8 | 10984 | 575 | 791 | 10194 | | p6.60.6 | 5409 | 185 | 215 | 5194 |
| | p12.10.11 | 10619 | 714 | 982 | 9637 | | p9.60.1 | 4709 | -13 | -18 | 4727 |
| | s15.12.1 | 11494 | 1329 | 1831 | 9663 | | s15.40.1 | 7040 | 1830 | 2156 | 4884 |
| | s15.12.2 | 11256 | 262 | 359 | 10897 | | s15.43.2 | 7241 | 1608 | 1894 | 5347 |
| | s15.12.4 | 11403 | 647 | 890 | 10513 | | s15.43.3 | 6300 | 1707 | 2011 | 4289 |
| | \$15.12.5 | 11251 | 253 | 346 | 10905 | | s15461 | 6453 | 1169 | 1376 | 5077 |
| 485.67 | p9 10 1 | 11594 | 467 | 548 | 11046 | | s15462 | 6707 | 1745 | 2056 | 4651 |
| 100.07 | $p^{9.10.1}$ | 11564 | 454 | 533 | 11031 | | s15.60.4 | 5215 | 709 | 834 | 4381 |
| | n9 10 3 | 11329 | 240 | 280 | 11049 | | s25 60 1 | 4667 | -607 | -719 | 5386 |
| | p9.10.5 | 11375 | 114 | 132 | 11243 | 510.63 | n6 40 3 | 7686 | 1860 | 2564 | 5122 |
| | p).10.4 | 11141 | 875 | 1030 | 10112 | 510.05 | p0.40.5 | 5409 | 475 | 653 | 4757 |
| | p12.10.1 | 11103 | 952 | 1120 | 0083 | | p6.60.2 | 5170 | 504 | 693 | 4/3/ |
| | p12.10.2 | 8481 | 538 | 638 | 0110 | | p0.00.2 | 5263 | 575 | 701 | 1173 |
| | p12.10.3 | 10984 | - 538 574 | -038 674 | 10310 | | p0.00.4 | 4872 | 573 | 791 | 4084 |
| | $p_{12.10.0}$ | 10934 | 696 | 806 | 10116 | | p0.00.5 | 5400 | 402 | 676 | 4004 |
| | p12.10.10 | 10922 | 645 | 758 | 0861 | | p0.00.0 | J409 1700 | 336 | 461 | 4733 |
| | s15 12 1 | 11404 | 2218 | 2614 | 9801 | | p9.00.1 | 4709 | 106 | 140 | 4240 |
| | s15.12.1 | 11494 | 1866 | 2014 | 0057 | | o15.40.1 | 7040 | - 100 | - 149 | 2075 |
| | s15.12.2 | 11230 | 2244 | 2199 | 9037 | | s15.40.1 | 6476 | 1404 | 2050 | 3973 |
| | s15.12.5 | 0500 | 100 | 2703 | 0917 | | s15.45.1 | 7241 | 1494 | 2039 | 441/ |
| 401 67 | s15.19.0 | 12652 | - 190 | - 227 | 10226 | | s15.45.2 | 6200 | 1908 | 2050 | 2045 |
| 491.07 | p0.10.1 | 12055 | 2039 | 2427 | 8620 | | s15.45.5 | 6452 | 1601 | 2333 | 3943 4210 |
| | p12.10.4 | 10004 | 2001 | 2429 | 8029 7015 | | s15.40.1 | 6707 | 1021 | 2234 | 4219 |
| | s15.19.1 | 10604 | 2431 | 2009 | 7915 | | s15.40.2 | 2429 | 1799 | 2460 | 4227 |
| | \$15.19.2 | 10044 | 2362 | 2000 | 7830 | | s15.00.1 | 5456 | -403 | - 042 | 4080 |
| | s15.19.5 | 10270 | 2449 | 2007 | 7367 | | s15.00.2 | 2452 | 803 261 | 262 | 2015 |
| | \$15.19.4 | 10273 | 2479 | 2922 | 7535 | | s15.00.5 | 5452 | -201 | - 303 | 3013 4255 |
| | s15.20.1 | 0654 | 1665 | 2965 | 7555 | | s15.00.4 | 3213 | 750 | 1022 | 4233 |
| | \$15.28.2 a15.29.4 | 9004 | 1005 | 1962 | /092 | | \$25.00.1 h10.20.1 | 400/ | / 50 | 1032 | 2022 1790 |
| | s15.20.4 | 6990 5916 | 339 | 560 | 6333 | | h10.50.1 | 3004 | -008 | - 923 | 4/09 |
| 106 67 | \$25.30.1 -15 29 1 | 2810 0429 | 4// | 2028 | 5250 | 509 76 | n10.00.1 | 2780 | -455 | - 028 | 3414 2461 |
| 496.6/ | \$15.28.1 | 9438 | 2484 | 2928 | 6510 | 528.76 | p6.40.1 | /340 | 3290 | 38/9 | 3401 |
| | \$15.28.2 | 9654 | 24/1 | 2913 | 6/41 | | p6.40.3 | /686 | 3481 | 4105 | 3581 |
| | s15.28.3 | 10230 | 2599 | 3064 | /166 | | p6.60.5 | 4872 | 1595 | 18/9 | 2993 |
| | \$15.28.5 | 91/0 | 1436 | 1691 | 14/9 | | \$15.60.1 | 5458 | 1003 | 1181 | 2257 |
| 500 CA | s25.30.1 | 5816 | 384 | 450 | 5366 | | s15.60.3 | 3452 | 837 | 985 | 2467 |
| 500.64 | p6.40.2 | 8624 | 1866 | 2572 | 6052 | | n10.30.1 | 3864 | /11 | 836 | 3028 |
| | p6.60.1 | 5409 | 236 | 323 | 5086 | 540 FC | n10.60.1 | 2786 | 140 | 162 | 2624 |
| | p6.60.2 | 5170 | 95 | 128 | 5042 | 543.76 | p6.40.1 | 7340 | 3861 | 4553 | 2787 |
| | p6.60.3 | 5384 | 101 | 136 | 5248 | | s15.60.1 | 3439 | 1430 | 1684 | 1755 |
| | p6.60.4 | 5263 | 158 | 215 | 5048 | | s15.60.3 | 3452 | 1297 | 1527 | 1925 |
| | p6.60.6 | 5409 | 253 | 346 | 5063 | | h10.30.1 | 3864 | 1472 | 1734 | 2130 |

comparison shows that $v_{\text{lines}} \sim v_{\text{Fe}} > v_{\text{Sc}}$. While v_{Fe} and v_{Sc} have low internal errors when considered individually, the average derived from multiple weak lines displays considerable scatter. This demonstrates that the technique of using a few preselected weak absorption lines has the potential to produce very different results, so that the internal precision of the Fe or Sc method must reflect the velocity scatter yielded by all lines, which is ~20%. Figure 11 shows a comparison between the velocities derived from measuring the weak metal lines and the CC method. During the first 15

days, line velocities are $\sim 20\%$ lower than the CC velocities, after which this difference becomes negligible. In our lastepoch spectrum, on the other hand, there is a hint that the velocity derived from absorption lines is higher than that obtained from the CC method, although the difference amounts to only $\sim 1 \sigma$.

3.3. The Distance to SN 1999em

In this section we use EPM to derive the distance to SN 1999em. In doing so we adopt the foreground extinction

TABLE 6EXPANSION VELOCITIES FOR SN 1999em

| JD -2451000 | $v_{ m lines}$ (km s ⁻¹) | $v_{\rm Fe}$ (km s ⁻¹) | $v_{\rm Sc}$ (km s ⁻¹) | $v_{\rm CC}$ (km s ⁻¹) |
|-------------|--------------------------------------|------------------------------------|------------------------------------|---------------------------------------|
| 481.79 | ••• | | | 11328 (611) |
| 484.64 | | | | 10776 (721) |
| 485.67 | 8067 | | | 10023 (859) |
| 491.67 | 6997 (1451) | 6739 (483) | | 7817 (1238) |
| 496.67 | 5631 (1473) | 5947 (125) | | 6652 (811) |
| 500.64 | | ••• | | 4975 (442) |
| 501.66 | 4808 (1004) | 5065 (60) | 4831 | 4976 (402) |
| 510.63 | ••• | | | 4307 (415) |
| 528.76 | 3132 (702) | 3209 (58) | 2736 (46) | 2916 (496) |
| 543.76 | 2972 (661) | 2973 (63) | 2441 (3) | 2149 (452) |

 $A_{\text{Gal}}(V) = 0.13$ measured by Schlegel et al. (1998). The presence of interstellar Na I D in the SN spectrum at the wavelength corresponding to the velocity of the host galaxy with an equivalent width of ~ 2 Å suggests that additional reddening affected the SN. According to the correlation between equivalent width and reddening of Munari & Zwitter (1997), SN 1999em was reddened by $E(B - V)_{\text{host}} \sim$ 1.0 ± 0.15 . This estimate is highly inconsistent with the independent estimate of $E(B - V)_{host} \approx 0.01 - 0.06$ and $E(B - V)_{\text{host}} < 0.11$ from theoretical modeling of the spectra of SN 1999em (Baron et al. 2000).⁹ This disagreement suggests that the light of SN 1999em was likely absorbed by a gas cloud with a relatively large gas-to-dust ratio, perhaps ejected by the supernova progenitor in an episode of mass loss. This example demonstrates the difficulty of using the equivalent width of interstellar lines to estimate dust extinction, because of the uncertainty in the calibration. Another example that illustrates the problem of

 9 That paper provides constraints to $E\,(B-V)_{\rm total},$ which includes 0.04 mag of foreground reddening.

applying the Galactic calibration of Munari & Zwitter to SNe is the highly reddened Type Ia SN 1986G. The spectra of this SN revealed interstellar Na I D absorption with an equivalent width of 4.1 Å (Phillips et al. 1987), which implies $E(B - V) \sim 2$, yet the reddening yielded by color considerations was E(B - V) = 0.62 (Phillips et al. 1999).

Below we examine the sensitivity of EPM to dust, for which we adopt a wide range of extinction values between $A_{\text{host}}(V) = 0$ and 0.45 mag. Figure 12 shows the EPM distances derived for eight filter subsets (from B through K). This plot reveals that the distance from subset $\{BV\}$ decreases from 7.4 to 6.2 Mpc when the adopted extinction increases from 0 to 0.45 mag. A similar behavior can be appreciated from filters $\{BVI\}$. From $\{VI\}$ we find that the distance changes only from 7.6 to 7.0 Mpc, i.e., EPM is very insensitive to our choice of $A_{host}(V)$ when observing with these filters. This trend reverses with subsets including the IR filters, i.e., the distance gets larger as the adopted extinction increases. This plot shows empirically that the EPM distances are quite robust to the effects of extinction. The other interesting feature of this plot is that these curves show a convergence toward small values of $A_{host}(V)$, which allows us to constrain the value of the extinction in the host galaxy. In the following discussion we adopt $A_{host}(V) =$ 0.18, which is the most likely value derived by Baron et al. (2000) and, as Figure 12 shows, is also consistent with the EPM analysis.

Tables 7–10 summarize the EPM quantities derived for SN 1999em using eight filter subsets. The photospheric velocities come from the polynomial fit to the velocities obtained from the CC technique (Fig. 11, solid line), to which we assign a statistical uncertainty of 5%. The color temperature T_s and the quantity $\theta \zeta_s$ correspond to parameters obtained from the χ^2 minimizing procedure described in § 3.1 (eq. [1]), which allows us to estimate statistical uncertainties in the derived parameters from the photometric errors. Also listed in these tables is the dilution factor ζ_s required for the derivation of the $(\theta/v)_s$ quantity needed



FIG. 11.—Expansion velocity of SN 1999em vs. Julian Day, derived from the cross-correlation technique (*filled circles*) and the minimum of the spectral absorptions (*open circles*). The solid and dashed lines represent polynomial fits to the filled and open circles, respectively.



FIG. 12.—EPM distance derived from different filter subsets, as a function of the adopted visual extinction in the host galaxy.

TABLE 7 EPM QUANTITIES DERIVED FOR SN 1999em from Subsets $\{BV\}$ and $\{VI\}$

| JD -2451000 | $v_{\rm ph} \ ({\rm km~s^{-1}})$ | $\begin{array}{c} T_{BV} \\ (\mathbf{K}) \end{array}$ | $\frac{\theta \zeta_{BV}}{(10^{11} \text{ cm Mpc}^{-1})}$ | ζ_{BV} | $(\theta/v)_{BV}$ (100 s Mpc ⁻¹) | T_{VI} (K) | $\frac{\theta \zeta_{VI}}{(10^{11} \text{ cm Mpc}^{-1})}$ | ζ_{VI} | $(\theta/v)_{VI}$ (100 s Mpc ⁻¹) |
|-------------|----------------------------------|---|---|--------------|---|--------------|---|--------------|---|
| 481.76 | 11763 | 19490 (1471) | 220 (16) | 0.431 | 433 (39) | 13392 (589) | 323 (15) | 0.453 | 606 (41) |
| 481.80 | 11741 | 18387 (1292) | 234 (17) | 0.420 | 475 (41) | 12683 (487) | 347 (14) | 0.448 | 661 (43) |
| 483.72 | 10752 | 16362 (990) | 270 (18) | 0.400 | 627 (52) | 12966 (512) | 348 (15) | 0.450 | 719 (47) |
| 483.78 | 10722 | 16087 (1613) | 278 (30) | 0.397 | 652 (77) | 14501 (1685) | 310 (38) | 0.461 | 627 (84) |
| 484.76 | 10255 | 15122 (830) | 297 (19) | 0.388 | 747 (60) | 12870 (504) | 356 (15) | 0.449 | 773 (50) |
| 485.79 | 9788 | 14524 (759) | 305 (19) | 0.383 | 813 (65) | 12683 (487) | 356 (15) | 0.448 | 811 (53) |
| 486.80 | 9354 | 14278 (730) | 309 (19) | 0.381 | 869 (69) | 11717 (408) | 391 (15) | 0.441 | 946 (60) |
| 487.76 | 8964 | 13878 (685) | 316 (19) | 0.377 | 934 (73) | 11086 (359) | 415 (16) | 0.438 | 1057 (66) |
| 488.80 | 8562 | 13064 (598) | 338 (20) | 0.372 | 1060 (82) | 10649 (328) | 437 (16) | 0.437 | 1168 (73) |
| 489.81 | 8194 | 12709 (1119) | 347 (38) | 0.370 | 1146 (139) | 10320 (709) | 454 (41) | 0.436 | 1271 (132) |
| 490.79 | 7857 | 12059 (728) | 367 (29) | 0.367 | 1271 (118) | 9766 (270) | 486 (17) | 0.436 | 1421 (87) |
| 492.79 | 7224 | 10467 (366) | 449 (24) | 0.371 | 1675 (122) | 9804 (272) | 492 (18) | 0.436 | 1563 (96) |
| 493.74 | 6949 | 9869 (322) | 490 (26) | 0.378 | 1867 (135) | 9791 (271) | 496 (18) | 0.436 | 1638 (101) |
| 495.67 | 6437 | 8659 (295) | 596 (35) | 0.410 | 2258 (174) | 9640 (360) | 506 (26) | 0.436 | 1802 (129) |
| 495.74 | 6419 | 8086 (209) | 676 (33) | 0.438 | 2401 (168) | 9882 (277) | 494 (18) | 0.436 | 1766 (109) |
| 498.65 | 5758 | 7096 (182) | 849 (45) | 0.521 | 2833 (207) | 9531 (291) | 517 (21) | 0.436 | 2059 (134) |
| 498.68 | 5752 | 7081 (159) | 844 (40) | 0.522 | 2810 (195) | 9251 (239) | 535 (19) | 0.437 | 2128 (129) |
| 498.78 | 5731 | 7385 (173) | 773 (37) | 0.491 | 2749 (191) | 9229 (237) | 533 (18) | 0.437 | 2126 (129) |
| 499.81 | 5527 | 7133 (161) | 816 (39) | 0.516 | 2859 (198) | 8948 (221) | 552 (19) | 0.439 | 2276 (138) |
| 500.70 | 5362 | 6906 (233) | 858 (60) | 0.543 | 2944 (254) | 8937 (341) | 547 (31) | 0.439 | 2321 (174) |
| 501.71 | 5187 | 6388 (128) | 1023 (48) | 0.622 | 3173 (218) | 8906 (219) | 560 (19) | 0.439 | 2456 (149) |
| 501.75 | 5180 | 6537 (135) | 967 (46) | 0.596 | 3131 (216) | 8855 (216) | 560 (19) | 0.440 | 2459 (149) |
| 502.67 | 5031 | 6486 (210) | 982 (70) | 0.605 | 3229 (281) | 8449 (391) | 604 (44) | 0.444 | 2702 (239) |
| 504.67 | 4738 | 5917 (183) | 1197 (87) | 0.720 | 3507 (310) | 8676 (259) | 578 (26) | 0.442 | 2764 (185) |
| 504.74 | 4728 | 6093 (151) | 1109 (65) | 0.680 | 3452 (265) | 8252 (185) | 621 (20) | 0.447 | 2937 (176) |
| 505.72 | 4600 | 5687 (102) | 1294 (61) | 0.781 | 3601 (247) | 8296 (187) | 614 (20) | 0.446 | 2991 (179) |
| 506.// | 4472 | 5815 (106) | 1219 (57) | 0.746 | 3652 (250) | 8065 (176) | 638 (21) | 0.450 | 3169 (189) |
| 507.80 | 4356 | 5488 (138) | 1399 (90) | 0.843 | 3811 (311) | 8090 (177) | 636 (21) | 0.450 | 3246 (194) |
| 508.82 | 4249 | 5579 (98) | 1338 (63) | 0.814 | 3870 (265) | 7983 (172) | 648 (21) (47 (21) | 0.452 | 33/1 (201) |
| 510.75 | 4148 | 5323 (95) | 1498 (74) | 0.901 | 4009 (282) | 7983 (172) | 647 (21) 680 (22) | 0.452 | 3448 (205) |
| 510./5 | 4008 | 5252 (87) | 1550 (75) | 0.928 | 4125 (282) | 7779 (102) | 080 (22) 686 (22) | 0.457 | 3037 (217) |
| 511.85 | 3970 | 5224 (80) | 1502 (75) | 0.939 | 4185 (287) | 7690 (158) | 080 (22) | 0.459 | 3700 (223) |
| 515.72 | 3635 | 3021 (80) 4770 (75) | 1/39 (81) | 1.020 | 4417 (303) | 7322 (101) | 710 (23) | 0.404 | 4036 (243) |
| 510.71 | 3/85 | 4770 (73) | 2243 (105) | 1.155 | 4/18 (327) 5043 (346) | 7363 (144) | 742 (23) 764 (24) | 0.409 | 4342 (230) |
| 522 59 | 3353 | 4449 (63) | 2243 (103) | 1.270 | 5333 (366) | 7101 (136) | 780 (24) | 0.475 | 4891 (288) |
| 522.59 | 3348 | 4338 (60) | 2555 (114) | 1.301 | 5281 (363) | 6956 (126) | 809 (25) | 0.475 | 4077 (202) |
| 527.63 | 3139 | 4360 (256) | 2562 (461) | 1.443 | 5720 (1067) | 7289 (349) | 754 (64) | 0.400 | 5095 (501) |
| 528 59 | 3098 | 4307 (82) | 2650 (163) | 1.427 | 5819 (461) | 6799 (151) | 859 (35) | 0.472 | 5617 (361) |
| 531.76 | 2956 | 4205 (57) | 2816 (133) | 1.470 | 6122 (421) | 6607 (113) | 899 (27) | 0.505 | 6023 (352) |
| 538 56 | 2584 | 3981 (53) | 3328 (162) | 1.550 | 7250 (506) | 6507 (129) | 920 (34) | 0.505 | 6962 (433) |
| 538.60 | 2587 | 3894 (85) | 3618 (286) | 1.875 | 7475 (699) | 6618 (196) | 897 (49) | 0.504 | 6895 (513) |
| 540.55 | 2451 | 3941 (71) | 3394 (216) | 1.821 | 7605 (615) | 6523 (160) | 902 (43) | 0.510 | 7216 (497) |
| 546 55 | 2176 | 3792 (47) | 3851 (183) | 1 999 | 8850 (611) | 6332 (103) | 956 (29) | 0.510 | 8392 (489) |
| 546.61 | 2176 | 3823 (54) | 3781 (200) | 1.960 | 8865 (646) | 6436 (107) | 933 (28) | 0.516 | 8311 (485) |
| 547.60 | 2172 | 3768 (53) | 3977 (211) | 2.031 | 9018 (658) | 6426 (106) | 937 (28) | 0.517 | 8347 (487) |
| 550.55 | 2159 | 3733 (75) | 4058 (299) | 2.077 | 9051 (806) | 6337 (161) | 953 (48) | 0.523 | 8437 (600) |
| 551.61 | 2154 | 3752 (46) | 3970 (189) | 2.051 | 8988 (621) | 6260 (100) | 974 (29) | 0.529 | 8547 (497) |
| 551.66 | 2154 | 3693 (45) | 4258 (203) | 2.133 | 9271 (641) | 6308 (102) | 972 (29) | 0.525 | 8589 (500) |

for EPM. In the models of E96, this factor is primarily determined by temperature and, for a given temperature, ζ_s changes only by 5%–10% over a large range of other parameters. This is a remarkable result, permitting us to compute ζ_s for SN 1999em without having to craft specific atmospheric models. Using this approximation and the derived color temperature, we compute ζ_s from the polynomial fits to the dilution factors for our photometric system (Appendix C; eq. [C2]). With this approach we expect a component of systematic error (~5%–10%) in $(\theta/v)_s$. Since this is not a statistical uncertainty, we do not include it in the error quoted for $(\theta/v)_s$ in Tables 7–10.

Figure 13 shows θ/v as a function of time for four subsets including filters *B* through *Z*. The open circles show θ/v uncorrected for dilution factors, while the filled circles show the parameter after correction. In theory, θ/v should increase linearly with time (except for the very first days after explosion), and the slope of the relation gives the distance (eq. [A4]). Overall, this figure reveals that the dilution factors produce distances with reasonable consistency during a period of 70 days of SN evolution in which the photospheric temperature dropped from 15,000 to 5000 K, although it is evident that there are systematic departures from linearity. In particular, the earliest points provide evi-

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| JD -2451000 | v _{ph} (km s ⁻¹) | <i>Т_{вv1}</i> (К) | $\frac{\theta \zeta_{BVI}}{(10^{11} \text{ cm Mpc}^{-1})}$ | ζ_{BVI} | $(\theta/v)_{BVI}$ (100 s Mpc ⁻¹) | <i>T_{VZ}</i> (K) | $\frac{\theta \zeta_{VZ}}{(10^{11} \text{ cm Mpc}^{-1})}$ | ζ_{VZ} | $(\theta/v)_{VZ}$ (100 s Mpc ⁻¹) |
|-------------|--|-------------------------------|--|---------------|--|------------------------------|---|--------------|---|
| 481.76 | 11763 | 15674 (448) | 278 (8) | 0.443 | 533 (31) | 12827 (409) | 339 (11) | 0.475 | 607 (36) |
| 481.80 | 11741 | 14707 (364) | 301 (8) | 0.435 | 589 (33) | ••• | | | ••• |
| 483.72 | 10752 | 14295 (341) | 316 (8) | 0.431 | 682 (39) | 12526 (388) | 362 (12) | 0.472 | 713 (43) |
| 483.78 | 10722 | 15434 (1071) | 291 (22) | 0.441 | 615 (55) | ••• | ••• | | ••• |
| 484.76 | 10255 | 13794 (315) | 332 (9) | 0.427 | 759 (43) | 12454 (382) | 370 (12) | 0.472 | 766 (46) |
| 485.79 | 9788 | 13451 (297) | 335 (9) | 0.424 | 807 (45) | 11335 (309) | 409 (13) | 0.462 | 904 (53) |
| 486.80 | 9354 | 12741 (263) | 358 (9) | 0.419 | 913 (51) | 11335 (309) | 407 (13) | 0.462 | 943 (55) |
| 487.76 | 8964 | 12181 (238) | 375 (9) | 0.416 | 1007 (56) | 10543 (262) | 444 (13) | 0.457 | 1084 (63) |
| 488.80 | 8562 | 11608 (213) | 397 (9) | 0.413 | 1122 (62) | 10469 (258) | 447 (13) | 0.457 | 1142 (66) |
| 489.81 | 8194 | 11386 (545) | 402 (25) | 0.412 | 1190 (96) | 10073 (297) | 470 (16) | 0.456 | 1257 (76) |
| 490.79 | 7857 | 10378 (219) | 453 (12) | 0.412 | 1398 (80) | , | | | ′ |
| 492.79 | 7224 | 10091 (156) | 475 (10) | 0.413 | 1593 (87) | | | | |
| 493.74 | 6949 | 9826 (147) | 494 (11) | 0.415 | 1714 (93) | | | | |
| 495.67 | 6437 | 9135 (192) | 543 (18) | 0.422 | 2001 (120) | | | | |
| 495.74 | 6419 | 8981 (120) | 556 (12) | 0.424 | 2041 (111) | | | | |
| 498.65 | 5758 | 8267 (127) | 626 (16) | 0.441 | 2463 (139) | | | | |
| 498.68 | 5752 | 8132 (97) | 635 (13) | 0.446 | 2476 (134) | | | | |
| 498.78 | 5731 | 8299 (101) | 612 (12) | 0.440 | 2427 (131) | | | | |
| 499.81 | 5527 | 8033 (94) | 638 (13) | 0.449 | 2572 (139) | | | | |
| 500.70 | 5362 | 7919 (171) | 652 (24) | 0.453 | 2680 (167) | | | | |
| 501.71 | 5187 | 7572 (83) | 700 (14) | 0.469 | 2876 (155) | | | | |
| 501.75 | 5180 | 7644 (85) | 686 (14) | 0.466 | 2843 (153) | 8088 (144) | 650 (17) | 0.473 | 2654 (149) |
| 502.67 | 5031 | 7288 (173) | 766 (35) | 0.485 | 3136 (212) | 0000 (111) | | 00 | 2001 (115) |
| 504.67 | 4738 | 7527 (141) | 713 (23) | 0.472 | 3191 (191) | | | | |
| 504.74 | 4728 | 7340 (95) | 734 (17) | 0.482 | 3222 (177) | ••• | ••• | | |
| 505.72 | 4600 | 6897 (68) | 805 (16) | 0.513 | 3411(183) | ••• | | | |
| 506.77 | 4000 | 6889 (68) | 807 (16) | 0.515 | 3510 (188) | 7587 (125) | 710 (18) | 0.487 | 3259 (183) |
| 507.80 | 4356 | 7063 (94) | 777 (18) | 0.501 | 3562 (197) | (125) | /10 (10) | 0.107 | 5255 (105) |
| 508.82 | 4249 | 6710 (64) | 841 (16) | 0.501 | 3738 (200) | 7409 (119) | 739 (18) | 0.495 | 3519 (197) |
| 500.02 | 4148 | 6609 (66) | 861 (17) | 0.530 | 3848 (207) | 7354 (117) | 749 (19) | 0.497 | 3632 (203) |
| 510.75 | 4068 | 6426 (58) | 914 (17) | 0.540 | 4018 (215) | 7554 (117) | (1) | 0.477 | 5052 (205) |
| 511.85 | 3976 | 6376 (57) | 920 (17) | 0.565 | 4018 (219) | ••• | ••• | ••• | ••• |
| 513.72 | 3835 | 6130 (57) | 1004 (21) | 0.505 | 4386 (237) | ••• | ••• | ••• | ••• |
| 516.71 | 3645 | 5992 (52) | 1040 (21) | 0.577 | 4626 (248) | ••• | ••• | ••• | ••• |
| 519.72 | 3485 | 5791 (47) | 1114 (21) | 0.650 | 4915 (262) | | | ••• | ••• |
| 522 59 | 3353 | 5684 (45) | 1160 (22) | 0.050 | 5161 (275) | ••• | ••• | ••• | ••• |
| 522.59 | 3348 | 5528 (43) | 1205 (22) | 0.070 | 5127 (273) | ••• | ••• | ••• | ••• |
| 527.63 | 3130 | 6360 (221) | 961 (68) | 0.702 | 5401 (468) | ••• | ••• | ••• | ••• |
| 528 59 | 3098 | 5567 (67) | 1245 (35) | 0.507 | 5703 (333) | ••• | ••• | ••• | ••• |
| 531.76 | 2956 | 5316 (39) | 1329 (25) | 0.094 | 5984 (319) | ••• | ••• | | ••• |
| 538 56 | 2584 | 5030 (42) | 1529 (25) | 0.731 | 7064 (388) | 6347 (85) | | 0.565 | 6632 (367) |
| 538.50 | 2582 | 5134 (72) | 1319 (33) | 0.032 | 7004 (388) | 0347 (83) | 909 (23) | 0.505 | 0032 (307) |
| 540 55 | 2362 | 5134 (73) | 1408 (34) | 0.801 | 7101 (441) | ··· 6272 (82) | | 0.572 | 6077 (286) |
| 546.55 | 2431 | J120 (04) | 14/3 (40) | 0.000 | 1417 (440) 8168 (425) | 6280 (82) | 979 (23) 072 (22) | 0.575 | 7810 (422) |
| 546.55 | 21/0 2176 | 4741 (34) 5122 (41) | 1330 (28) | 0.001 | 0100 (433) | 0200 (83) | 913 (23) | 0.372 | 1019 (432) |
| 547.60 | 21/0 | 5022 (41) | 1424 (28) | 0.004 | 0137 (438) | ••• | ••• | ••• | ••• |
| 550 55 | 21/2 | 5002 (60) | 1448 (29) | 0.810 | 81/0 (44U) 8580 (520) | ··· | | | |
| 550.55 | 2139 | 5002 (69) 4800 (22) | 1559 (50) | 0.841 | 8363 (330) | 0249 (84) | 982 (24) | 0.375 | 1907 (439) |
| 551.01 | 2154 | 4890 (33) | 1503 (29) | 0.8/8 | 8262 (440) | ••• | ••• | ••• | ••• |
| 551.66 | 2154 | 4864 (33) | 1597 (29) | 0.887 | 8359 (445) | ••• | ••• | ••• | ••• |

dence that the angular radius is too large relative to the physical size implied by homologous expansion of the photosphere from a point. This suggests that the progenitor's radius (R_0) might have a nonnegligible contribution to the SN radius in the first observations (obtained a few days after shock breakout). A week after explosion R_0 becomes negligible, even for the largest red supergiants known $(R_0 = 300 R_{\odot}; \text{ van Belle et al. 1999})$, so its effect in the determination of the distance can be ignored. Hence, we now proceed to fit the data with a straight line using equation (A4), and in the next section we review the validity of this approximation.

To compute the distance it suffices, in principle, to perform a least-squares fit to the $(\theta_i/v_i, t_i)$ points. To perform such a fit it is necessary to know the uncertainty in each of the θ_i/v_i points. In our case this is rendered difficult by our lack of knowledge of the systematic errors in ζ_s , which is needed to obtain the θ/v parameter. By weighting the fits by the errors, the fits are going to be biased significantly to the earlier data, which carry a lot of weight. Equal weighting seems to be a more reasonable way to derive an "average" distance. To estimate the uncertainties in the distance and explosion time, we employ the bootstrap technique described by Press et al. (1992), which makes use of

TABLE 9 EPM Quantities Derived for SN 1999em from Subsets $\{VJ\}$ and $\{VH\}$

| JD -2451000 | v_{ph} (km s ⁻¹) | <i>Т_{VJ}</i> (К) | $\frac{\theta \zeta_{VJ}}{(10^{11} \text{cm Mpc}^{-1})}$ | ζ_{VJ} | $(\theta/v)_{VJ}$ (100 s Mpc ⁻¹) | <i>Т_{VH}</i> (К) | $\frac{\theta \zeta_{VH}}{(10^{11} \text{cm Mpc}^{-1})}$ | ζ_{VH} | $\frac{(\theta/v)_{VH}}{(100 \text{ s Mpc}^{-1})}$ |
|-------------|-----------------------------------|------------------------------|--|--------------|---|------------------------------|--|--------------|--|
| 481.80 | 11741 | 13207 (318) | 331 (8) | 0.586 | 481 (27) | 11318 (192) | 400 (7) | 0.590 | 578 (31) |
| 482.69 | 11271 | 10963 (348) | 421 (17) | 0.581 | 643 (41) | 10338 (178) | 456 (9) | 0.583 | 693 (37) |
| 483.76 | 10732 | 10993 (210) | 427 (9) | 0.581 | 685 (37) | 10541 (163) | 452 (8) | 0.585 | 720 (38) |
| 483.78 | 10722 | 12596 (342) | 364 (10) | 0.585 | 581 (33) | 9923 (207) | 498 (13) | 0.581 | 800 (45) |
| 484.76 | 10255 | 11310 (224) | 418 (9) | 0.582 | 700 (38) | 10706 (169) | 449 (8) | 0.586 | 748 (40) |
| 485.73 | 9815 | 10714 (488) | 440 (26) | 0.580 | 773 (60) | 10279 (284) | 466 (17) | 0.583 | 815 (50) |
| 486.77 | 9367 | 10218 (178) | 469 (9) | 0.579 | 864 (47) | 9909 (142) | 489 (8) | 0.580 | 900 (47) |
| 487.75 | 8968 | 10102 (173) | 471 (9) | 0.578 | 909 (49) | 9836 (140) | 490 (8) | 0.580 | 942 (50) |
| 488.76 | 8577 | 9645 (156) | 502 (10) | 0.577 | 1015 (54) | 9525 (130) | 511 (8) | 0.577 | 1033 (54) |
| 489.81 | 8194 | 9464 (188) | 514 (11) | 0.576 | 1089 (59) | 9304 (155) | 527 (9) | 0.576 | 1118 (59) |
| 495.74 | 6419 | 9211 (141) | 548 (10) | 0.575 | 1483 (79) | 9206 (120) | 548 (9) | 0.575 | 1486 (78) |
| 498.68 | 5752 | 9305 (240) | 531 (19) | 0.576 | 1602 (99) | 9252 (245) | 535 (21) | 0.575 | 1618 (102) |
| 501.71 | 5187 | 7668 (93) | 719 (13) | 0.568 | 2438 (129) | 8324 (96) | 624 (9) | 0.566 | 2125 (111) |
| 504.74 | 4728 | 8530 (118) | 588 (11) | 0.572 | 2172 (116) | 7983 (87) | 657 (10) | 0.562 | 2469 (129) |
| 505.72 | 4600 | 7943 (101) | 661 (12) | 0.570 | 2524 (134) | 7646 (79) | 707 (10) | 0.558 | 2752 (143) |
| 507.80 | 4356 | 7775 (96) | 681 (12) | 0.569 | 2751 (146) | 7834 (129) | 673 (18) | 0.561 | 2754 (156) |
| 510.75 | 4068 | 7744 (95) | 685 (12) | 0.569 | 2962 (157) | 7653 (79) | 699 (10) | 0.558 | 3079 (160) |
| 513.72 | 3835 | 7418 (89) | 737 (13) | 0.567 | 3389 (180) | 7475 (119) | 727 (19) | 0.556 | 3406 (193) |
| 516.71 | 3645 | 6643 (68) | 906 (15) | 0.562 | 4428 (233) | 6953 (64) | 828 (12) | 0.549 | 4140 (215) |
| 519.72 | 3485 | 6980 (76) | 823 (14) | 0.564 | 4189 (221) | 7067 (71) | 804 (13) | 0.550 | 4190 (219) |
| 522.59 | 3353 | 7056 (77) | 808 (14) | 0.565 | 4271 (225) | 6885 (63) | 848 (12) | 0.548 | 4616 (239) |
| 527.63 | 3139 | 6804 (95) | 861 (17) | 0.563 | 4874 (261) | 6809 (82) | 860 (13) | 0.547 | 5011 (262) |
| 528.59 | 3098 | 6793 (71) | 860 (14) | 0.563 | 4935 (260) | 6740 (60) | 874 (12) | 0.545 | 5172 (268) |
| 538.60 | 2582 | 6549 (80) | 917 (16) | 0.561 | 6329 (336) | 6557 (68) | 914 (13) | 0.542 | 6529 (340) |
| 546.61 | 2176 | 6375 (62) | 952 (15) | 0.560 | 7818 (411) | 6352 (52) | 959 (13) | 0.539 | 8182 (424) |
| 547.60 | 2172 | 6286 (60) | 981 (16) | 0.559 | 8084 (425) | 6399 (53) | 945 (13) | 0.540 | 8063 (417) |
| 551.66 | 2154 | 6491 (64) | 916 (15) | 0.561 | 7585 (399) | 6463 (55) | 924 (12) | 0.541 | 7933 (411) |

 $\label{eq:table_to_table_to_table} TABLE \ 10$ EPM Quantities Derived for SN 1999em from Subsets $\{VK\}$ and $\{JHK\}$

| JD -2451000 | v_{ph} (km s ⁻¹) | <i>Т_{VK}</i> (К) | $\frac{\theta \zeta_{VK}}{(10^{11} \text{cm Mpc}^{-1})}$ | ζ_{VK} | $(\theta/v)_{VK}$ (100 s Mpc ⁻¹) | <i>Т_{JHK}</i> (К) | $\frac{\theta \zeta_{JHK}}{(10^{11} \text{ cm Mpc}^{-1})}$ | ζ _{JHK} | $\frac{(\theta/v)_{JHK}}{(100 \text{ s Mpc}^{-1})}$ |
|-------------|-----------------------------------|------------------------------|--|--------------|---|-------------------------------|--|------------------|---|
| 481.80 | 11741 | 9944 (130) | 477 (7) | 0.698 | 583 (30) | 5640 (164) | 727 (22) | 0.628 | 987 (57) |
| 482.69 | 11271 | 9165 (209) | 543 (18) | 0.673 | 716 (43) | 6337 (484) | 693 (50) | 0.721 | 852 (75) |
| 483.76 | 10732 | 9451 (116) | 528 (8) | 0.682 | 722 (38) | 6574 (232) | 681 (22) | 0.749 | 848 (51) |
| 483.78 | 10722 | 8970 (166) | 579 (15) | 0.667 | 810 (45) | 4732 (167) | 970 (41) | 0.465 | 1947 (128) |
| 484.76 | 10255 | 9607 (142) | 523 (10) | 0.687 | 743 (40) | 6736 (278) | 666 (26) | 0.766 | 848 (54) |
| 485.73 | 9815 | 9642 (405) | 511 (31) | 0.688 | 757 (59) | 7532 (1186) | 601 (83) | 0.842 | 728 (107) |
| 486.77 | 9367 | 9079 (106) | 557 (8) | 0.670 | 888 (46) | 6716 (244) | 689 (23) | 0.764 | 962 (58) |
| 487.75 | 8968 | 9014 (105) | 558 (8) | 0.668 | 932 (48) | 6731 (245) | 684 (23) | 0.766 | 996 (60) |
| 488.76 | 8577 | 8850 (107) | 572 (9) | 0.663 | 1006 (53) | 7118 (294) | 662 (25) | 0.805 | 959 (60) |
| 489.81 | 8194 | 8563 (117) | 601 (9) | 0.654 | 1121 (58) | 6592 (234) | 721 (24) | 0.751 | 1172 (70) |
| 495.74 | 6419 | 9094 (130) | 559 (10) | 0.670 | 1298 (69) | 8814 (520) | 569 (28) | 0.934 | 949 (66) |
| 498.68 | 5752 | 8276 (147) | 639 (18) | 0.645 | 1722 (98) | 6160 (435) | 789 (54) | 0.700 | 1960 (166) |
| 501.71 | 5187 | 7705 (81) | 712 (11) | 0.629 | 2184 (114) | 8580 (458) | 635 (28) | 0.919 | 1332 (89) |
| 504.74 | 4728 | 7520 (74) | 730 (10) | 0.624 | 2472 (129) | 5447 (160) | 939 (29) | 0.598 | 3323 (195) |
| 505.72 | 4600 | 7379 (81) | 754 (13) | 0.621 | 2640 (140) | 6020 (220) | 880 (32) | 0.682 | 2807 (174) |
| 507.80 | 4356 | 7298 (106) | 764 (19) | 0.619 | 2834 (158) | 6417 (329) | 827 (43) | 0.731 | 2597 (188) |
| 510.75 | 4068 | 7388 (132) | 746 (23) | 0.621 | 2951 (174) | 6825 (363) | 776 (40) | 0.776 | 2461 (176) |
| 513.72 | 3835 | 7024 (87) | 816 (17) | 0.614 | 3468 (189) | 6177 (286) | 890 (42) | 0.702 | 3306 (228) |
| 516.71 | 3645 | 6809 (56) | 863 (11) | 0.610 | 3879 (200) | 7613 (323) | 782 (29) | 0.848 | 2529 (157) |
| 519.72 | 3485 | 6495 (50) | 951 (11) | 0.607 | 4495 (231) | 5356 (146) | 1093 (31) | 0.583 | 5384 (311) |
| 522.59 | 3353 | 6815 (68) | 865 (14) | 0.610 | 4228 (223) | 6077 (225) | 949 (35) | 0.689 | 4109 (256) |
| 527.63 | 3139 | 6439 (67) | 963 (13) | 0.607 | 5056 (262) | 5555 (163) | 1069 (32) | 0.615 | 5539 (324) |
| 528.59 | 3098 | 6469 (53) | 950 (13) | 0.607 | 5054 (262) | 5659 (175) | 1047 (33) | 0.631 | 5360 (317) |
| 538.60 | 2582 | 6127 (54) | 1055 (13) | 0.607 | 6733 (347) | 5116 (132) | 1206 (34) | 0.541 | 8636 (494) |
| 546.61 | 2176 | 6261 (64) | 989 (19) | 0.606 | 7495 (401) | 6004 (235) | 1016 (40) | 0.679 | 6871 (439) |
| 547.60 | 2172 | 6240 (49) | 997 (13) | 0.606 | 7570 (392) | 6207 (215) | 988 (33) | 0.706 | 6451 (389) |
| 551.66 | 2154 | 6339 (48) | 962 (12) | 0.606 | 7368 (379) | 5892 (181) | 1016 (31) | 0.664 | 7104 (416) |



FIG. 13.— θ/v as a function of time for filter subsets {BV, VI, VZ, BVI}. Open circles show θ/v uncorrected for dilution factor, while filled circles show the parameter corrected with the factors computed by E96. In theory, this quantity should increase linearly with time, and the slope of the relation gives the distance (Appendix A). The small departures of these points from the ridge lines demonstrate the good performance of the dilution factors at different times over a broad wavelength range.

the data themselves as an estimator of the underlying probability distribution (which we do not know). The method consists of randomly drawing from the parent population a synthetic data set of the same size as the parent. By drawing points with replacement, we end up with a randomly modified data set, from which we perform a uniform-weight least-squares fit in order to solve for the time of explosion, t_0 , and the distance, D. From a large number (10,000) of simulations, we obtain average parameters and estimates of the uncertainties in t_0 and D from the dispersion among the many bootstrap realizations.

The ridge lines in Figure 13 correspond to the solutions determined from the bootstrap method, and the results of the fits are given in Table 11. The range in distance (6.9–7.8 Mpc) derived from observing through these four filter subsets is quite small ($\pm 6\%$). This shows the good performance of the dilution over the broad wavelength range encompassed by the *BVIZ* filters. The nominal error yielded by the bootstrap method for the individual subsets ranges between 1% and 2%, which proves significantly smaller than the 6% distance range encompassed by the

four subsets. Most likely, this is a symptom of systematic errors in the dilution factors.

Figure 14 shows θ/v as a function of time from filter subsets including IR wavelengths. The scatter from the ridge line is somewhat higher than that obtained from

 TABLE 11

 Distance and Explosion Time for SN 1999em

| Filter Subset | D (Mpc) | t ₀ (JD – 2451000) | | |
|-------------------|-----------------|----------------------------------|--|--|
| $\{BV\}$ | 6.91 ± 0.09 | 478.3 ± 0.4 | | |
| $\{BVI\}$ | 7.40 ± 0.08 | 477.9 ± 0.3 | | |
| $\{VI\}$ | 7.31 ± 0.10 | 479.6 ± 0.4 | | |
| { <i>VZ</i> } | 7.79 ± 0.10 | 477.6 ± 0.3 | | |
| { <i>VJ</i> } | 8.01 ± 0.29 | 479.9 ± 0.8 | | |
| { <i>VH</i> } | 7.82 ± 0.28 | 479.8 ± 0.9 | | |
| { <i>VK</i> } | 8.22 ± 0.23 | 479.1 ± 0.8 | | |
| {JHK} | 8.56 ± 0.69 | 477.5 ± 2.1 | | |
| All 8 | 7.54 ± 0.08 | 478.8 ± 0.5 | | |
| $\{BVIJHK\}\dots$ | 7.82 ± 0.15 | 478.9 ± 0.5 | | |



FIG. 14.—Same as Fig. 13, but for filter subsets $\{VJ, VH, VK, JHK\}$

optical wavelengths, because of the relatively larger photometric errors in the IR. This problem becomes even stronger for the $\{JHK\}$ subset, because the errors in the derived color temperatures increase as the Rayleigh-Jeans limit is approached. Despite the larger scatter in the distances derived from IR observations, this plot confirms the internal consistency of the dilution factors computed by E96 from IR wavelengths. The fits to the data are listed in Table 11, which shows that the resulting distances are quite consistent with those derived from optical observations, although the differences are somewhat larger than the formal errors (more below).

We also include in Table 11 a solution derived from a simultaneous least-squares fit to all the $(\theta/v)_S$ values in Tables 7–10. Not surprisingly, the resulting distance of 7.54 Mpc is close to the value of 7.75 Mpc obtained from taking a straight average of the eight individual distances. We prefer the former estimate because it weighs the distances of the individual subsets according to their time sampling of the $(\theta/v)_S$ parameter. Also given in Table 11 is the distance of 7.82 Mpc determined from subset $\{BVIJHK\}$. In this case we must restrict the sample of $(\theta/v)_{BVIJHK}$ values to those epochs in which we obtained simultaneous observations with all six filters. Thus, the solution is not weighted

by the higher frequency of the optical observations, so the result is very close to the value of 7.75 Mpc obtained by averaging the individual distances yielded by the eight subsets. Below we adopt the value of 7.54 Mpc, which takes into account the better sampling of the optical light curves.

The values derived for the explosion time are listed in Table 11. The average from the eight filter subsets is JD 2451478.8 (± 1 day). This confirms that the SN was caught at a very young stage and that our first photometric and spectroscopic observation was obtained at an age of only 3 days after shock breakout. This is far earlier than any other SN, except for SN 1987A.

4. DISCUSSION

One of the challenges of EPM involves the determination of photospheric velocities. The spectra of SN 1999em show that the technique of cross-correlating the SN spectra with the models of E96 can produce expansion velocities with an average uncertainty of 11%. This is significantly lower than the 20% precision yielded by the method of measuring velocities from the minimum of weak absorption features (Table 6). The cross-correlation technique is not only more precise, but also more accurate, since the velocity derived from individual lines tend to correspond to the value of the thermalization surface, which expands more slowly than the photosphere (the last scattering surface). A clear advantage of the CC method is that it can be used during the initial hot phases of SN evolution when no weak lines are available. The other advantage of the CC technique is that it permits one to estimate velocities from lower S/N spectra, thus extending the potential of EPM to high redshifts, where high-quality spectra are difficult to obtain.

The effects of dust extinction can seriously hamper the determination of distances when using "standard candle" techniques. EPM, on the other hand, is quite robust to the effects of dust absorption, as pointed out by E96 and by Schmidt et al. (1992, 1994). While extinction reduces the observed flux, it also makes the photosphere appear cooler and hence less luminous, so that these two effects cancel to a significant degree. The data of SN 1999em provide empirical confirmation that the EPM distance to this SN is not very sensitive to the adopted absorption. We find that while the EPM distances derived from optical colors decrease with increasing $A_{host}(V)$, this trend reverses when using IR filters (Fig. 12). This analysis reveals that, even though IR photometry is less affected by dust, the EPM distances derived from filter subsets including one or more IR filters are not less sensitive to dust than those determined from optical filters alone. This result challenges the suggestion of Schmidt et al. (1992), namely, that one of the advantages of using IR for EPM is that "the uncertainty in a distance due to extinction is less than half that incurred when optical photometry is used." Our analysis shows that the $\{VI\}$ and $\{VZ\}$ subsets have the least sensitivity to the effects of dust. In particular, the distances derived with the $\{VI\}$ filters vary by a mere 7% when the adopted absorption is varied in a wide range of values between 0 and 0.45 mag. The other interesting result is that, despite the weak sensitivity of EPM to dust, multicolor observations can be useful for constraining $A_{host}(V)$.

EPM has the great advantage that observations at different epochs are essentially independent distance measurements. The exceptional data obtained for SN 1999em afford a unique opportunity to perform this valuable internal check and test the dilution factors of E96 over a wide range in temperature and wavelength. Figures 15 and 16 show that the EPM distance (in units of the average value of 7.54 Mpc obtained from the eight filter subsets) varies systematically over time (the error of one point is highly correlated to the error in the next point). This problem is particularly pronounced over the first week since explosion (JD 2451478.8), in which the distances prove even 50% lower than the average owing to the large photometric angular radius relative to the physical size of the SN. There are different possible causes for this discrepancy, which we proceed to examine. The high degree of correlation in the errors derived from the different filter subsets suggests that the small linear radius might be due to an underestimate of the photospheric velocity. If this was the case, the expansion velocity in the first observation epoch (JD 2451481.79) would have to be 50% higher than the adopted value. This is well beyond the $\sim 5\%$ uncertainty in the CC technique, so we can rule out errors in the photospheric velocities as the source of this discrepancy. Another possible cause for the large initial distance residuals is the neglect of the initial radius R_0 in the linear size of the SN. To examine this issue in detail, Figure 17 shows how θ/v changes with time in a log-log scale, for the eight filter subsets. Overplotted are the



FIG. 15.—EPM distance as a function of time, for filter subsets $\{BV, VI, VZ, BVI\}$.

lines corresponding to homologous expansion (eq. [A3]) for the case of a progenitor with $R_0 = 0$ (solid line) and $R_0 = 5 \times 10^{13}$ cm (dotted line), which is 2 times larger than the largest supergiant known (van Belle et al. 1999). It is evident that the two models are almost identical at later times (when the effects of R_0 in the SN radius become negligible), and that they both fit the data very well after day 7. The earliest points, on the other hand, all fall on the high side of the lines of homologous expansion. This plot shows that, while the initial radius of the SN progenitor can account for some of the high θ/v values observed at the earliest epochs, there must be other reasons to explain the relatively large



FIG. 17.— θ/v as a function of time since explosion (JD 2451478.8) for filter subsets $\{BV, VI, VZ, BVI, VJ, VH, VK, JHK\}$. The solid line shows the regression line for $R_0 = 0$, the dotted line corresponds to the fit obtained with $R_0 = 5 \times 10^{13}$ cm (714 R_{\odot}), and the dashed line is for $R_0 = 10^{14}$ cm.

angular size of the SN. We cannot rule out, of course, that the large initial residuals are due to incorrect dilution corrections, which would act to increase the derived values of θ . For this to be true, the dilution corrections for all filter subsets should be increased by 2 times. It is conceivable that such an error could be caused by circumstellar material which could lead to the formation of the photosphere at a much larger radius (Bartunov & Blinnikov 1992; Pooley 2001). This is an interesting possibility that could be clarified with an expanded set of atmosphere models for SNe II.

Leaving aside the origin of the high initial distance residuals, it is interesting to ask what their effect is in the derived distance to SN 1999em. For this purpose we employ equation (A3) to solve simultaneously for R_0 , t_0 , and D. A least-squares fit to the data, however, yields a degenerate and nonphysical solution for the three parameters, most likely caused by the large residuals of the earliest points, which demand an extremely large R_0 . If, instead, we fix R_0 to the value of a very large progenitor, 5×10^{13} cm, we obtain a modest increase of 4% in the distance. Alternatively, we now ask what would be the distance if we exclude the first observations. Limiting the data set to epochs later than JD 2451485.7 (1 week after explosion), a linear fit yields $D = 7.40 \pm 0.09$ Mpc and $t_0 = 2451479.7 \pm 0.5$, which are indistinguishable from the values derived from the entire data set.

After day 7 (JD 2451485), the scatter in the EPM distances is much lower: 9% in $\{BV\}$, 4% in $\{BVI\}$, 4% in $\{VI\}$, and 4% in $\{VZ\}$. Inspection of Figure 15 shows that the residuals vary systematically over time. If these were caused by the adopted velocity, the effect would be the same in the different filter subsets, which is not the case. We believe, instead, that the problem lies in the derived photospheric angular radii. In fact, Figure 7 reveals discrepancies of up to 10% in the values of θ obtained from different filter subsets. It could well be that these residuals are caused by the use of average dilution factors which, according to E96, have errors of between 5% and 10%. Systematic errors in the photometry could also explain the discrepancies in θ . Although the nominal uncertainties due to photon statistics are ~ 0.015 mag, the transformation of instrumental magnitudes to the standard system could have significant systematic errors owing to the nonstellar nature of the SN spectrum (Hamuy et al. 1990). In the IR, the rms in the EPM distances after day 7 are 10% in $\{VJ\}$, 10% in $\{VH\}$, 9% in $\{VK\}$, and 27% in $\{JHK\}$. In theses cases the observational uncertainties are partially responsible for these relatively greater spreads, although it is evident that the EPM distances are systematically higher than the average and that they decrease steadily with time. We believe that this trend could be caused by systematic errors in the dilution factors or the photometry.

The distance residuals shown in Figures 15 and 16 reveal the potential problem of applying EPM to SNe II with small time baseline light curves. To illustrate this point, we compute distances for SN 1999em using the data subset comprising the first days of SN evolution (up to JD 2451490), which yields D(BV) = 10.34, D(VI) = 9.70, D(BVI) = 10.24, D(VZ) = 9.95, D(VJ) = 13.26, D(VH) =13.98, D(VK) = 14.46, and D(JHK) = 20.78 Mpc. Note that these distances are much higher than the 7.54 Mpc average value, whereas Figures 15 and 16 show that the EPM distances in the first week are on the low side of the average. This difference turns out to be a consequence of the shallower slope displayed by the early-time points in Figures 13 and 14. A shallower slope implies a greater distance (eq. [A4]), despite the fact that the individual points imply smaller distances because of their relatively larger photospheric angular radii. This test reveals that a snapshot" distance based only on a small time baseline light curve is clearly inappropriate. Poorly sampled light curves, on the other hand, do not seem to be a problem. We checked this by randomly drawing three data points from the $\{VI\}$ data set. From 100 realizations, the computed distances fall within 10% of the distance derived from the entire data set (on average). For five data points, the distribution of distances has an rms of 6% around the mean, while for 10 points the rms drops to only 4%. This implies that poorly sampled light curves can yield precise distances, as long as the spacing in time is reasonable.

Schmidt et al. (1992) made the claim that one of the advantages of using IR photometry for EPM is that the JHK bands have fewer spectral features (which can be checked in Fig. 5), making it easier to derive a color temperature from broadband photometry. They also pointed out also that, despite the advantage of there being many fewer lines in the IR, measuring the color temperature from IR photometry is more difficult than in the optical since the spectrum is close to the Rayleigh-Jeans limit. This could be particularly severe if the IR photometry has lower precision than that at optical bands. Our IR data confirm this concern, i.e., the angular radii derived from filters JHK have substantially higher scatter, leading thus to a much less (5 times less) precise distance estimate than that obtained from optical wavelengths. Filter subsets involving a combination of one IR filter and one optical filter do not suffer from the proximity to the Rayleigh-Jeans limit, yet the EPM distances have precisions that are 2 times lower than those including optical filters alone. This lower precision is a symptom of the larger IR photometric errors.

Unfortunately, most of the IR photometry of SN 1999em was obtained with the YALO/ANDICAM, camera which suffered from significant vignetting that introduced illumination variations $\sim 50\%$ in all the images (N. B. Suntzeff et al., in preparation). This made it necessary to apply large photometric corrections to the SN and the field standards. Considering these problems, it is not surprising that the internal precision of EPM appears lower from subsets $\{VJ,$ VH, VK, yet it is encouraging that the IR results are consistent with those obtained from optical wavelengths. For a better assessment of the performance of the dilution factors in the IR, it will be necessary to obtain data with smaller observational errors. It is worth mentioning that the initial points (up to JD 2451490) obtained with the LCO 1 m IR camera show a much smaller spread, comparable to optical photometry (1%-2%), which demonstrates the potential precision that can be reached with IR photometry. Our guess is that, for a data set obtained under normal circumstances, $\{VK\}$ would work the best because the errors in temperature are very small for a given level of photometric errors (see Fig. 21).

Table 11 shows that the distances yielded by subsets $\{BV,$ VI, BVI, VZ, VJ, VH, VK, JHK from the first 70 days of SN evolution lie between 6.9 and 8.6 Mpc. The lowest value corresponds to that yielded by subset $\{BV\}$, which disagrees from the rest if we consider the formal uncertainty of 1%-2% yielded by the bootstrap method. As discussed above, these discrepancies are possibly caused by errors in the dilution corrections. They could be due to metallicity effects, which are expected to be relatively stronger in the B band due to line blanketing at these wavelengths. It could well be that the metallicity of SN 1999em was lower than the solar value adopted by E96 (as suggested by Baron et al. 2000), thus increasing its B-band observed flux relative to the models and making the distance to appear lower. The largest value in Table 11 is due to $\{JHK\}$, which has a substantial uncertainty of 8% associated with it, mainly because of the lower precision in the YALO IR data and the proximity to the Rayleigh-Jeans limit. The distances derived from $\{VJ, VH, VK\}$ appear 9% higher (1-3 σ) than those derived from optical wavelengths. We investigate two possible causes for this systematic effect. First, since most of our IR data come from the YALO telescope, whereas the adopted filter functions for the EPM analysis correspond to those used with the LCO IR camera (Appendix B), we repeat here the EPM calculations using the YALO JHK filter tracings. We obtain D(VJ) = 8.27, D(VH) = 7.77, D(VK) = 8.22, and D(JHK) = 7.72 Mpc, which prove insignificantly different from the values listed in Table 11. Second, since the EPM distances shown in Figures 15 and 16 change over time, we now examine the possibility that the optical distances might differ from those derived from $\{VJ, VH, VK\}$ because of the different sampling of the SN evolution. By restricting the optical sample to a subset with the same time sampling as the IR observations, we get D(BV) = 6.81, D(BVI) = 7.39, and D(VI) = 7.44 Mpc, which are negligibly different from the solutions obtained from the entire optical data set. These two tests confirm the existence of a systematic difference between optical and IR distances. It will be interesting to investigate whether or not these discrepancies persist from other SNe II with better IR data.

Altogether, Table 11 shows that the internal precision in the average distance must lie between a minimum of 2% (the formal statistical error from an individual filter subset) and a maximum of 7% (the actual scatter obtained from the eight subsets). Adopting the average solution yielded by the eight filter subsets, our best estimate for the distance to SN 1999em is $D_{1999em} = 7.5 \pm 0.5$ Mpc.

We cannot rule out systematic errors beyond this estimate. Leonard et al. (2001) has recently done a detailed multiepoch spectropolarimetric study of SN 1999em that suggests a minimum asphericity of $\sim 7\%$ during the plateau phase. Their lower limit could overestimate the distance by 7% for an edge-on view, or lead to an underestimate of 4%for a face-on line of sight. From a lower limit, it proves difficult to ascertain the actual effect on our distance estimate. It is reassuring, on the other hand, to see the good agreement between EPM, Tully-Fisher, and Cepheid distances found from a sample of 11 galaxies (Schmidt et al. 1994), which suggests that the asphericity factor is probably small among SNe II-P. This conclusion is further supported by Leonard et al. (2001), who used the distance residuals in the SN II Hubble diagram derived by Schmidt et al. to estimate an average asphericity for SNe II-P of only 10%. This value will be constrained even more as the Hubble diagram is populated with well-measured EPM distances.

One possibility for testing the overall accuracy is to compare our EPM distance to other methods. There is a distance estimate to NGC 1637 of $7.8^{+1.0}_{-0.9}$ Mpc based on the brightness of red supergiants (Sohn & Davidge 1998), which compares with our EPM distance of $D_{1999em} = 7.5 \pm 0.5$ Mpc. This galaxy is part of the 21 cm H I line profile catalog of Haynes et al. (1998), which lists a velocity width of 180.2 ± 1.7 km s⁻¹ that can be used to derive a Tully-Fisher distance. Giovanelli (2001, private communication) points out that NGC 1637 has an I-band extinctioncorrected magnitude of 9.37 and an axial ratio of 1.62, which leads to an inclination-corrected velocity width of log $W = 2.33 \pm 0.41$. The application of the Tully-Fisher template relation derived by Giovanelli et al. (1997) yields a cosmic microwave background (CMB) recession velocity of 669 ± 116 km s⁻¹ for NGC 1637, which, when combined with the Cepheid-based value of $H_0 = 69 \pm 5$ km s⁻¹ Mpc^{-1} derived by the same authors, leads to a distance of 9.7 ± 1.7 Mpc. This value is somewhat larger than that derived from our EPM analysis, but it must be kept in mind that the H I velocity width and inclination for NGC 1637 are quite uncertain because of its lopsidedness. Certainly, it would be very useful to have a precise Cepheid distance to NGC 1637, in order to further test the dilution factors of E96 and the EPM result.

The observations of SN 1999em and the EPM analysis of this paper demonstrate that it is possible to achieve EPM distances with internal precisions of 7% from optical observations. We are carrying out further tests of the external precision and accuracy of the method from the study of the Hubble diagram with SNe II well into the Hubble flow. When this study is complete, we expect to have a firm assessment of the performance of EPM. If we confirm the results found in this paper, the next step will be the observation of high-z SNe, an idea initially proposed by Wagoner (1977). As we have demonstrated, the cross-correlation technique will significantly extend the reach of EPM to higher redshifts, thus offering the possibility of obtaining a determination of the cosmological parameters completely independent of the results yielded by SNe Ia (Riess et al. 1998; Perlmutter et al. 1999).

5. CONCLUSIONS

1. We develop a technique for measuring accurate photospheric velocities by cross-correlating SN spectra with the models of E96. The application of this technique to SN 1999em shows that we can reach an average uncertainty of 11% in velocity from an individual spectrum. This approach will significantly extend the reach of EPM to higher redshifts.

2. Using the data of SN 1999em, we show that EPM is quite robust to the effects of dust. In particular, the distances derived from the $\{VI\}$ filter subset change by only 7% when the adopted visual extinction in the host galaxy is varied by 0.45 mag. Despite the weak sensitivity of EPM to dust, our analysis reveals that multicolor photometry (BVIJ) can be very useful in constraining the value of $A_{\rm host}(V)$. In particular, we find evidence for small $[A_{\rm host}(V) < 0.2]$ dust absorption in SN 1999em, in good agreement with the independent estimate of $A_{\rm host} \approx 0.03-0.18$ and $A_{\rm host} < 0.33$ from theoretical modeling of the spectra of this SN (Baron et al. 2000). These estimates are highly inconsistent with the value of $A_{\rm host} \sim 3.1 \pm 0.47$ implied by the equivalent width of the interstellar Na I D line measured from the SN spectrum.

3. EPM has the advantage that observations at different epochs are essentially independent distance measurements. The superb sampling of the BVIZJHK light curves of SN 1999em permits us to examine in detail the internal consistency of EPM. Our analysis shows that our first photometric and spectroscopic observation was obtained at an age of only 3 days after shock breakout, which is far earlier than any other SN, except for SN 1987A. Our tests show that the distances computed with the dilution factors of E96 prove even 50% lower than the average during the first week since explosion. We cannot rule out errors in the dilution factors as the source of the problem. It is conceivable that such error could be caused by circumstellar material, which could lead to the formation of the photosphere at a much larger radius. Over the following 65 days, on the other hand, our analysis lends strong credence to the models of E96, and confirms their prediction that the use of average dilution factors can produce consistent distances without having to craft specific models for each SN. The $\{VI\}$ filter subset shows the greatest internal consistency (with an average scatter of only 4%) and the least sensitivity to the adopted dust extinction, making it the most reliable route to cosmic distances. Our tests show that it is necessary to obtain light curves with reasonable spacing in time (once per week) in order to avoid systematic biases introduced by the use of average dilution factors. A few (5-10) points properly spaced over the plateau phase can produce distances with internal precisions of 4%-6%.

4. When comparing distances derived from the first 70 days of SN evolution, we find that those determined from $\{VJ, VH, VK\}$ appear to be 9% higher $(1-3 \sigma)$ than those yielded by the optical filter subsets $\{BV, VI, VZ\}$. Better IR data will be required in the future to ascertain whether this is a problem of this particular data set or a more general feature of the atmosphere models of E96. The average distance obtained from filter subsets {BV, VI, BVI, VZ, VJ, VH, VK, JHK} is $D_{1999em} = 7.5 \pm 0.5$ Mpc, where the quoted uncertainty (7%) is a conservative estimate of the internal precision based on the rms distance spread yielded by all these filter subsets. This EPM distance compares with the value of $7.8^{+1.0}_{-0.9}$ Mpc derived by Sohn & Davidge (1998) from the brightness of red supergiants in the host galaxy of SN 1999em. A Tully-Fisher distance of 9.7 ± 1.7 Mpc has been derived for this galaxy, which proves to be 1.3 σ larger than the EPM value. A more precise Cepheid distance to the host galaxy of SN 1999em would be very useful in order to test our results.

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APPENDIX A

THE EXPANDING PHOTOSPHERE METHOD

The expanding photosphere method (EPM) involves measuring a photometric angular radius and a spectroscopic physical radius from which a SN distance can be derived. Assuming that continuum radiation arises from a spherically symmetric photosphere, a photometric measurement of its color and magnitude determines its angular radius θ ,

$$\theta = \frac{R}{D} = \sqrt{\frac{f_{\lambda}}{\zeta_{\lambda}^2 \pi B_{\lambda}(T) 10^{-0.4A(\lambda)}}},$$
(A1)

where R is the photospheric radius, D is the distance to the supernova, $B_{\lambda}(T)$ is the Planck function at the color temperature of the blackbody radiation, f_{λ} is the apparent flux density, and $A(\lambda)$ is the dust extinction. The factor ζ_{λ} accounts for the fact that

a real supernova does not radiate like a blackbody at a unique color temperature. Its role (as defined in Appendix C) is to convert the observed angular radius into the photospheric angular radius, defined as the region of total optical depth $\tau = \frac{2}{3}$ or the last scattering surface. Since the continuum opacity in the optical and NIR is dominated by electron scattering, the opacity is gray, and the photospheric angular radius is independent of wavelength (E96). A measurement of the photospheric radius R can then convert this angular radius to the distance to the supernova. Because supernovae are strong point explosions, they rapidly attain a state of homologous expansion in which the radius at a time t is given by

$$R = R_0 + v(t - t_0), (A2)$$

where v is the photospheric velocity measured from spectral lines, t_0 is the time of explosion, and R_0 is the initial radius of the shell. Combining these equations, we get

$$\theta_i = \frac{R_0 + v_i(t_i - t_0)}{D},$$
 (A3)

where θ_i and v_i are the observed quantities measured at time t_i . Because the expansion is so rapid (typically ~10⁹ cm s⁻¹), R_0 rapidly becomes insignificant. Even for a large progenitor with $R_0 = 5 \times 10^{13}$ cm (2 times larger than the largest luminosity class I star known; van Belle et al. 1999), the initial radius is only 10% of the SN radius at an age of 5 days (and less at later times), so it is safe to use the following approximation for all but the first days:

$$\frac{\theta_i}{v_i} \approx \frac{(t_i - t_0)}{D} \,. \tag{A4}$$

This equation shows that photometric and spectroscopic data at two or more epochs are needed to solve for D and t_0 . Clearly, the determination of distances relies on our knowledge of ζ_{λ} . The SN atmosphere has a large ratio of scattering to absorptive opacity, a ratio that varies with wavelength because of line blanketing and varying continuous absorption. The result is that the photosphere, which lies at a larger radius than the thermalization depth where the color temperature is set, radiates less strongly than a blackbody at that temperature, and the color temperature itself depends on the photometric bands employed to measure it. The parameter ζ_{λ} is known as the "flux dilution correction," although it takes into account departures from a blackbody SN for all effects.

EPM was first applied to SNe II by Kirshner & Kwan (1974), assuming that SNe II emitted like perfect blackbodies $(\zeta_{\lambda} = 1)$. Schmidt et al. (1992) corrected this situation by computing dilution factors from SNe II atmosphere models and optical distance correction factors derived empirically from SN 1987A. Using this approach they computed distances to nine nearby SNe, from which they derived a value of the Hubble constant of 60 km s⁻¹ Mpc^{-1} . In a subsequent paper Schmidt et al. (1994) used preliminary values of the dilution factors computed by E96 (see below) and high-quality data obtained at CTIO in order to extend the Hubble diagram to z = 0.05. From 16 SNe they obtained a value of $H_0 = 73 \pm 6 \text{ km s}^{-1} \text{ Mpc}^{-1}$, in good agreement with the Tully-Fisher method.

A major step forward in the knowledge of the dilution factors was achieved by E96 from detailed NLTE models of SNe II-P encompassing a wide range in luminosity, density structure, velocity, and composition. They found that the most important variable determining ζ_{λ} was the effective temperature; for a given temperature, ζ_{λ} changed by only 5%–10% over a very large variation in the other parameters.

One great advantage of distances determined by EPM is that they are independent of the "cosmic distance ladder." Observations at two epochs and a physical model for the supernova atmosphere lead directly to a distance. Moreover, additional observations of the same supernova are essentially independent distance measurements as the properties of the photosphere change over time. This provides a valuable *internal* consistency check.

APPENDIX B

THE COMPUTATION OF SYNTHETIC MAGNITUDES

The implementation of EPM requires fitting the observed SN magnitudes to those of a blackbody, from which the color temperature and the angular radius of the SN can be obtained. This process involves synthesizing broadband magnitudes from Planck spectra. It is crucial, therefore, to place the synthetic magnitudes on the same photometric system employed in the observations of the SN.

Since the SN magnitudes are measured with photon detectors, a synthetic magnitude is the convolution of the object's photon number distribution $(N_{\lambda} = F_{\lambda} \lambda/hc)$ with the filter transmission function $[S(\lambda)]$, i.e.,

$$mag = -2.5 \log_{10} \int N_{\lambda} A(\lambda) S(\lambda) d\lambda + ZP , \qquad (B1)$$

where ZP is the zero point for the magnitude scale and $A(\lambda)$ is the factor that accounts for the attenuation of the stellar flux due to interstellar dust absorption (in this paper we adopt the extinction law of Cardelli, Clayton, & Mathis 1989 for $R_V = 3.1$). For an adequate use of equation (B1), $S(\lambda)$ must include the transparency of the Earth's atmosphere, the filter transmission, and the detector quantum efficiency (QE). For BVRI we adopt the filter functions B_{90} , V_{90} , R_{90} , and I_{90} published by Bessell (1990). However, since these curves are meant for use with energy and not photon distributions (see Appendix in Bessell 1983), we must divide them by λ before employing them in equation (B1). Also, since these filters do not



FIG. 18.—BVRI filters functions of Bessell (1990) meant for use with energy distributions (dotted curves). Solid lines show the curves modified for use with photon distributions, to which we added the telluric lines.

include the atmospheric telluric lines, we add these features to the R and I filters (in B and V there are no telluric features), using our own atmospheric transmission spectrum. Figure 18 shows the resulting curves. For the Z filter we use the transmission curve of filter 611 and the QE of CCD TEK36 of the NTT/EMMI instrument. We include the telluric lines, but we ignore continuum atmospheric opacity, which is very small at these wavelengths. For JHK we use the J_S , H, and K_S filter transmissions tabulated by Persson et al. (1998), a nominal NICMOS2 QE, and the IR atmospheric transmission spectrum (kindly provided to us by J. G. Cuby). Figure 19 shows the resulting ZJHK filter functions, along with the corresponding detector QEs.

The ZP in equation (B1) must be determined by forcing the synthetic magnitude of a star to match its observed magnitude. We use the spectrophotometric calibration of Vega published by Hayes (1985) in the range 3300-10405 Å and the V magnitude of 0.03 mag measured by Johnson et al. (1966), from which we solve for the ZP in the V band. In principle, we can use the same procedure for *BRI*, but Vega's photometry in these bands is not very reliable, since it was obtained in the old



FIG. 19.—Z, J_s, H, K_s filter functions. Also shown are the QE of TEK36 and NICMOS2 that we employed to construct these functions.



FIG. 20.—Adopted spectrophotometric calibration for Vega. In the optical ($\lambda \le 10500$ Å), the calibration is from Hayes (1985), and at longer wavelengths we adopted the Kurucz spectrum with parameters $T_{\text{eff}} = 9400$ K, log g = 3.9, [Fe/H] = -0.5, $V_{\text{microturb}} = 0$.

Johnson standard system. To avoid these problems, we employ 10 stars with excellent spectrophotometry (Hamuy et al. 1994) and photometry in the modern Kron-Cousins system (Cousins 1971, 1980, 1984). Before using these standards we remove the telluric lines from the spectra, since the filter functions already include these features. With this approach we obtain an average and more reliable zero point for the synthetic magnitude scale with rms uncertainty of ~ 0.01 mag. With these ZPs we find that the synthetic magnitudes of Vega are brighter than the observed magnitudes (Johnson et al. 1966) by 0.016 mag in *B*, 0.025 in *R*, and 0.023 in *I* (Table 12), which is not so disappointing considering that this comparison requires transforming the Johnson *RI* magnitudes to the Kron-Cousins system (Taylor 1986).

In our Z photometric system Vega has a magnitude of 0.03. Note that this value is not the result of a measurement but, instead, of defining the zero point for the Z photometric system to give V - Z = 0 for Vega (Appendix D).

At longer wavelengths, where no continuous spectrophotometric calibration is available for Vega (or any other star), we adopt the solar model of Kurucz with the parameters $T_{eff} = 9400$ K, log g = 3.9, [Fe/H] = -0.5, and $V_{microturb} = 0$ (see Cohen et al. 1992 for a detailed description of the model and Gray & Corbally 1994 for the calibration of the MK spectral system). After flux-scaling this model and bringing it into agreement with the V = 0.03 magnitude of Vega, the model matches the Hayes calibration at the level of 1% or better over the *BVRI* range, lending credence to the calibration assumed for longer wavelengths. Figure 20 shows the adopted spectrophotometric calibration for Vega in the optical and IR. To calculate the zero points in *JHK*, we adopt the magnitude of Vega in the CIT photometric system (Elias et al. 1982), namely, 0.00 mag at all wavelengths. The original CIT system comprises stars of 4th-7th magnitude. It has been recently extended by Persson et al. (1998) to fainter standards, which are the stars we used for the calibration of the *JHK* light curves of SN 1999em.

Table 12 summarizes the zero points computed with equation (B1), and the corresponding magnitudes for Vega in such system. For the proper use of these ZPs it is necessary to express F_{λ} in ergs s⁻¹ cm⁻² Å⁻¹, λ in Å, and the physical constants c and h in cgs units. From the 10 secondary standards we estimate that the uncertainty in the zero points is ~0.01 mag in *BVRI*. At longer wavelengths the zero points are more uncertain, since they come from the adopted model energy distribution of Vega, which is probably accurate to better than 5%.

Following E96, we proceed to compute $b_{\bar{\lambda}}(T)$, the magnitude of $\pi B_{\lambda}(T)$ for a filter with central wavelength $\bar{\lambda}$, to which we fit a polynomial of the form

$$b_{\bar{\lambda}}(T) = \sum_{i=0}^{5} c_i(\lambda) \left(\frac{10^4 \text{ K}}{T}\right)^i \tag{B2}$$

| Source | В | V | R | Ι | Ζ | J_S | Н | K _s |
|------------|---------|---------|---------|---------|---------|---------|---------|----------------|
| Zero point | 35.287 | 34.855 | 35.060 | 34.563 | 32.724 | 32.230 | 32.098 | 32.175 |
| Vega | 0.014 | 0.030 | 0.042 | 0.052 | 0.030 | 0.00 | 0.00 | 0.00 |
| Sun | -26.083 | -26.752 | -27.120 | -27.451 | -27.592 | -27.918 | -28.243 | -28.285 |

 TABLE 12

 Photometric Zero Points and Synthetic Magnitudes for Vega and the Sun

| i | $c_i(B)$ | $c_i(V)$ | $c_i(R)$ | $c_i(I)$ | $c_i(Z)$ | $c_i(J_s)$ | $c_i(H)$ | $c_i(K_s)$ |
|---|----------|----------|----------|----------|----------|------------|----------|------------|
| 0 | -45.144 | -44.766 | -44.597 | -44.345 | -44.232 | -43.913 | -43.767 | -43.638 |
| 1 | 7.159 | 6.793 | 6.628 | 6.347 | 6.262 | 6.022 | 5.878 | 5.737 |
| 2 | -4.301 | -4.523 | -4.693 | -4.732 | -4.810 | -4.859 | -4.914 | -4.881 |
| 3 | 2.639 | 2.695 | 2.770 | 2.739 | 2.778 | 2.772 | 2.797 | 2.757 |
| 4 | -0.811 | -0.809 | -0.831 | -0.811 | -0.825 | -0.819 | -0.829 | -0.813 |
| 5 | 0.098 | 0.096 | 0.099 | 0.096 | 0.098 | 0.097 | 0.098 | 0.096 |
| | | | | | | | | |

NOTE.— $b_{\bar{\lambda}}(T) = \sum_{i} c_{i}(\lambda) T_{4}^{-i}, T_{4} = T/10^{4} \text{ K}.$

in the range 4000 < T < 25,000 K. We choose this high order so that the residuals in magnitude are always below 0.01 mag. Table 13 gives the resulting coefficients $c_i(\lambda)$. From these fits it is straightforward to compute the color temperature from any combination of magnitudes. Figure 21 (top) illustrates some of these temperature-color curves. Note that, as expected, all these curves intersect at $T \sim 10,000$ K, which corresponds to the temperature of Vega, which has nearly zero colors at all wavelengths. The bottom panel shows the temperature difference between our calibration and that of E96. This comparison reveals that significant differences in color temperatures can be obtained depending on the photometric system adopted. The disagreement is particularly large at high temperatures, where a small difference in color translates into a large variation in temperature.

APPENDIX C

THE DILUTION FACTORS IN OUR PHOTOMETRIC SYSTEM

Figure 21 reveals that, in order to use our photometric system, it is not possible to use the dilution factors published by E96, since these were computed in a different photometric system. We proceed now to recompute ζ_{λ} in our photometric system from the model spectra of E96. The calculation consists of fitting the models with blackbody curves, $B_{\lambda}(T_s)$, and solving for color temperature, $T_{\rm s}$, and dilution correction factor, $\zeta_{\rm s}$, by minimizing the quantity

$$\sum_{\bar{\lambda} \in S} \left[M_{\bar{\lambda}} + 5 \log \left(\frac{R_{\rm ph}}{10 \, {\rm pc}} \right) + 5 \log \zeta_S - b_{\bar{\lambda}}(T_S) \right]^2, \tag{C1}$$

where $M_{\bar{\lambda}}$ is the broadband absolute magnitude of the atmosphere model for a filter with central wavelength $\bar{\lambda}$, R_{ph} is the photospheric radius, $b_{\bar{\lambda}}(T_S)$ is the synthetic magnitude of $\pi B_{\lambda}(T_S)$, and S is the filter combination used to fit the atmosphere models with blackbody curves, i.e., $S = \{BV\} = \{VI\} = \{BVI\} = \cdots$. As explained in Appendix A, the term "photosphere" corresponds to the last scattering surface that is independent of wavelength in the optical and NIR.



FIG. 21.— (a) Relation between color temperature and four different colors in our photometric system. (b) Difference in color temperature between our calibration and that of E96.



FIG. 22.—Dilution factors ζ computed from E96 atmosphere models vs. color temperature derived from eight different filter subsets. The solid lines correspond to a polynomial fit to $\zeta(T_s)$, from which three deviant models (crosses) are removed.

Figure 22 shows the resulting ζ_s factors for eight filter combinations. The differences between the new dilution factors and those of E96 are less than 5% and, not surprisingly, we recover the result that ζ_s is primarily determined by temperature. For convenience, therefore, we perform polynomial fits to $\zeta_s(T_s) \approx z(T_s)$, where

$$z(T_S) = \sum_{i=0}^{2} a_{S,i} \left(\frac{10^4 \text{ K}}{T_S} \right)^i.$$
 (C2)

Table 14 gives the resulting coefficients $a_{S,i}$ for nine filter subsets, and in Figure 22 we compare these fits to the individual ζ_S factors. Following E96, we remove the peculiar models s15.5.1, s25.5.1, and h10.30.1 (shown with crosses), since they are not appropriate models for SNe II-P.

| | TABLE 1 | 14 | | |
|-----------------|-----------------------|-----------------------|-----------------------|-----------------------|
| | Fits to ζ(| T_{s}) | | |
| S | <i>a</i> ₀ | <i>a</i> ₁ | <i>a</i> ₂ | σ^{a} |
| <i>BV</i> } | 0.7557 | -0.8997 | 0.5199 | 0.048 |
| <i>BV1</i> } | 0.7336 | -0.6942 | 0.3740 | 0.027 |
| <i>VI</i> } | 0.7013 | -0.5304 | 0.2646 | 0.029 |
| VZ } | 0.8185 | -0.7137 | 0.3510 | 0.031 |
| <i>VJ</i> | 0.6104 | -0.0323 | 0.0000 | 0.025 |
| <i>VH</i> } | 0.6548 | -0.0737 | 0.0000 | 0.031 |
| <i>VK</i> } | 1.2865 | -0.8571 | 0.2700 | 0.051 |
| JHK} | 1.4787 | -0.4799 | 0.0000 | 0.046 |
| <i>BVIJHK</i> } | 1.1551 | -0.9790 | 0.3913 | 0.024 |
| - | | | | |

NOTE.— $\zeta(T_s) = \sum_i a_{s,i} (10^4 \text{ K}/T_s)^i$. ^a σ is the rms of the fit.

APPENDIX D

THE Z-BAND PHOTOMETRIC SYSTEM

We define the Z band as the product of the transmission of the Z filter (number 611) and the QE of CCD TEK36 of the NTT/EMMI instrument. The resulting bandpass also includes telluric lines (see Fig. 19). We employ this filter function to compute synthetic magnitudes from the tertiary spectrophotometric standards published by Hamuy et al. (1994). However, since these spectra contain telluric lines it is necessary first to remove these features. Then we use equation (B1) and an *adopted* ZP of 32.724 that yields a magnitude of 0.03 for Vega. We choose this ZP so that V - Z = 0 for Vega. The resulting synthetic magnitudes for the tertiary standards are listed in Table 15, and this is the system relative to which we calibrated a photometric sequence around SN 1999em. In Hamuy et al. (1994) we showed that synthetic magnitudes in the I band had typical uncertainties of 0.018 mag. Therefore, we believe that the Z magnitudes in Table 15 have errors of 0.02 mag.

| Standard Stars for the Z Band | | | | | |
|---------------------------------|---------------|--|--|--|--|
| Star | $Z \pm 0.020$ | | | | |
| LTT 377 | 10.523 | | | | |
| LTT 1020 | 10.648 | | | | |
| EG 21 | 11.619 | | | | |
| LTT 1788 | 12.369 | | | | |
| LTT 2415 | 11.526 | | | | |
| Hiltner 600 | 10.132 | | | | |
| L745-46A | 12.670 | | | | |
| LTT 3218 | 11.652 | | | | |
| LTT 3864 | 11.374 | | | | |
| LTT 4364 | 11.181 | | | | |
| Feige 56 | 11.154 | | | | |
| LTT 4816 | 13.792 | | | | |
| CD -32 | 10.041 | | | | |
| LTT 6248 | 10.966 | | | | |
| EG 274 | 11.359 | | | | |
| LTT 7379 | 9.376 | | | | |
| LTT 7987 | 12.437 | | | | |
| LTT 9239 | 11.144 | | | | |
| Feige 110 | 12.249 | | | | |
| LTT 9491 | 14.071 | | | | |

TABLE 15

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